

SISCone

A Seedless Infrared-Safe Cone jet algorithm

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code available at `http://projects.hepforge.org/siscone`
or as a FastJet plugin (`http://www.lpthe.jussieu.fr/~salam/fastjet`)

- Cone jet algorithms
- Infrared-Safety issues:
 - Why is this mandatory ?
 - IR unsafety of the midpoint algorithm
- SIScone: a practical solution
- Physical consequences:
 - Algorithm speed
 - Inclusive jet spectrum
 - Jet mass spectrum in multi-jet events
- Conclusions

Cone jet algorithms

- Given: set of N particles with their 4-momentum
- Quest: clustering those particles into jets
- Idea: jets \equiv cones around dominant energy flows

for a cone of radius R in the (y, ϕ) plane, **stable cones** are such that:
centre of the cone \equiv direction of the total momentum of its particles

- Algorithm: **Tevatron Run II**
 - Step 1: find **ALL** stable cones of radius R
 - Step 2: run a split-merge procedure with overlap f
to deal with overlapping stable cones
- This talk: **Why** finding **all** stable cones and **how**.
→ C++ implementation: **Seedless Infrared Safe Cone algorithm (SISCone)**

Midpoint cone algorithm

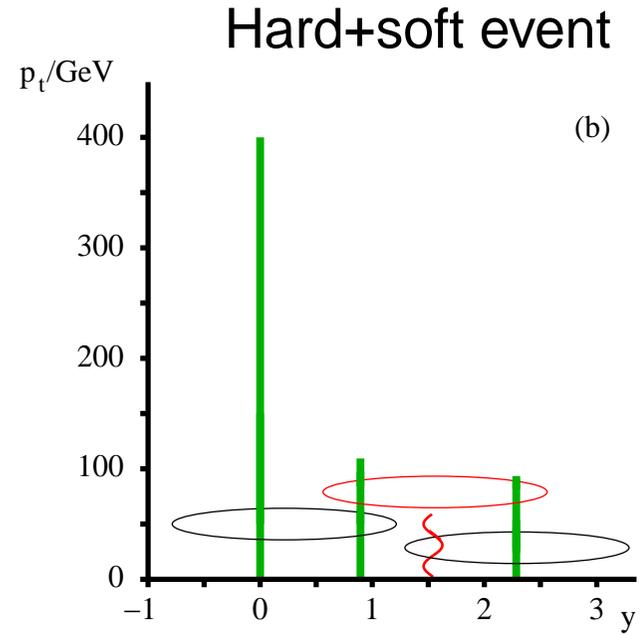
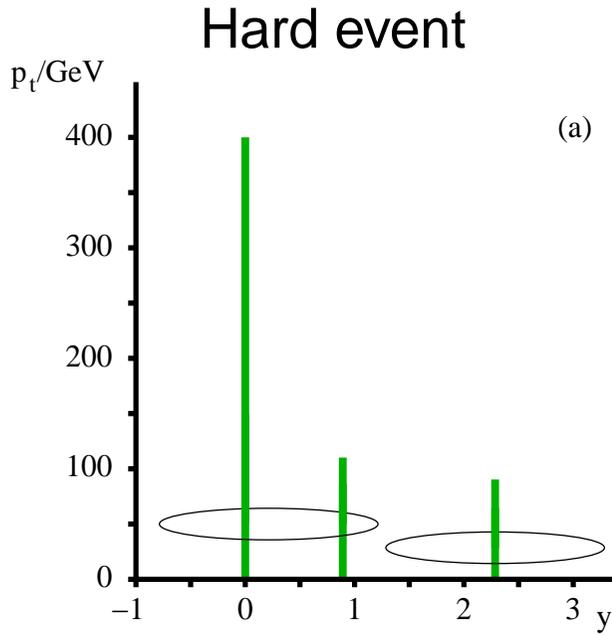
Usual **seeded** method to search stable cones: **midpoint cone algorithm**

- **For an initial seed**
 1. sum the momenta of all particles within the cone centred on the seed
 2. use the direction of that momentum as new seed
 3. repeat 1 & 2 until stable state cone reached
- **Sets of seeds:**
 1. All particles (above a p_t threshold s)
 2. **Midpoints** between stable cones found in 1.

Problems:

- **the p_t threshold s is collinear unsafe**
- **seeded approach \Rightarrow stable cones missed \Rightarrow infrared unsafety**

Midpoint IR Unsafety



Stable cones:

Midpoint: {1,2} & {3}

Seedless: {1,2} & {3} & {2,3}

{1,2} & {3} & {2,3}

{1,2} & {3} & {2,3}

Jets: ($f = 0.5$)

Midpoint: {1,2} & {3}

Seedless: {1,2,3}

{1,2,3}

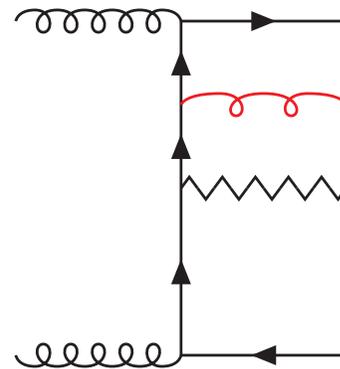
{1,2,3}

→ IR unsafety of the midpoint algorithm

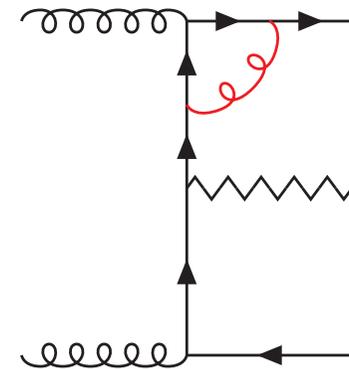
Infrared Safety: Why ?

Ellipsis: IR safety, i.e. stability upon emission of soft particles, is required for perturbative computations to make sense!

Cancellation of IR divergences between real and virtual emissions of SOFT gluons



NLO, real



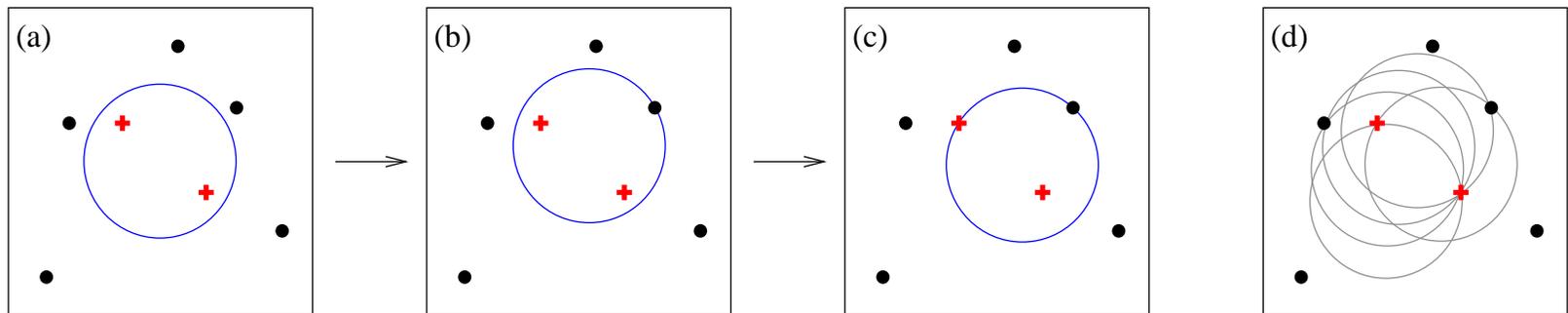
NLO, virtual

- IF Jet clustering is different in both cases, THEN the cancellation is not done and the result is not consistent with pQCD
- **Stable cones must not change upon addition of soft particles**
- Divergence at NLO is parametrically of the same order as LO contribution

SISCone: seedless solution

- Naive approach: check stability of each subset of particle
Complexity is $\mathcal{O}(N2^N)$ *i.e.* definitely unrealistic (10^{17} years for $N = 100$)

- Idea: all enclosures are defined by a **pair of points**

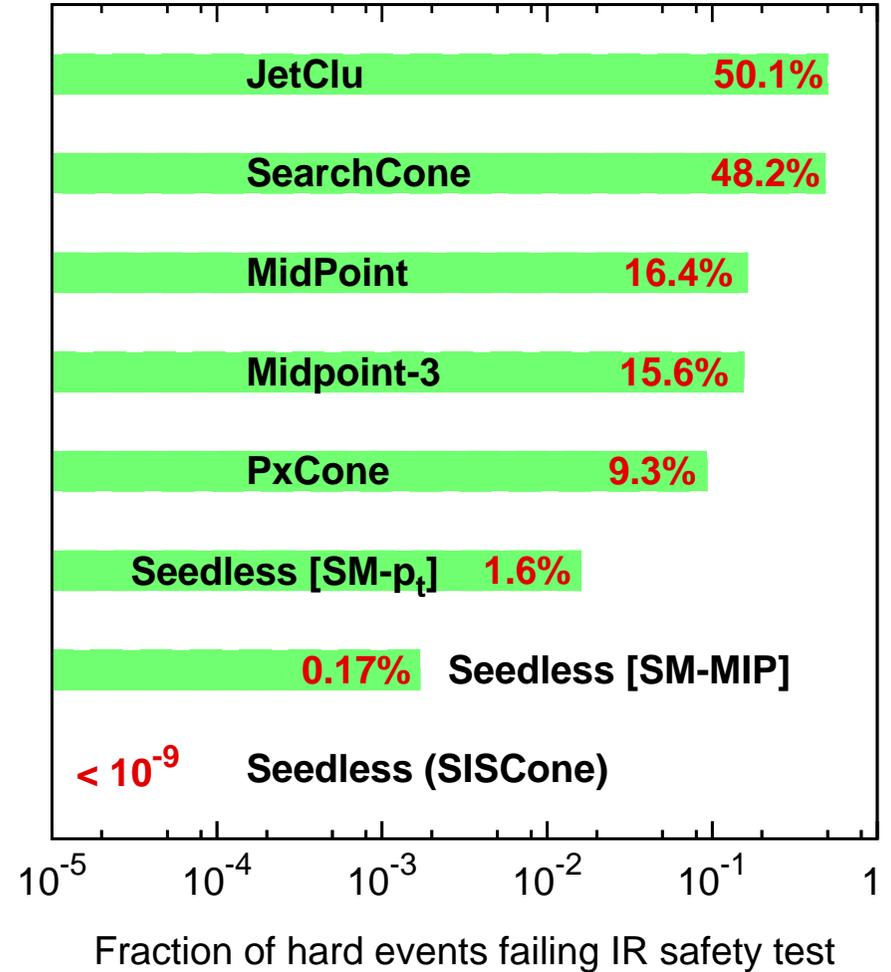


- Tricks: e.g. traversal order to avoid recomputation of the cone content
- Complexity:
 - SIScone is $\mathcal{O}(Nn \ln n)$ (with $n \sim N$ the number of points in a circle of radius R)
 - midpoint standard implementation is $\mathcal{O}(N^2n)$

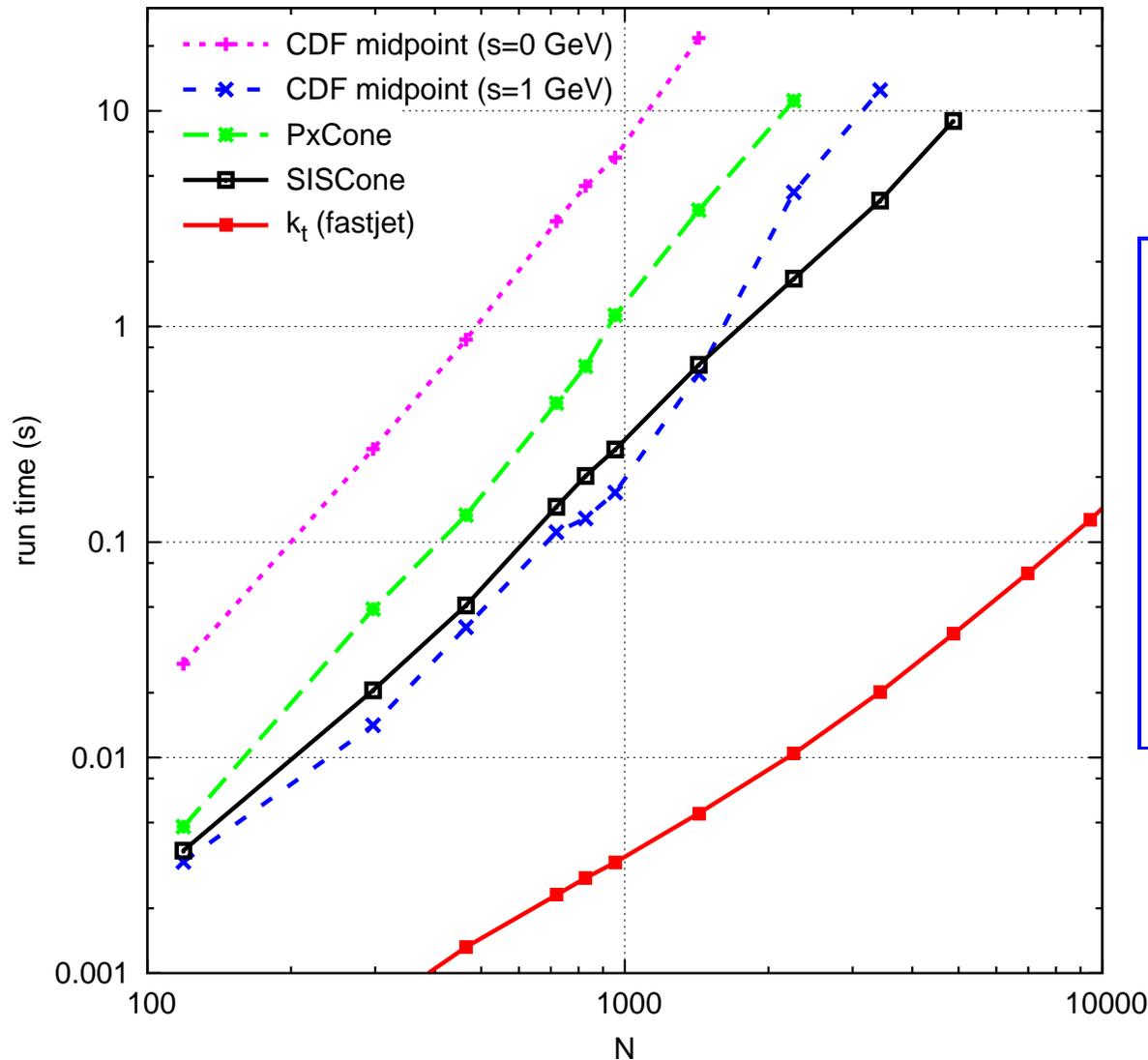
IR Unsafety failure rates

- Hard event: 2-10 particles
- Soft add-on: 1-5 particles
- Run:
 - “hard” only
 - many “hard+soft” trials
 - Search differences

Unsafety level	failure rate
2 hard + 1 soft	~ 50%
3 hard + 1 soft	~ 15%
SISCone	IR safe !



NB: small issues in the split-merge



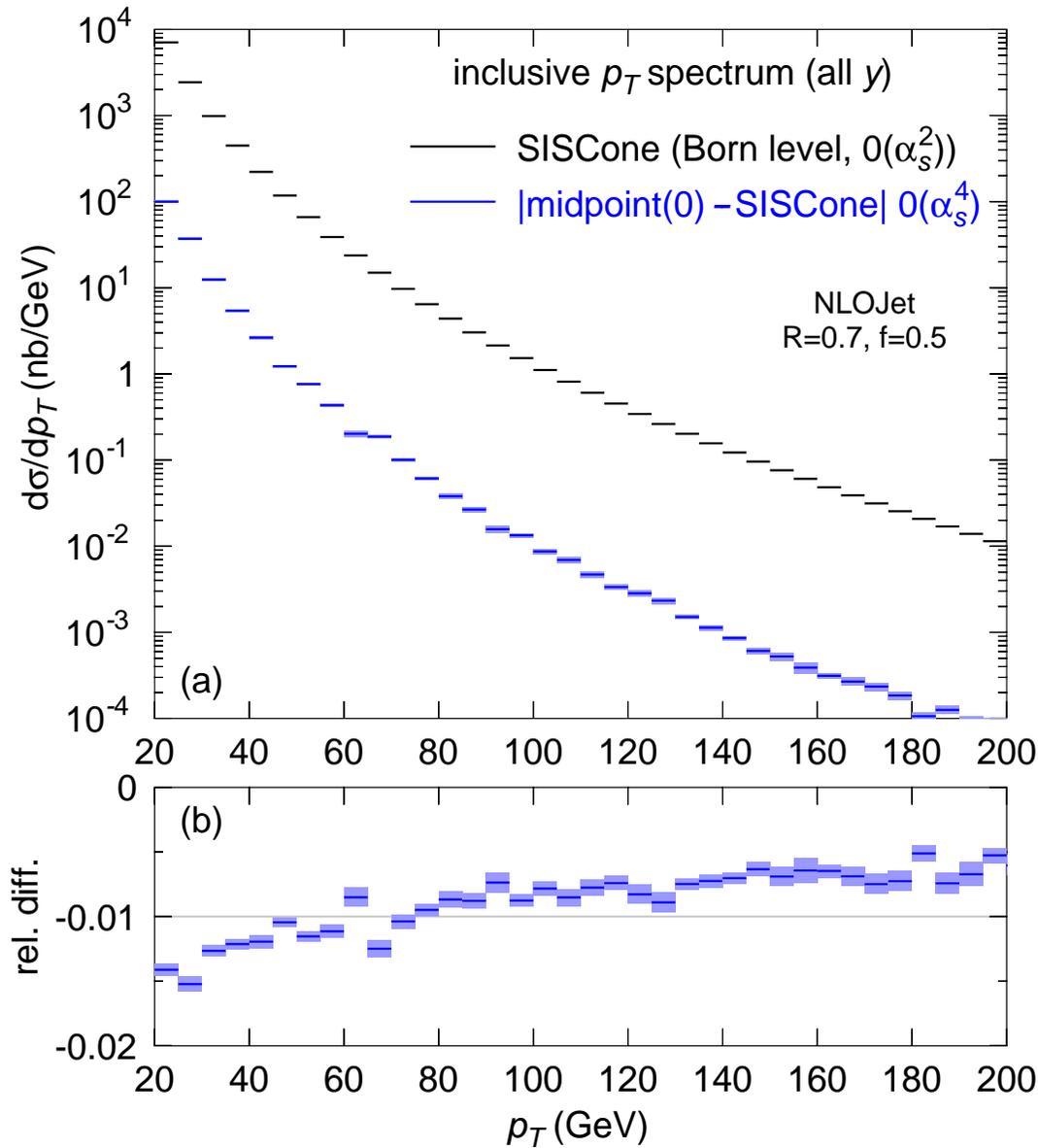
- at least as fast as other cones
- IR safe
- others are not
- collinear safe
- midpoint($s > 0$) is not

Impact on inclusive jet spectrum

Physical impact: SISCone vs. midpoint(s) ?

- IR unsafety of midpoint: 3 particles in the same vicinity + 1 to balance p_t
⇒ starts at the $2 \rightarrow 4$ level ($\mathcal{O}(\alpha_s^4)$)
- 3 contributions at this order:
 $2 \rightarrow 4$ at LO (tree), $2 \rightarrow 3$ at NLO (1 loop) and $2 \rightarrow 2$ at NNLO (2 loops)
⇒ $2 \rightarrow 4$ at LO is IR divergent
BUT the difference between SISCone and midpoint(s) is finite since it is 0 at the $2 \rightarrow 2$ and $2 \rightarrow 3$ levels
⇒ compute |SISCone-midpoint(s)| for $2 \rightarrow 4$ diagrams
- Compare with the $2 \rightarrow 2$ (LO) spectrum to estimate effect

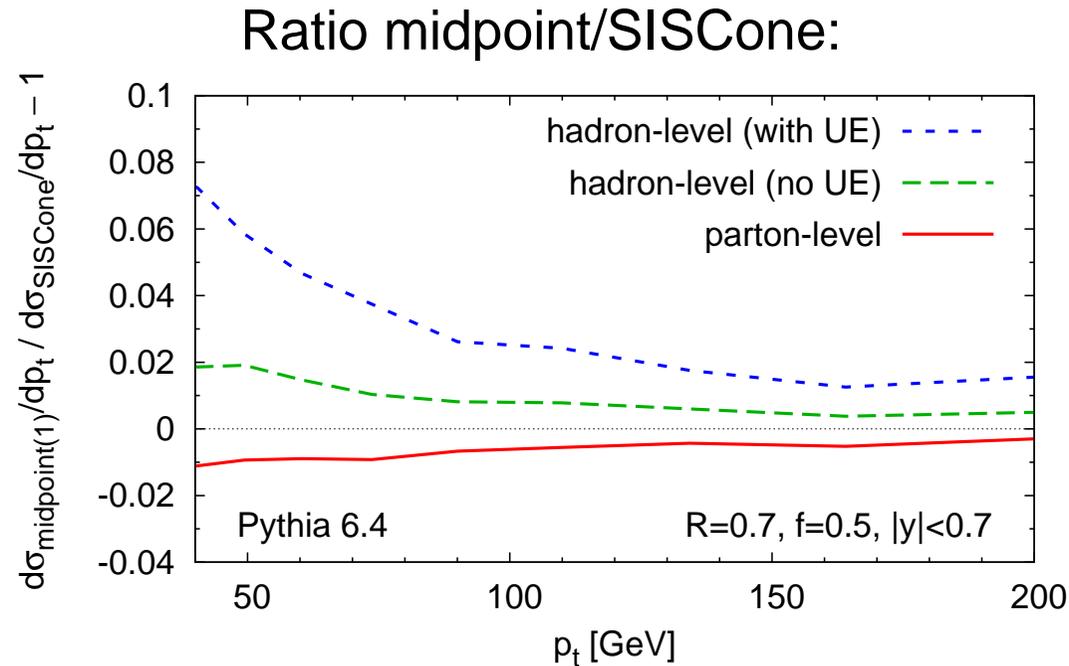
Impact on inclusive jet spectrum



Differences of order 1-2 %

Impact on inclusive jet spectrum

Including parton shower, hadronic corrections and/or underlying event:

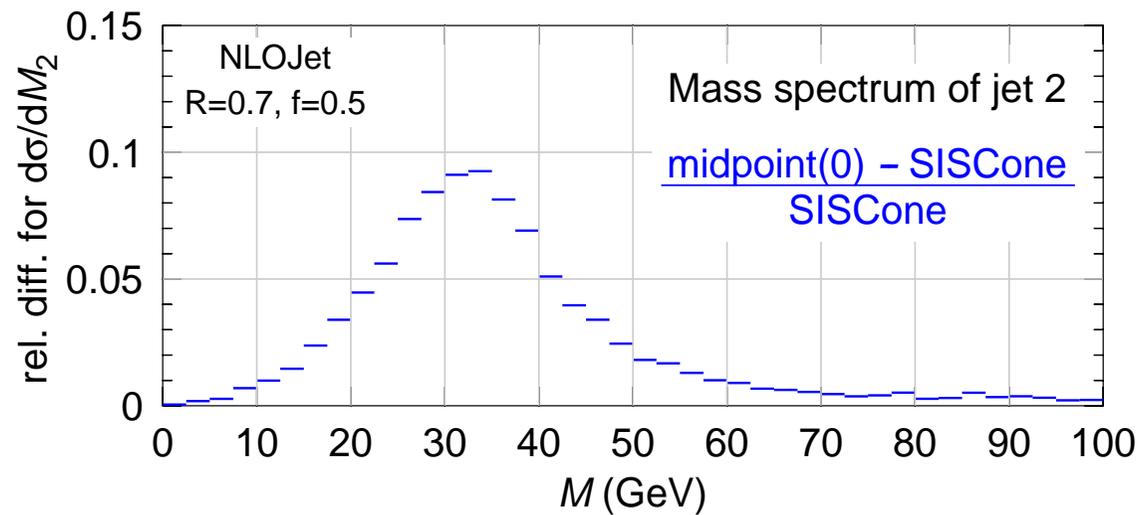


- Differences up to 6 %
- Less effect from underlying event in SISCone

Impact on jet mass spectrum

Study of more exclusive quantity e.g. mass spectrum in 3-jet events

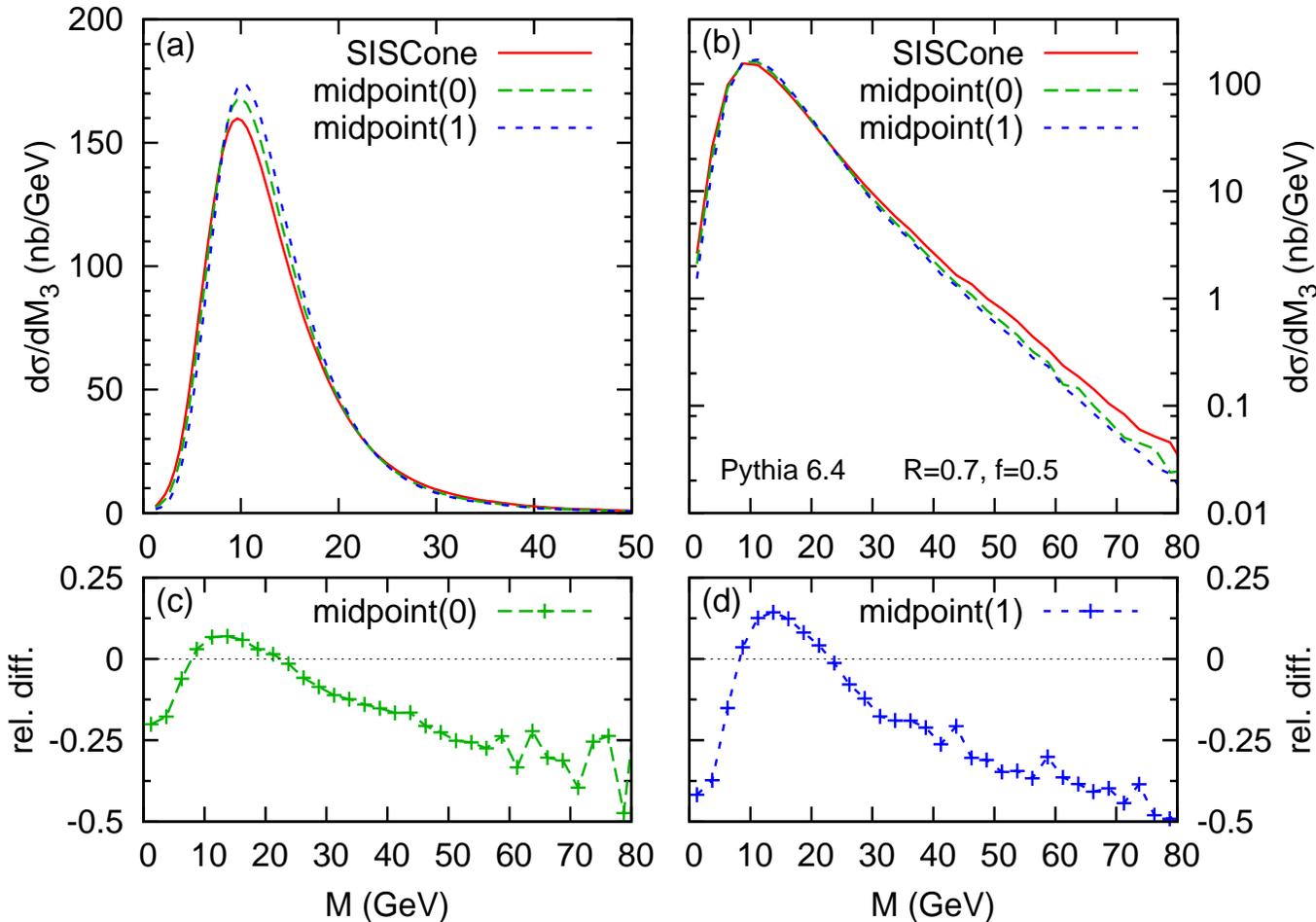
1. At fixed order (NLOJet, LO, $2 \rightarrow 4$)



Differences up to 10 %

Impact on jet mass spectrum

2. At fixed order (PYTHIA)



- ▷ Differences of order 10 %
- ▷ Larger effects in the tail
- ▷ seed threshold even worse

Conclusions

- Cone jet algorithms are widely used
- seeded implementations are **IR unsafe** (sometimes **collinear unsafe**)
IR safety is a prerequisite for perturbative QCD to make sense

We propose a [new cone algorithm \(SISCone\)](#):

- **IR safe** (and **collinear safe**)
- as **fast** as available cone implementations
- has **10% impact on jet mass spectra**
- is **less affected by underlying events**