# QCD corrections to Heavy Quarkonium Production

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### Plan

- Inclusive quarkonium production at the Tevatron
- Associated production at the Tevatron
- Conclusion

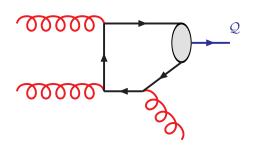
### Naïve non-relativistic approach: the CS

non-perturbative effects are factorized in the wave function

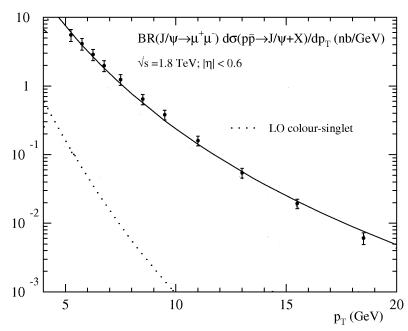
$$\sigma(ij \to QX) \approx \hat{\sigma} \left( (ij \to Q\bar{Q} + X) \right) |\psi(0)|^2$$

- $\hat{\sigma}(ij \to Q\bar{Q} + X)$  : creation of an on-shell  $Q\bar{Q}$  pair (perturbative expansion)
- $\psi(0)$  : Schrödinger wave function at the origin (non-perturbative parameter)
- the  $Q \bar Q$  pair is created with the same quantum numbers as the physical bound state
- this model is very predictive

### At LO in $\alpha_s$ and v



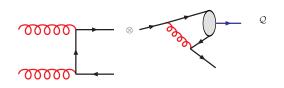
$$\frac{\frac{d}{dP_T^2}\hat{\sigma}(gg \to Q\bar{Q}(^3S_1^{[1]})g)|\psi(0)|^2}{\sim \alpha_s^3 \frac{1}{P_T^8}}$$



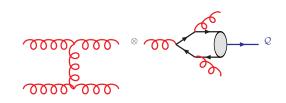
wrong  $P_T$  spectrum wrong normalization

[from M. Kramer, Prog. Part. Nucl. Phys. 47: 141-201,2001. experimental data: F. Abe et al (CDF collaboration), Phys. Rev. Lett. 79 (1997)]

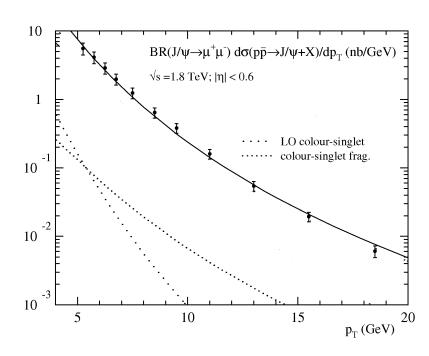
### Frag. contribution (higher order in $\alpha_s$ )



$$\frac{d}{dP_T^2}\hat{\sigma}(gg \to Q\bar{Q}) \otimes D(Q \to \mathcal{Q}(^3S_1^{[1]}) + Q) + \mathcal{O}(\frac{m_Q}{P_T})$$
$$\sim \alpha_s^4 \frac{1}{P_T^4}$$



$$\frac{\frac{d}{dP_T^2}\hat{\sigma}(gg \to gg) \otimes D(g \to \mathcal{Q}(^3S_1^{[1]}) + gg) + \mathcal{O}(\frac{m_Q}{P_T})}{\sim \alpha_s^5 \frac{1}{P_T^4}}$$



 $P_T$  shape is right wrong normalization

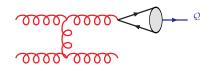
### **NRQCD** expansion

 non-pertubative effects are factorized into long distance matrix elements (LDME)

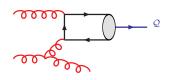
$$\sigma(ij \to Q + X) \sim \sum_{n} \hat{\sigma}_{\Lambda}(ij \to Q\bar{Q}(n) + X) \langle \mathcal{O}^{Q}(n) \rangle_{\Lambda}$$

- $\hat{\sigma}(i+j \to Q\bar{Q}(n)+X)$  is the short distance cross section
- $\langle \mathcal{O}^{\mathcal{Q}}(n) \rangle$  is the long distance matrix element their importance can be assessed using power counting rules
- $_{\bullet}$  sum over all possible quantum states n of intermediate  $Q\bar{Q}$  pair
- the LDME are a priori unknown

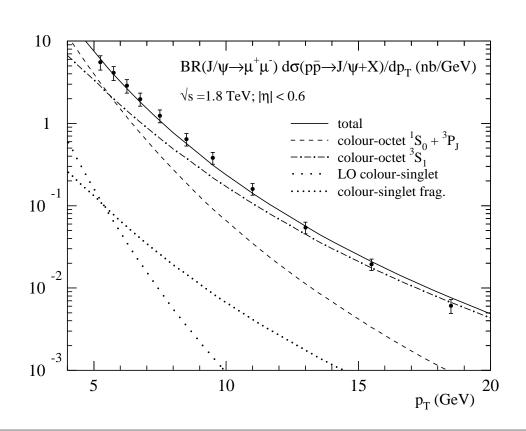
### **Consequence: color-octet transition**



$$\frac{d}{dP_T^2}\hat{\sigma}(gg \to gQ\bar{Q}(^3S_1^{[8]}))\langle \mathcal{O}^{\mathcal{Q}}(^3S_1^{[8]})\rangle \sim \alpha_s^3 \frac{1}{P_T^4} v^4$$



$$\frac{d}{dP_T^2}\hat{\sigma}(gg \to Q\bar{Q}(^1S_0^{[8]}) + g)\langle \mathcal{O}^{\mathcal{Q}}(^1S_0^{[8]})\rangle \sim \alpha_s^3 \frac{(2m_c)^2}{P_T^6} v^4$$



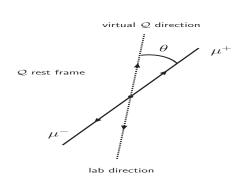
Fit of the color-octet LDME to reproduce the data

### $J/\psi$ production at the Tevatron

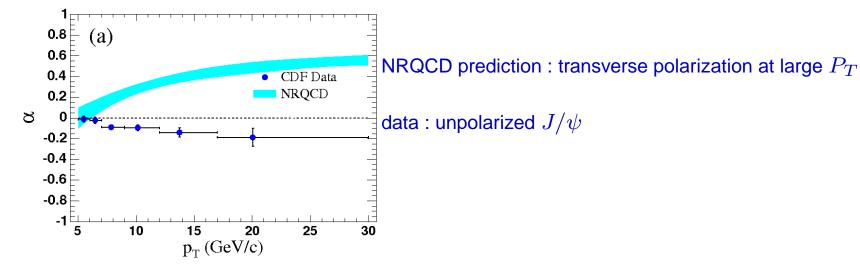
extracted from the angular distribution of the produced leptons

$$I(\cos \theta) = \frac{3}{2(\alpha+3)} (1 + \alpha \cos^2 \theta)$$

$$\alpha = \frac{\sigma_T - 2\sigma_L}{\sigma_T + 2\sigma_L}$$



CDF data and NRQCD prediction for the prompt polarization



[from A. Abulencia et al (CDF collaboration), hep-ex/07040638]

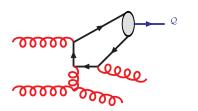
### **Appraisal**

- Open questions :
  - role of the color-octet mechanism is not clear up to now (polarization problem)
  - Universality of the long distance matrix elements is not well established
- further possible studies :
  - higher order corrections in  $\alpha_s$  to the inclusive production
  - more exclusive signatures to disentangle the various transitions

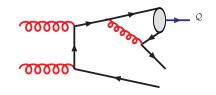
# NLO correction to CS $J/\psi$ production

[F. Maltoni, J. Campbell, F. Tramontano 2007]

#### new channels :

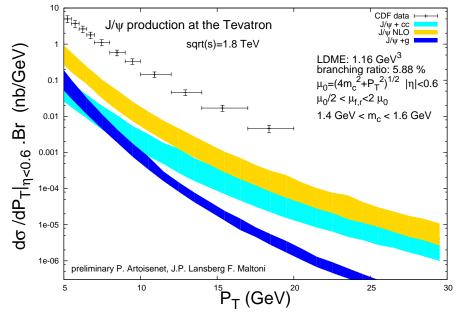


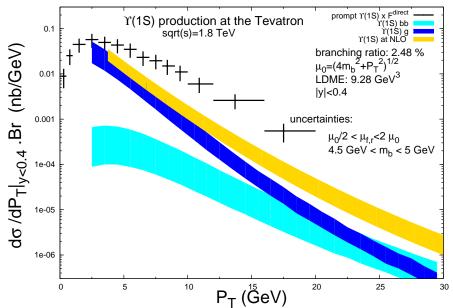
$$\sim \alpha_s^4 \frac{1}{P_T^6}$$



$$\sim \alpha_s^4 \frac{1}{P_T^4}$$

#### comparison with the data



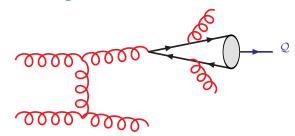


### What is missing?

We need new contributions with a more gentle  $P_T$  spectrum  $(\frac{1}{P_T^4})$ 

At  $\alpha_s^5$ , we have both

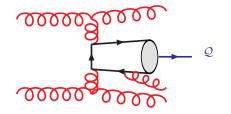
1. fragmentation channel



estimated in the

fragmentation approximation

2. high-energy enhanced channel



estimated in the

 $k_t$  factorization

These channels should dominate at large  $P_T$ 

technical difficulties :  $p\bar{p} \rightarrow \mathcal{Q} + 3$  jets is challenging subprocesses:

da uuur dhhar 2011
dg_uuxdbbx3S11
uxu_ddxgbbx3S11
uxd_uxdgbbx3S11
ug_uuuxbbx3S11
gux_uxggbbx3S11
gu_uddxbbx3S11
gu_uggbbx3S11

```
gd_uuxdbbx3S11
du_udgbbx3S11
uxu_gggbbx3S11
uxdx_uxdxgbbx3S11 uxu_uuxgbbx3S11
uu_uugbbx3S11
ud_udgbbx3S11
udx_udxgbbx3S11
```

uux\_uuxgbbx3S11 ug\_uggbbx3S11 gux\_uxddxbbx3S11 gg\_uuxgbbx3S11 dxux\_uxdxgbbx3S11

• technical difficulties :  $p\bar{p} \to \mathcal{Q} + 3$  jets is challenging

#### subprocesses:

```
uux_uuxgbbx3S11
dg_uuxdbbx3S11
                 gd_uuxdbbx3S11
                                    gu_uuuxbbx3S11
                                                     ug_uddxbbx3S11
uxu_ddxgbbx3S11
                 du_udgbbx3S11
                                    gdx_uuxdxbbx3S11_oux_uuxuxbbx3S11_
                                                                       ug_uggbbx3S11
                 uxu_gggbbx3S11
                                    dux_uxdgbbx3S11 gg_gggbbx3S11
                                                                       gux_uxddxbbx3S11
uxd_uxdgbbx3S11
                 uxdx_uxdxgbbx3S11
                                   uxu_uuxgbbx3S11 dxg_uuxdxbbx3S11
                                                                        gg_uuxgbbx3S11
ug_uuuxbbx3S11
                 uu_uugbbx3S11
                                    uxg_uuxuxbbx3S11 uxux_uxuxgbbx3S11 dxu_udxgbbx3S11
gux_uxggbbx3S11
                                    uux_ddxgbbx3S11
gu_uddxbbx3S11
                 ud_udgbbx3S11
                                                     uxg_uxddxbbx3S11
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                                    uux_gggbbx3S11
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```

pprox 2000 Feynman diagrams (reduced by a factor  $\frac{1}{4}$  after the colour and spin projections are applied)

• technical difficulties :  $p \bar{p} o \mathcal{Q} + 3$  jets is challenging

#### subprocesses:

```
dg_uuxdbbx3S11
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                                                                       uux_uuxgbbx3S11
uxu_ddxgbbx3S11
                 du_udgbbx3S11
                                    gdx_uuxdxbbx3S11_oux_uuxuxbbx3S11_
                                                                       ug_uggbbx3S11
                                    dux_uxdgbbx3S11 gg_gggbbx3S11
                                                                       gux_uxddxbbx3S11
uxd_uxdgbbx3S11
                 uxu_gggbbx3S11
                                   uxu_uuxgbbx3S11 dxg_uuxaxbbx3S11
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ug_uuuxbbx3S11
                 uxdx_uxdxgbbx3S11
                                    uxg_uuxuxbbx3S11 uxux_uxuxgbbx3S11 dxu_udxgbbx3S11
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                                    uux_ddxgbbx3S11
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                 udx_udxgbbx3S11
```

pprox 2000 Feynman diagrams (reduced by a factor  $\frac{1}{4}$  after the colour and spin projections are applied)

How can we deal with it?

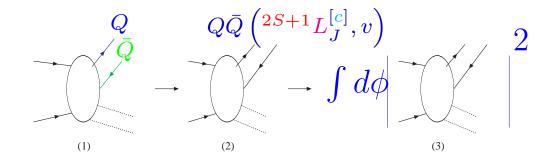
• technical difficulties :  $p\bar{p} \to \mathcal{Q} + 3$  jets is challenging subprocesses :

```
uux_uuxgbbx3S11
dg_uuxdbbx3S11
                gd_uuxdbbx3S11
                                  gu_uuuxbbx3S11
                                                  ug_uddxbbx3S11
uxu_ddxgbbx3S11
                du_udgbbx3S11
                                  gdx uuxdxbbx3S11 gux uuxuxbbx3S11
                                                                   ug uggbbx3S11
                uxu_gggbbx3S11
                                  dux_uxdgbbx3S11 gg_gggbbx3S11
                                                                   gux_uxddxbbx3S11
uxd_uxdgbbx3S11
                uxdx_uxdxgbbx3S11
                                 gg_uuxgbbx3S11
ug_uuuxbbx3S11
                uu uugbbx3S11
                                  uxg uuxuxbbx3S11 uxux uxuxgbbx3S11
                                                                    dxu udxgbbx3S11
gux_uxggbbx3S11
gu_uddxbbx3S11
                ud_udgbbx3S11
                                  uux_ddxgbbx3S11
                                                  uxg_uxddxbbx3S11
                                                                    dxux_uxdxgbbx3S11
gu_uggbbx3S11
                udx_udxgbbx3S11
                                  uux_gggbbx3S11
                                                  uxg_uxggbbx3S11
```

pprox 2000 Feynman diagrams (reduced by a factor  $\frac{1}{4}$  after the colour and spin projections are applied)

How can we deal with it?

Solution: MadOnia (automatic tree-level computation of quarkonium amplitude) [P. A., F. Maltoni, T. Stelzer 2008]



- (1) open quark amplitude (MadGraph)
- (2) projected amplitude (MadOnia)
- (3) phase-space integration

• Physical difficulties : IR divergences in  $p\bar{p} \to \Upsilon + 3jets$  To cut the IR divergences, we impose

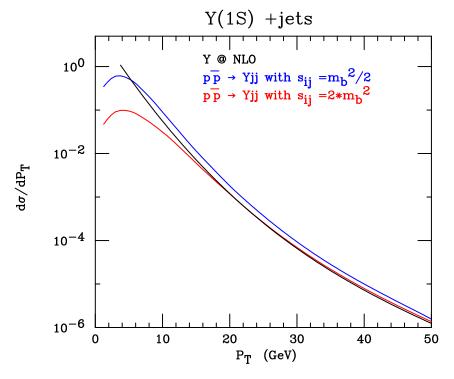
$$s_{i,j} > x \ m_b^2$$

At large  $P_T$ , the dependence in this cut is expected to be small, as

$$\frac{d\sigma}{dP_T} = \frac{c_1}{P_T^8} \log \frac{P_T^2}{xm_b^2} + \frac{c_2}{P_T^6} \log \frac{P_T^2}{xm_b^2} + \frac{c_3}{P_T^4}$$

### Check of this approach with the NLO

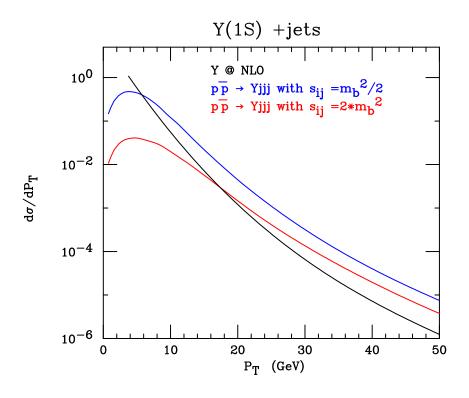
•  $p \bar{p} 
ightarrow \Upsilon$  +2 jets versus full NLO



- ullet very small band at large  $P_T$
- ullet good agreement with the full NLO at large  $P_T$

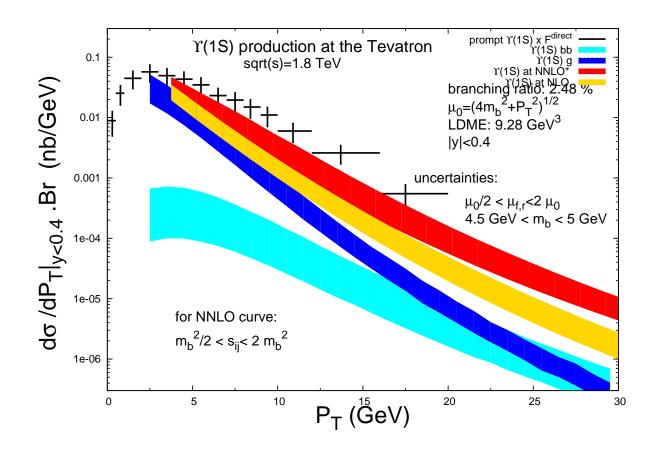
### Check of this approach with the NLO

•  $p \bar{p} \to \Upsilon$  +3 jets



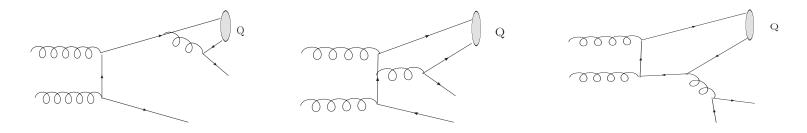
- ullet the width of the band (slowly) decreases with  $P_T$
- ullet the contribution  $\Upsilon+3$  jets dominates over the NLO yield at large  $P_T$

# $\alpha_s^5$ contributions to $\Upsilon(1S)$ production



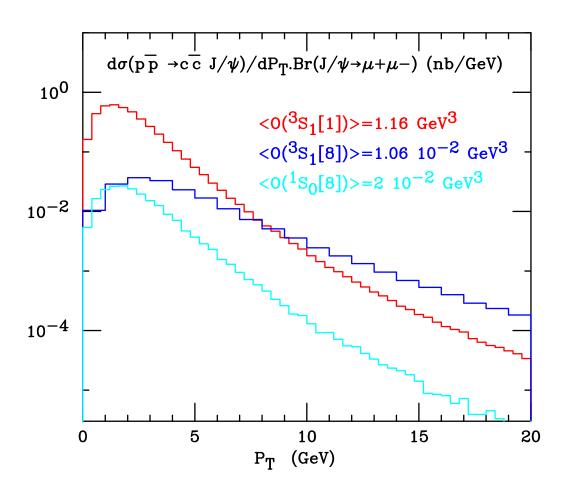
### **Associated production**

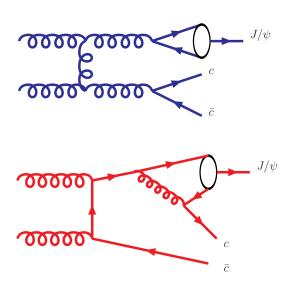
• Analysis of the  $J/\psi$  production in association with a charm quark pair [P. A., J.P. Lansberg, F. Maltoni 2007]



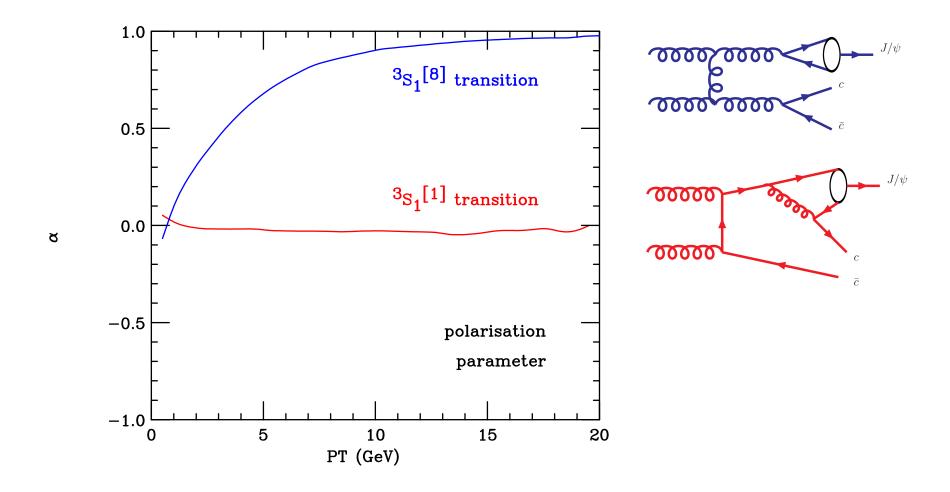
- full calculation includes topologies that are not taken into account in the fragmentation approximation
- theoretical prediction for this channel can be tested experimentally
- new signature to study the various transitions and assess the universality of LDME

### $P_T$ spectrum

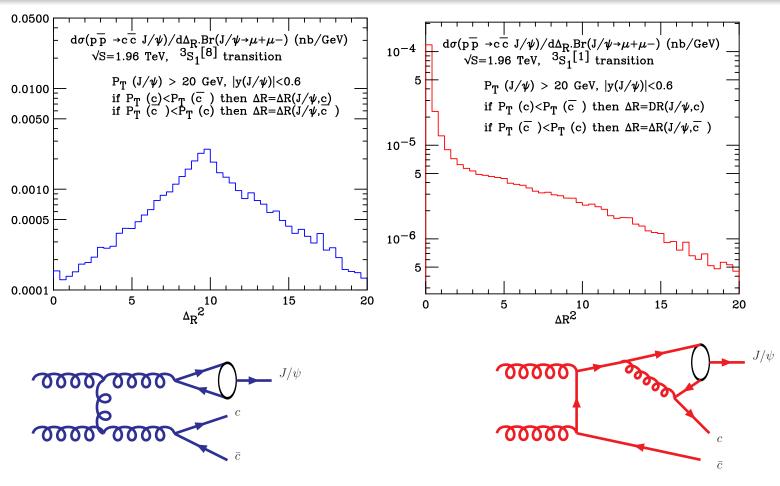




### **Polarization**



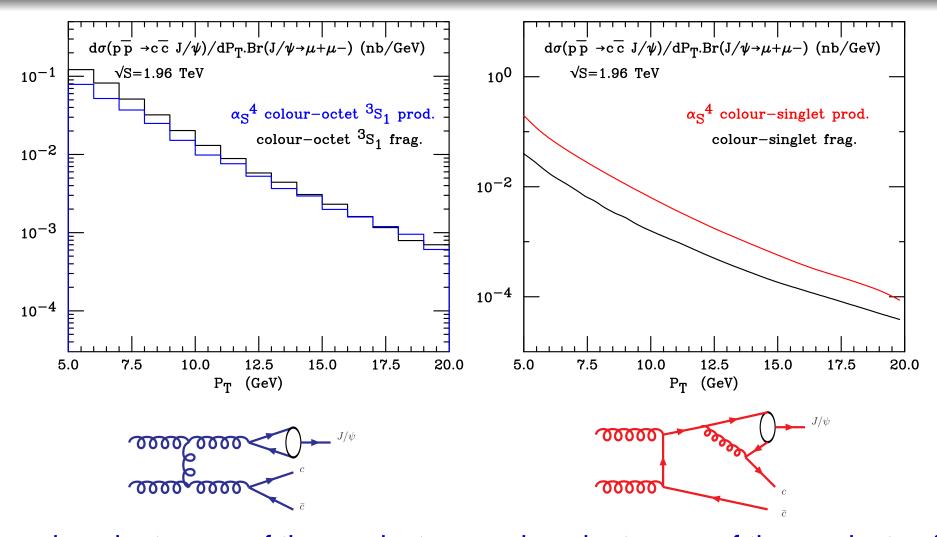
### **Charmed meson distribution**



the softest charmed meson recoils against the  $J/\psi$ 

the softest charmed meson moves along with the  $J/\psi$ 

## Fragmentation approximation



invariant mass of the products of fragmentation is  $2m_c$ 

invariant mass of the products of fragmentation is larger then  $3m_c$ 

### **Conclusion**

- $J/\psi$  production at the Tevatron
  - inclusion of higher order correction in  $\alpha_s$  reduces the discrepancy between the color-singlet yield and the data, but there is still a gap
  - the associated production  $p\bar p\to J/\psi c\bar c$  is an interesting signature to study the production mechanisms
- $\Upsilon(1S)$  production at the Tevatron
  - with the inclusion of higher order correction in  $\alpha_s$ , the color-singlet mechanism reproduces the data (with a large uncertainty)
  - the color-singlet yield has a longitudinal polarization