

Defining jets at the dawn of the LHC

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- Jet algorithms and jet definitions
 - basic ideas: why jets? recombinations and cones
 - failures of the 20th-century cone algorithms
 - new algorithms without the failures
- More advanced topics: how to better use the tools we have?
 - jet areas: tool for pileup subtraction
 - new generation of algorithms
 - optimal choice (for kinematic reconstructions)

Unavoidable theory

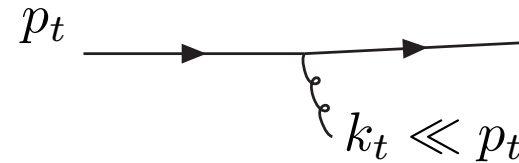
QCD probability for gluon emission (angle θ and \perp -mom. k_t):

$$dP \propto \alpha_s \frac{d\theta}{\theta} \frac{dk_t}{k_t}$$

Two divergences:



collinear



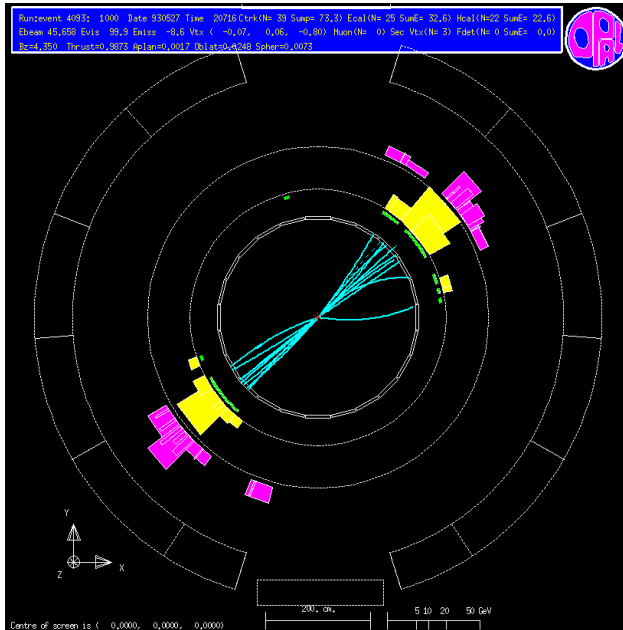
soft

Divergences cancelled by virtual corrections

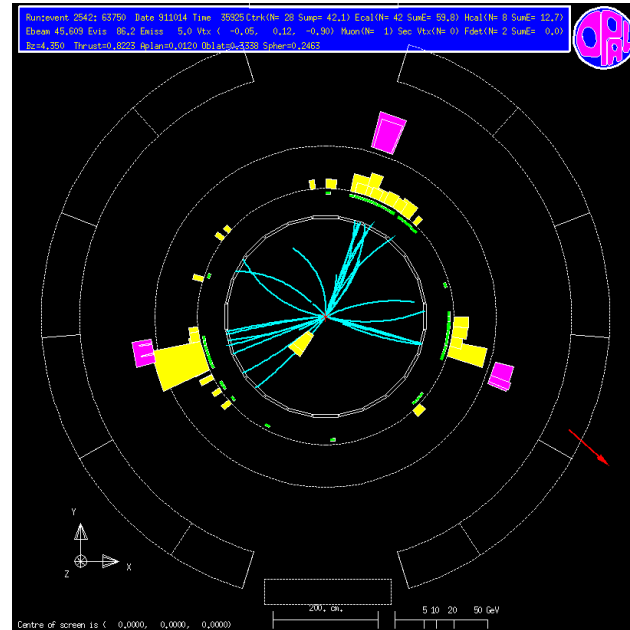
Motivation: why jets

Collinear divergence \Rightarrow QCD produces “jetty” showers

Example: LEP (OPAL) events



2 jets



3 jets

“Jets” \equiv bunch of collimated particles \cong hard partons

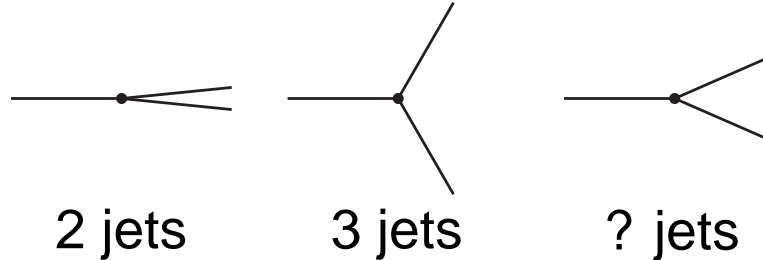
Motivation: why jets

Collinear divergence \Rightarrow QCD produces “jetty” showers

“Jets” \equiv bunch of collimated particles \cong hard partons

BUT

- a “parton” is an ambiguous concept (NLO)
- “collinear” has some arbitrariness



Motivation: why jets

Collinear divergence \Rightarrow QCD produces “jetty” showers

“Jets” \equiv bunch of collimated particles \cong hard partons

BUT

- a
- “c

In practice: use of a jet definition

particles $\{p_i\}$ $\xrightarrow[\text{definition}]{\text{jet}}$ jets $\{j_k\}$

Jet algorithm: the recipe (insufficient!)

Jet definition: algorithm + the parameters

20th century jet algorithms

Recombination:

- k_t algorithm
- Cambridge/Aachen alg.

Cone:

- CDF JetClu
- CDF MidPoint
- D0 (run II) Cone
- PxCone
- ATLAS Cone
- CMS Iterative Cone
- PyCell/CellJet
- GetJet

20th century jet algorithms

Recombination:

- k_t algorithm
- Cambridge/Aachen alg.

Idea: undo the showering

Successively

- find the closest pair of particles
- recombine them

Distance:

k_t :

$$d_{i,j} = \min(k_{t,i}^2, k_{t,j}^2)(\Delta\phi_{i,j}^2 + \Delta y_{i,j}^2)$$

Cam/Aachen:

$$d_{i,j} = \Delta\phi_{i,j}^2 + \Delta y_{i,j}^2$$

stop at a distance R

20th century jet algorithms

Idea: dominant flow of energy

Stable cone (radius R):

sum of particles in the cone points
towards the cone centre

All these are **iterative cones**:

- start from a **seed**
- iterate until stable

seeds = {particles, midpoints}

**Jet \equiv stable cone
modulo overlapping**

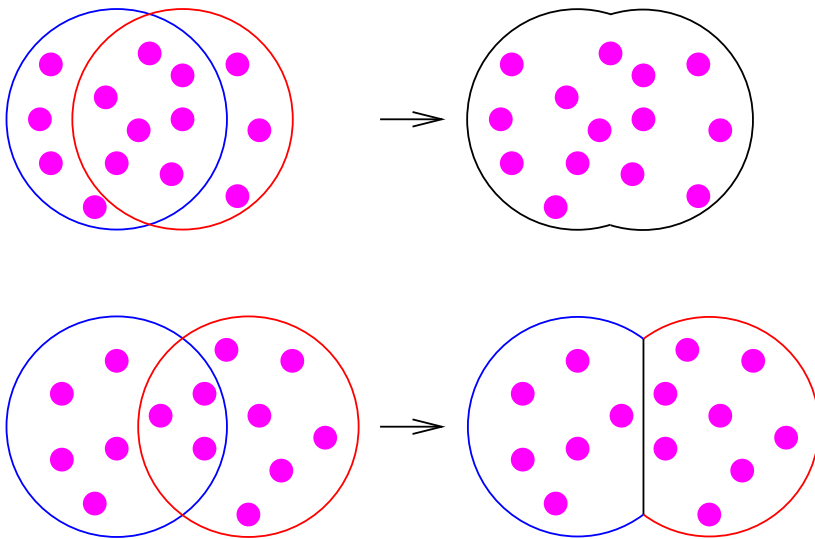
Cone:

- CDF JetClu
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20th century jet algorithms

Cone with split-merge

Split/merge if the overlap is smaller/larger than a threshold f



Cone:

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20th century jet algorithms

Cone with progressive removal

Successively

- iterate from hardest particle
- call that a jet (remove particles)

Basic property:

hard circular jets

Cone:

- CDF JetClu
- CDF MidPoint
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20th century jet algorithms

Recombination:

- k_t algorithm
- Cambridge/Aachen alg.

✓ perturbative behaviour

Cone:

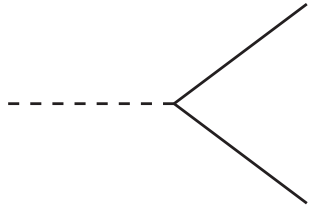
- CDF JetClu
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✓ UE sensitivity

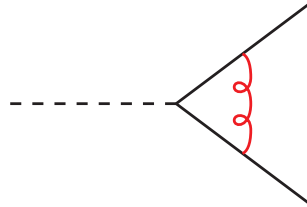
21st century: how does that picture change?

QCD divergences

Ingredient: QCD soft and collinear divergencies

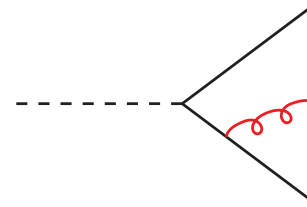


LO



NLO(virt)

∞



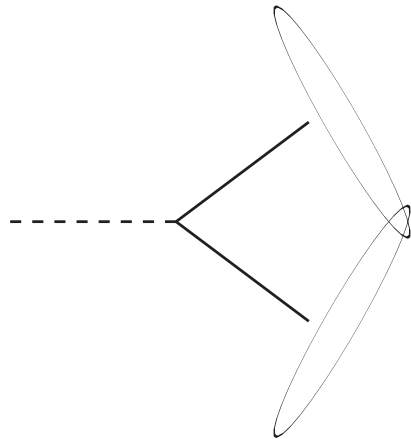
NLO(real)

∞

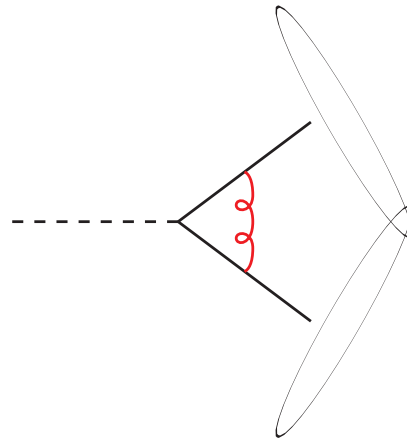
• ∞ (from soft gluons) cancel (inclusive x-section)

QCD divergences

Ingredient: QCD soft and collinear divergencies

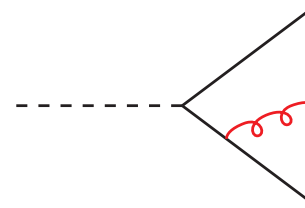


LO



NLO(virt)

∞



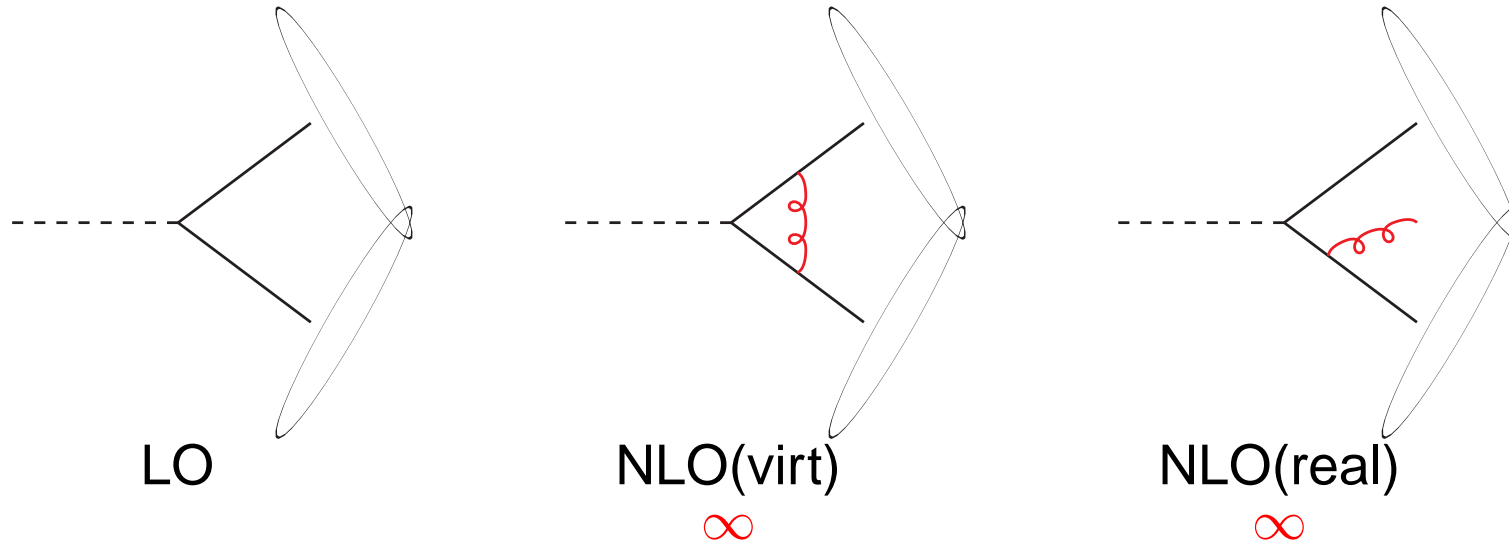
NLO(real)

∞

- Consider an extra (NLO) **soft** gluon
- Assume LO gives 2 jets \Rightarrow NLO(virt) gives 2 jets

QCD divergences

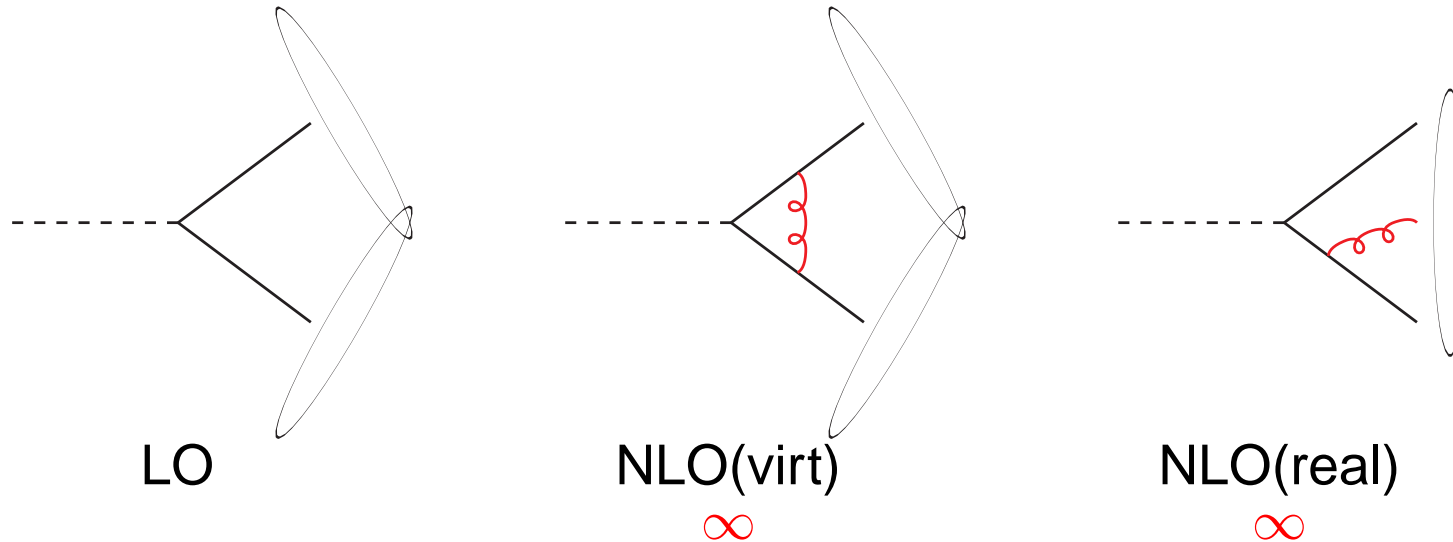
Ingredient: QCD soft and collinear divergencies



- Consider an extra (NLO) **soft** gluon
- Assume LO gives 2 jets \Rightarrow NLO(virt) gives 2 jets
- NLO(real) gives 2 jets $\Rightarrow \infty$ cancel \Rightarrow finite jet cross-section

QCD divergences

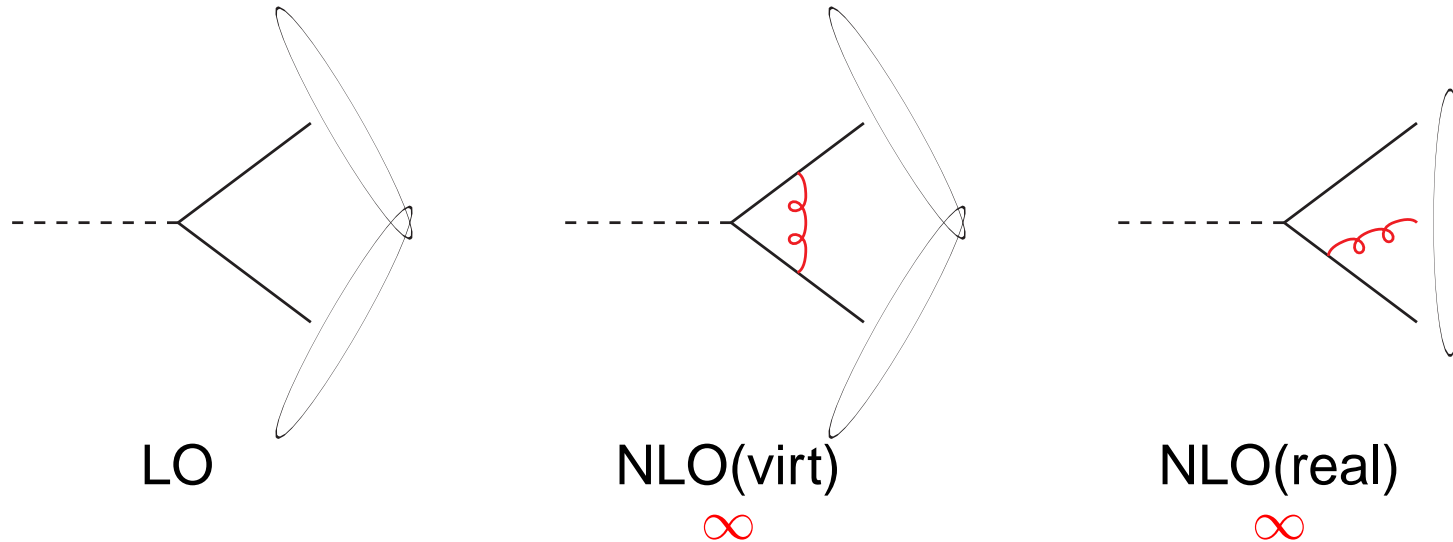
Ingredient: QCD soft and collinear divergencies



- Consider an extra (NLO) **soft** gluon
- Assume LO gives 2 jets \Rightarrow NLO(virt) gives 2 jets
- NLO(real) gives 2 jets $\Rightarrow \infty$ cancel \Rightarrow finite jet cross-section
NLO(real) gives 1 jets $\Rightarrow \infty$ do not cancel \Rightarrow infinite jet x-section

QCD divergences

Ingredient: QCD soft and collinear divergencies

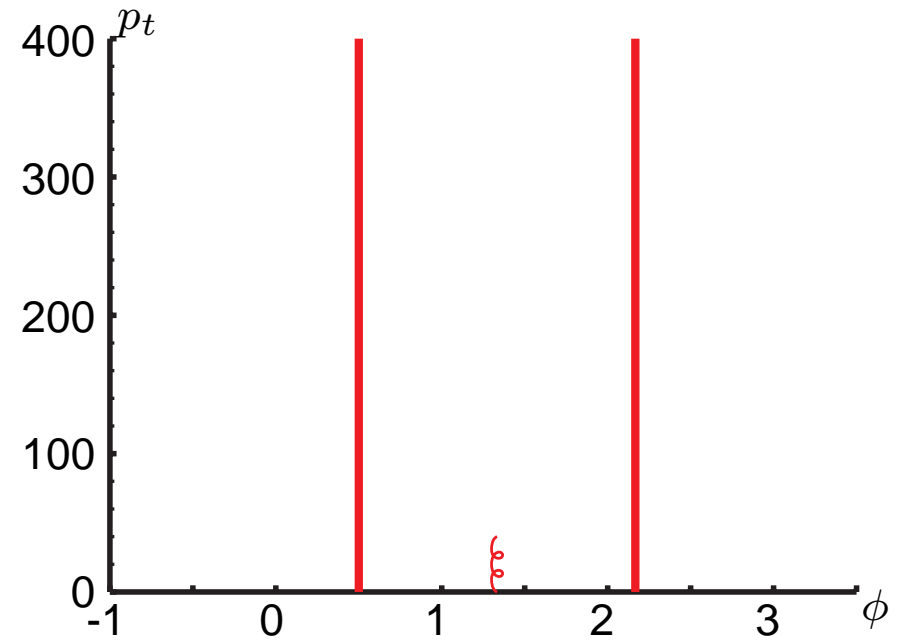
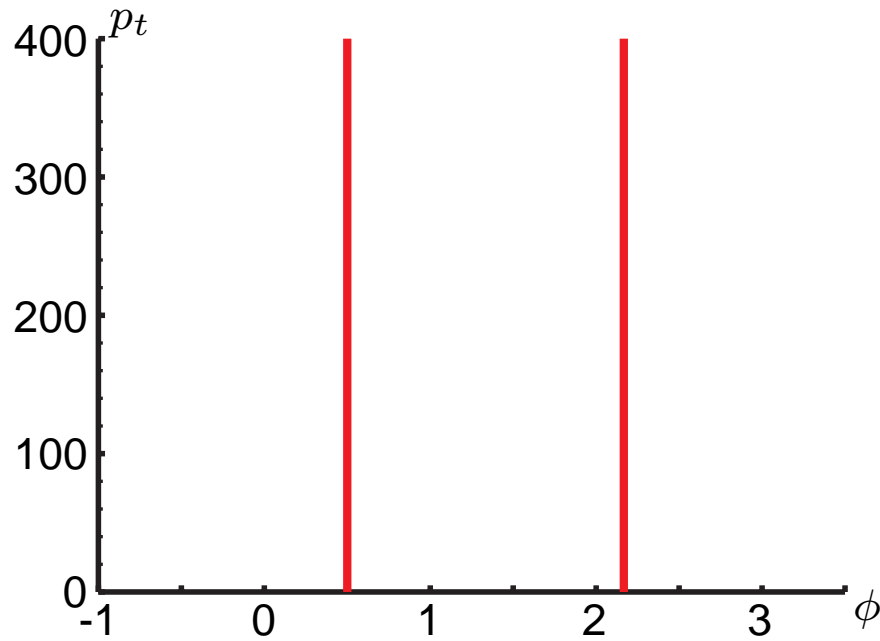


For pQCD to make sense, the (hard) jets should not change when

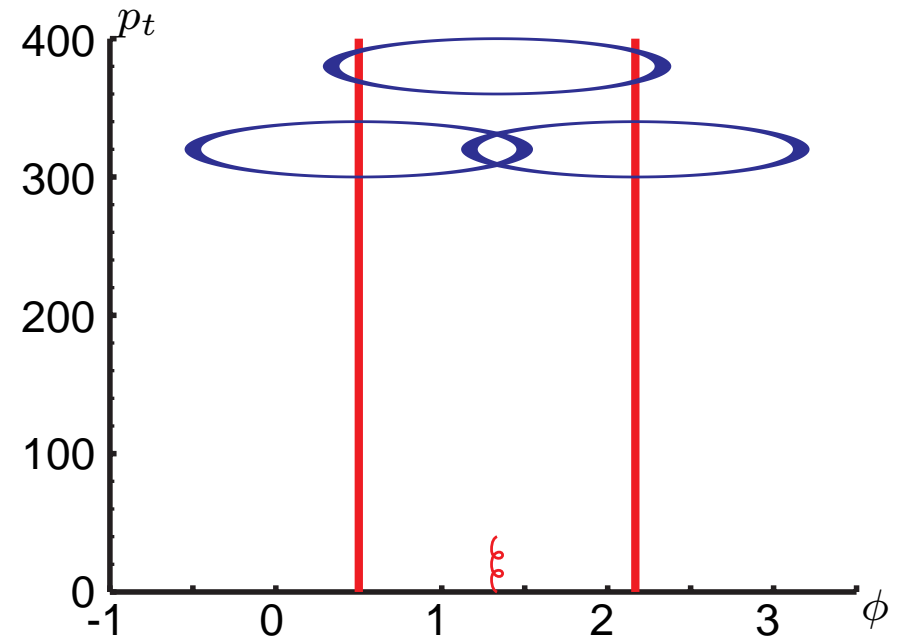
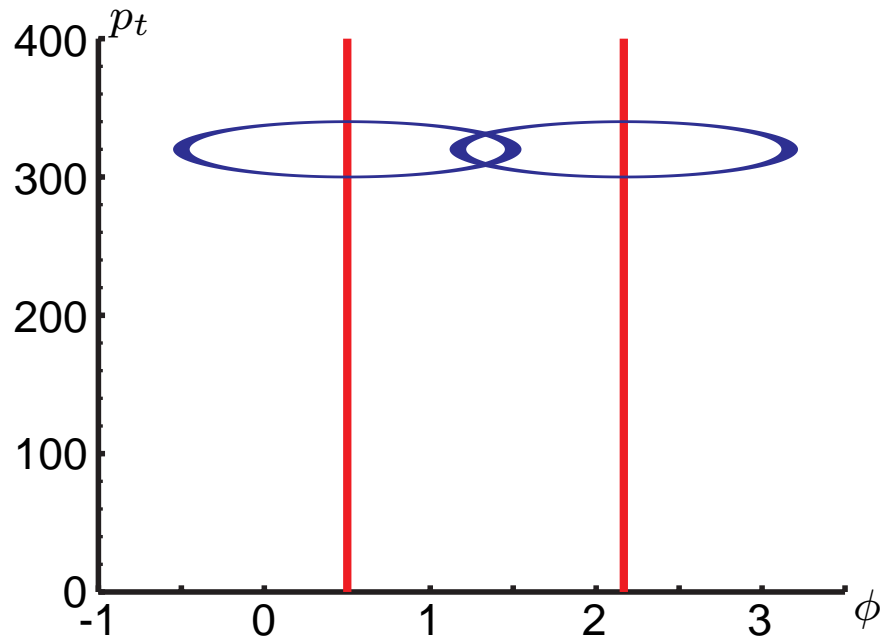
- one has a soft emission *i.e.* adds a very soft gluon
- one has a collinear splitting
i.e. replaces one parton by two at the same place (η, ϕ)

[SNOWMASS Accords, Fermilab, 1990]

IR (un)safety? JetClu and Atlas Cone

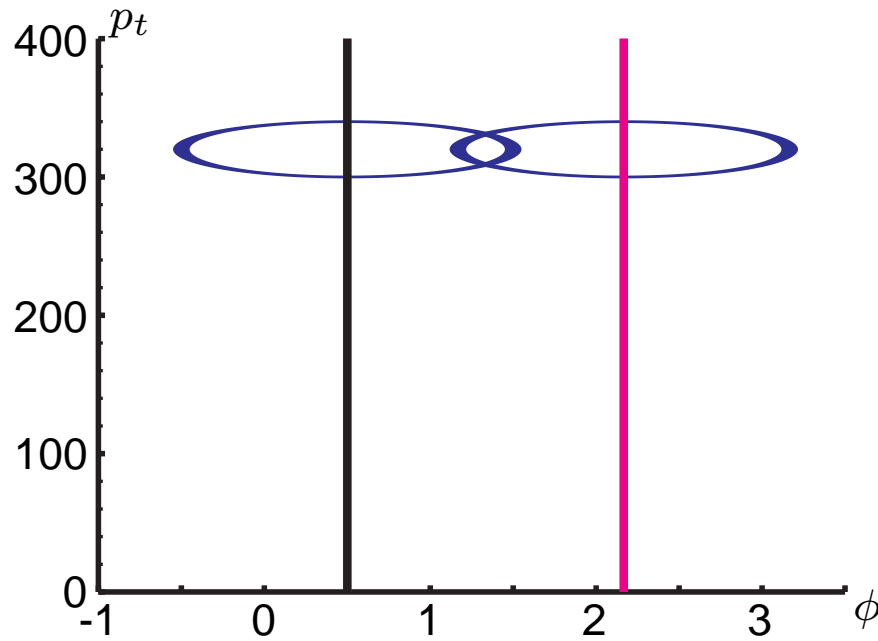


IR (un)safety? JetClu and Atlas Cone

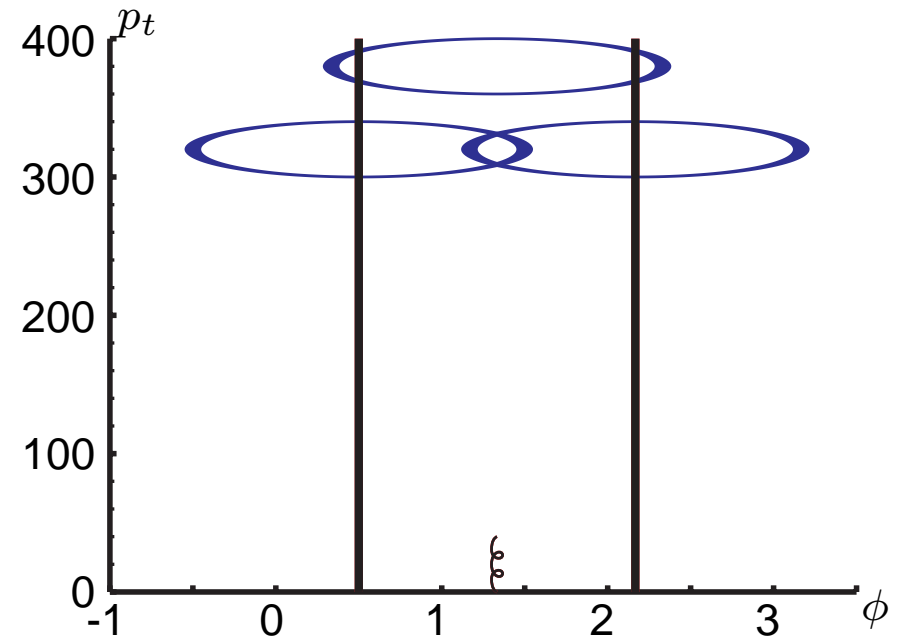


Stable cones found

IR (un)safety? JetClu and Atlas Cone



2 jets

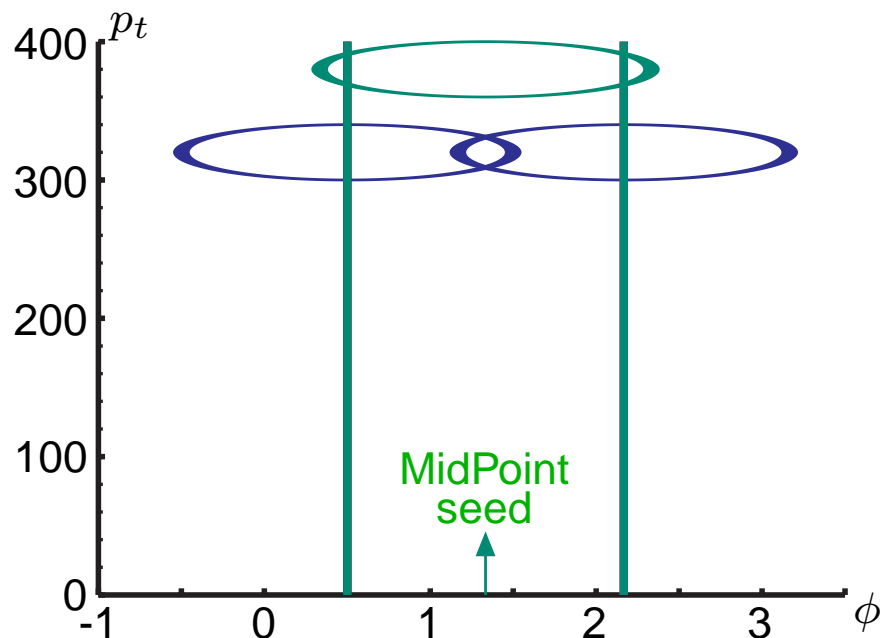


1 jet

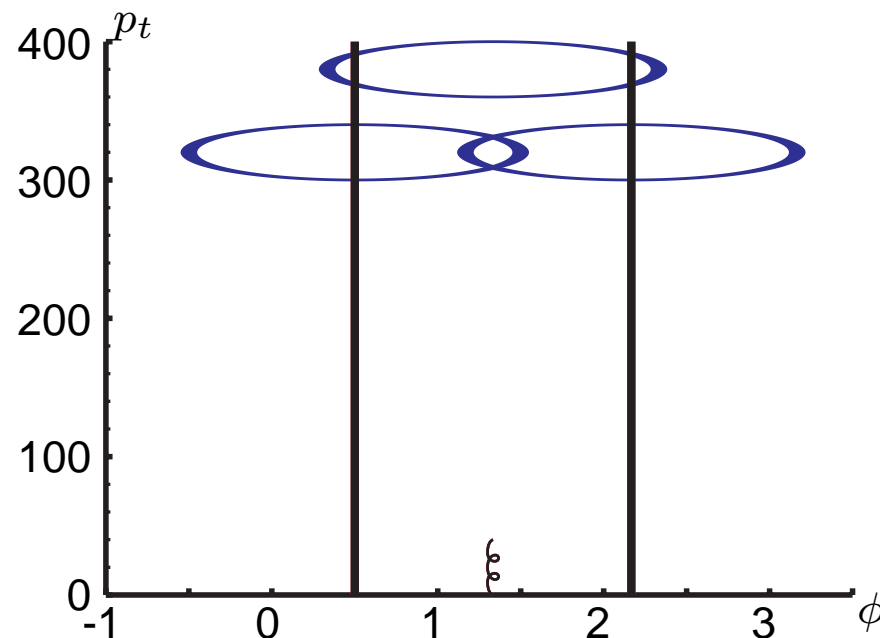
A soft gluon changed the number of jets

⇒ IR unsafety of JetClu and the ATLAS Cone

IR (un)safety? JetClu and Atlas Cone



2 jets



1 jet

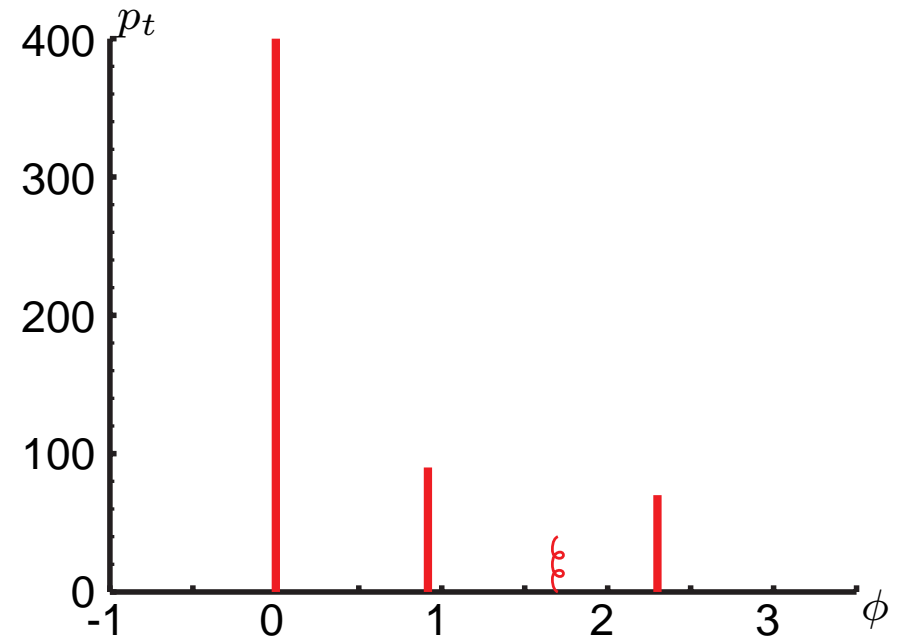
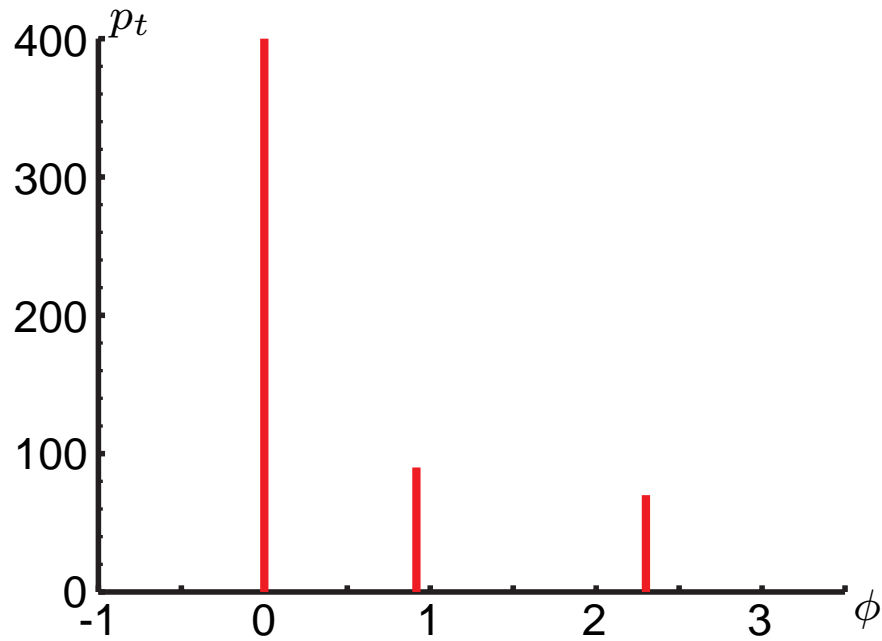
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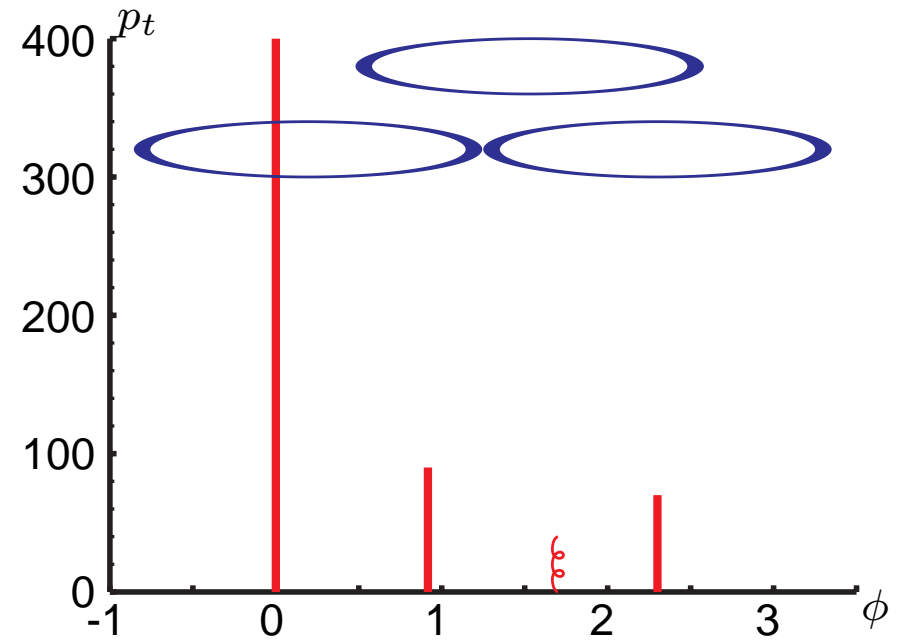
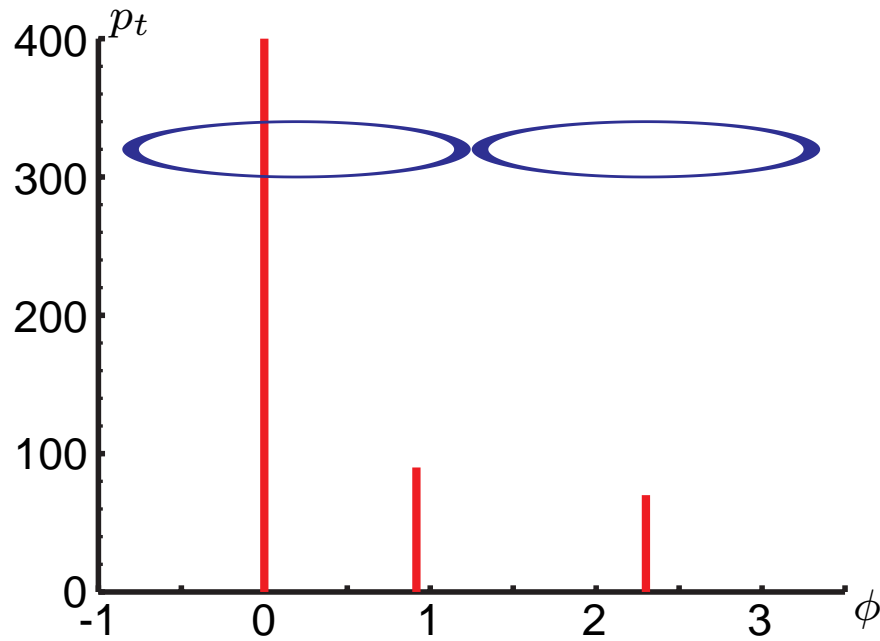
Fixed by MidPoint

[Blazey *et al.*, 00]

IR (un)safety? MidPoint

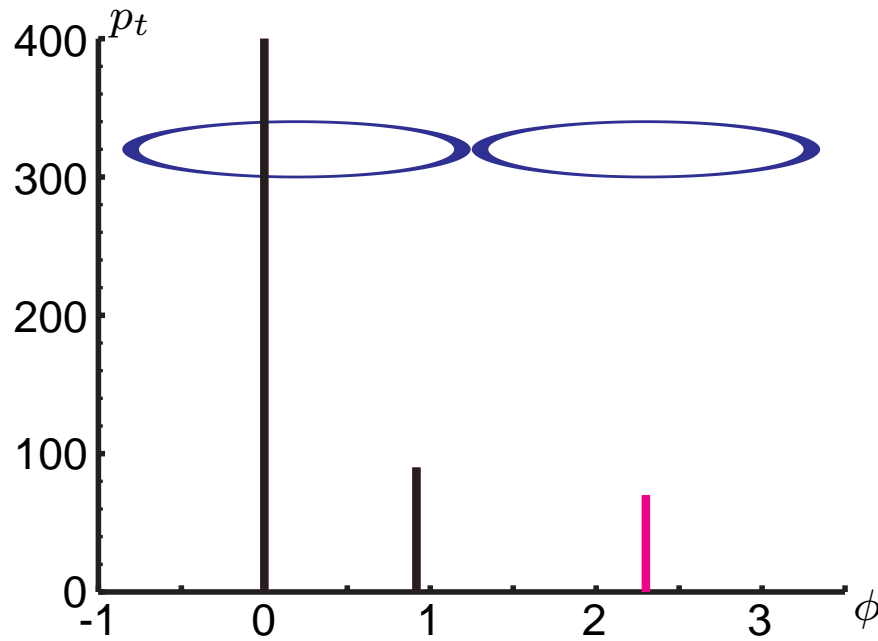


IR (un)safety? MidPoint

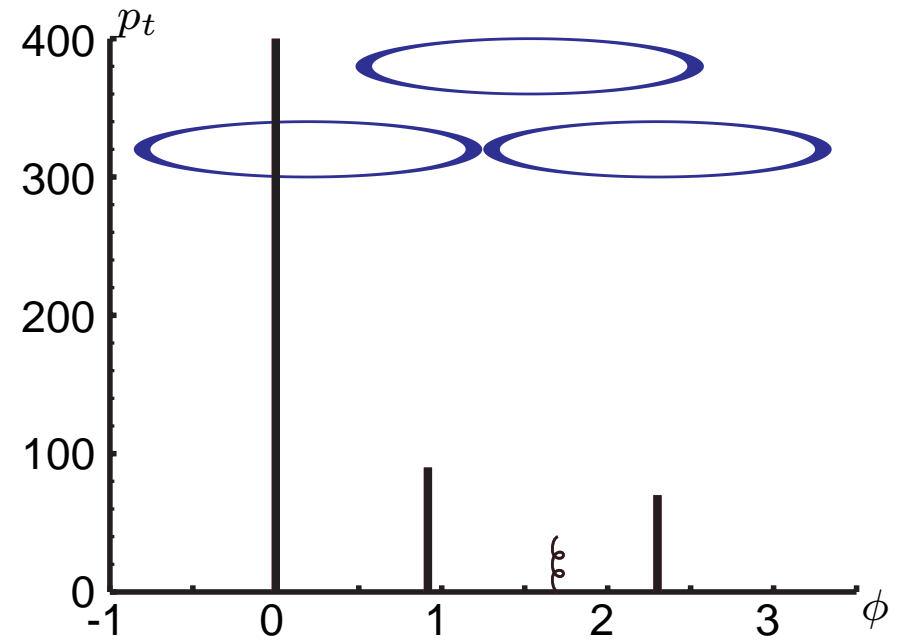


Stable cones found

IR (un)safety? MidPoint



2 jets

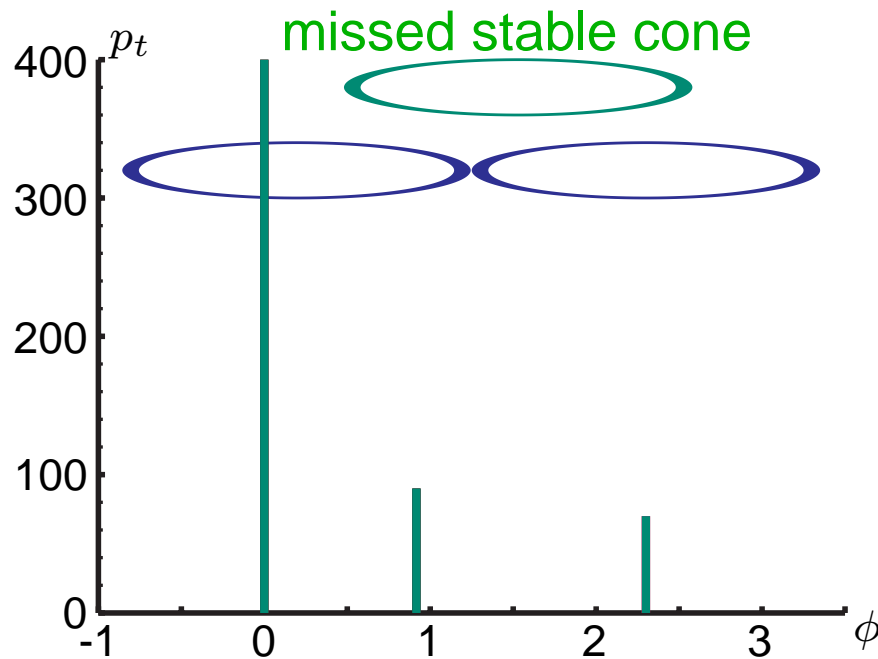


1 jet

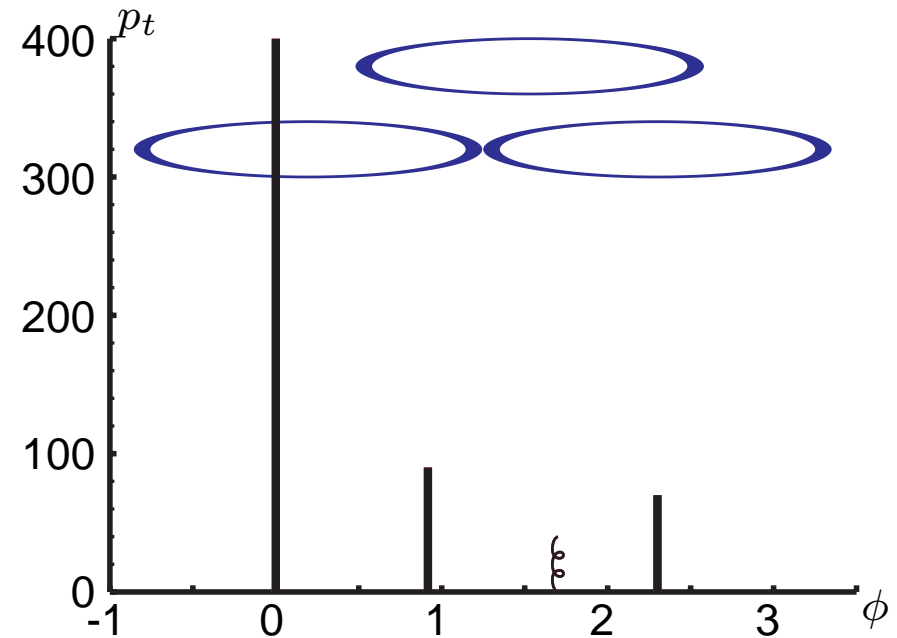
A soft gluon changed the number of jets

\Rightarrow IR unsafety of MidPoint (1 order in α_s later than JetClu)

IR (un)safety? MidPoint



2 jets



1 jet

Solution: be sure to find all stable cones

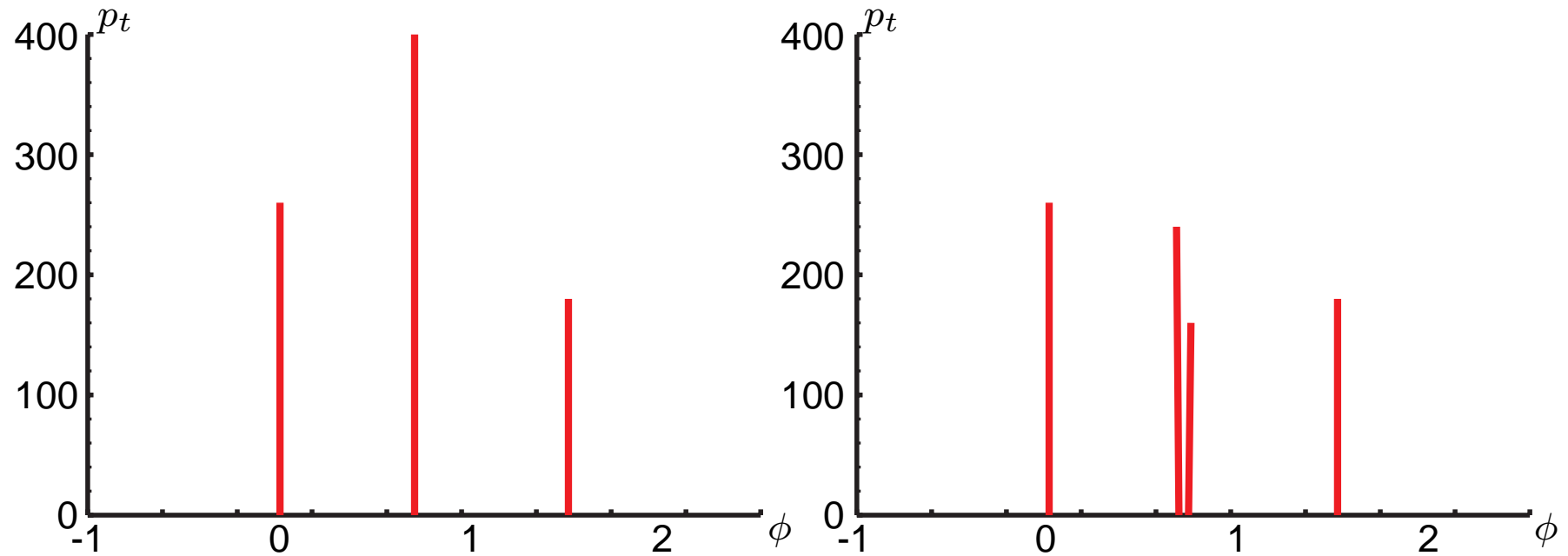
SISCone: Seedless Infrared-Safe Cone algorithm

<http://projects.hepforge.org/siscone>

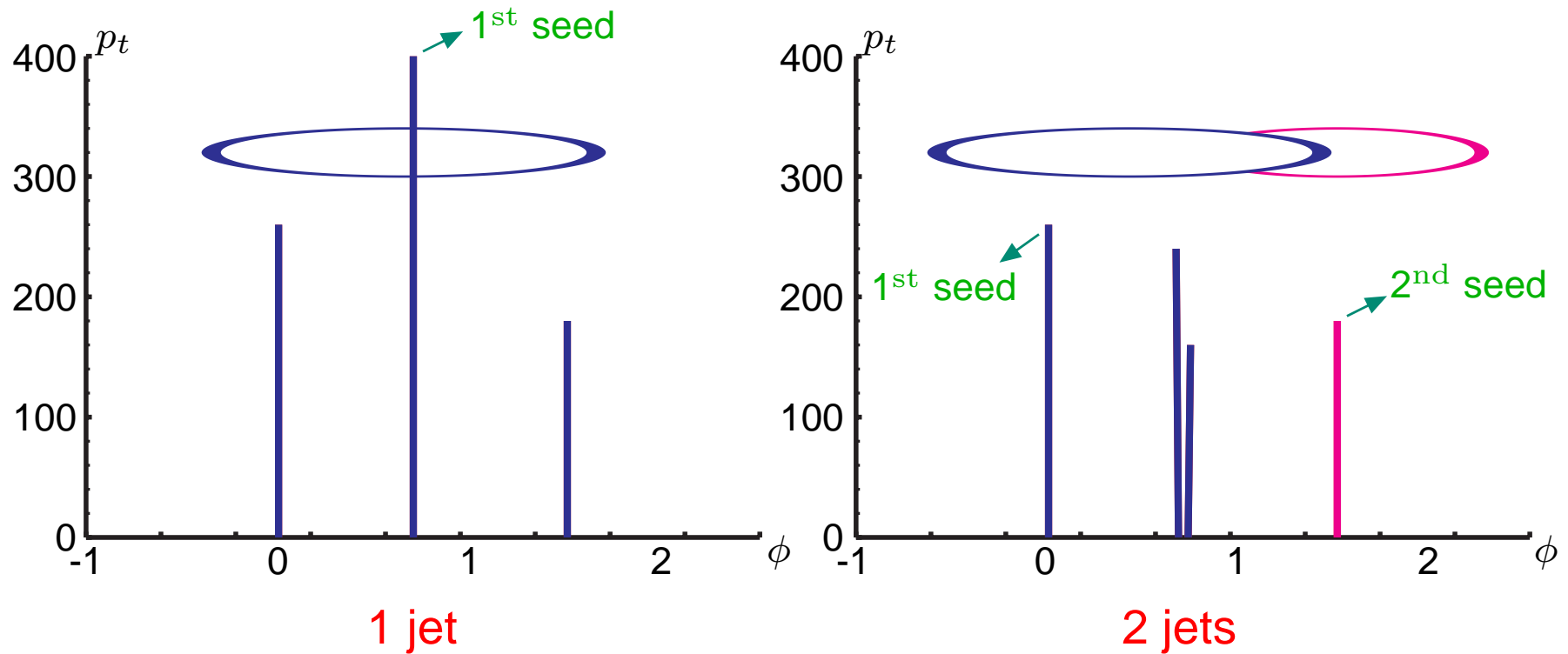
[G.Salam, G.S., 07]

Idea: enumerate enclosures by enumerating pairs of particles

Collinear (un)safety? the CMS iterative cone



Collinear (un)safety? the CMS iterative cone



A collinear splitting changed the number of jets

⇒ Collinear unsafety of the CMS iterative cone

Come back to recombination-type algorithms:

$$d_{ij} = \min(k_{t,i}^{2p}, k_{t,j}^{2p}) (\Delta\phi_{ij}^2 + \Delta\eta_{ij}^2)$$

- $p = 1$: k_t algorithm
- $p = 0$: Aachen/Cambridge algorithm

Come back to recombination-type algorithms:

$$d_{ij} = \min(k_{t,i}^{2p}, k_{t,j}^{2p}) (\Delta\phi_{ij}^2 + \Delta\eta_{ij}^2)$$

- $p = 1$: k_t algorithm
- $p = 0$: Aachen/Cambridge algorithm
- $p = -1$: anti- k_t algorithm [M.Cacciari, G.Salam, G.S., 08]

Why should that be related to the iterative cone ?!?

- “large $k_t \Rightarrow$ small distance”
i.e. hard partons “eat” everything up to a distance R
i.e. circular/regular jets, jet borders unmodified by soft radiation
- infrared and collinear safe

21st century jet algorithms

Recombination:

- k_t algorithm
- Cambridge/Aachen alg.
- **anti- k_t algorithm**

4 available
safe algorithms

Cone:

- CDF JetClu
- CDF MidPoint
- D0 (run II) Cone
- PxCone
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- GetJet
- **SISCone**

anti- k_t adopted as default by ATLAS and CMS

21st century jet algorithms

Recombination:

- k_t algorithm

- Cambridge/Aachen

```
#-----  
#                               FastJet release 2.4  
#       Written by M. Cacciari, G.P. Salam and G. Soyez  
#                               http://www.fastjet.fr  
#-----
```

All those algorithms (and much more)
implemented (efficiently) in FastJet

safe algorithms

Cone:

- CDF JetClu

- CDF MidJet

- GetJet

- **SISCone**

anti- k_t adopted as default by ATLAS and CMS

When does IRC safety matters?

Take e.g. the MidPoint cone

$$\overbrace{\alpha_s^2 \times \dots}^{2 \text{ particles}} + \overbrace{\alpha_s^3 \times \dots}^{3 \text{ particles}} + \overbrace{\alpha_s^4 \times \dots}^{4 \text{ particles}} + \overbrace{\alpha_s^5 \times \dots}^{4 \text{ particles} + 1 \text{ soft}} + \dots$$

● QCD expansion (one α_s can be replaced by α_{EW})

When does IRC safety matters?

Take e.g. the MidPoint cone

$$\overbrace{\alpha_s^2 \times \dots}^{2 \text{ particles}} + \overbrace{\alpha_s^3 \times \dots}^{3 \text{ particles}} + \overbrace{\alpha_s^4 \times \dots}^{4 \text{ particles}} + \overbrace{\alpha_s^5 \times \log(p_t/\Lambda_{\text{QCD}}) \dots}^{4 \text{ particles} + 1 \text{ soft}} + \dots$$

- QCD expansion (one α_s can be replaced by α_{EW})
- IRC unsafety (regulated at the hadronic scale $\sim \Lambda_{\text{QCD}}$)

When does IRC safety matters?

Take e.g. the MidPoint cone

$$\begin{array}{ccccccc} \text{2 particles} & & \text{3 particles} & & \text{4 particles} & & \text{4 particles + 1 soft} \\ \underbrace{\alpha_s^2 \times \dots} & + & \underbrace{\alpha_s^3 \times \dots} & + & \underbrace{\alpha_s^4 \times \dots} & + & \underbrace{\alpha_s^5 \times \log(p_t/\Lambda_{\text{QCD}}) \dots + \dots} \\ & & & & & & \text{cannot be trusted} \end{array}$$

- QCD expansion (one α_s can be replaced by α_{EW})
- IRC unsafety (regulated at the hadronic scale $\sim \Lambda_{\text{QCD}}$)
- $\alpha_s \log(p_t/\Lambda_{\text{QCD}}) \sim 1$
- **last meaningful order = α_s^3 or $\alpha_{\text{EW}}\alpha_s^2$**

When does IRC safety matters?

Take e.g. the MidPoint cone

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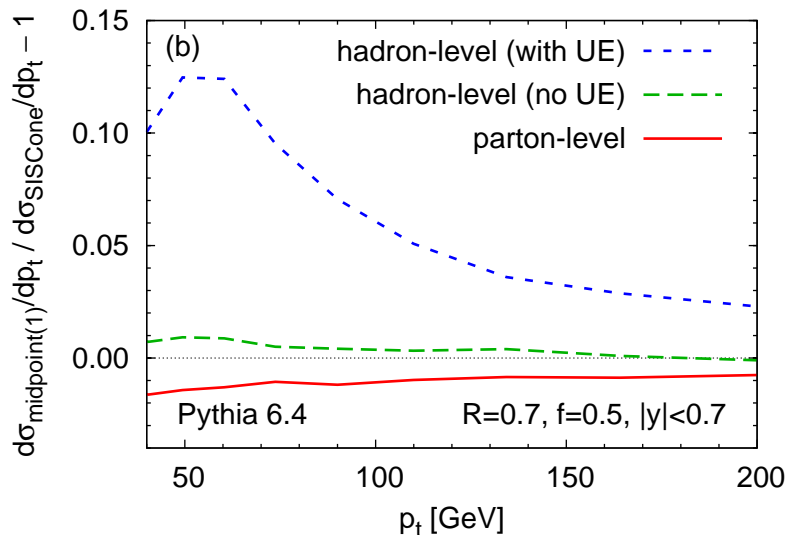
- QCD expansion (one α_s can be replaced by α_{EW})
- IRC unsafety (regulated at the hadronic scale $\sim \Lambda_{\text{QCD}}$)
- $\alpha_s \log(p_t/\Lambda_{\text{QCD}}) \sim 1$
- **last meaningful order = α_s^3 or $\alpha_{\text{EW}}\alpha_s^2$**
- same argument for the Iterative Cone
- 1 order worse for JetClu or the ATLAS cone

Physical impact

Observable	Last meaningful order	
	MidPoint/CMS	JetClu/ATLAS
Inclusive jet cross sect.	NLO	LO (NLOJet: NLO)
3 jet cross section	LO	none (NLOJet: NLO)
$W/Z/H + 2$ jet x-sect.	LO	none (MCFM: NLO)
jet masses in 3 jets	none	none (NLOJet: LO)

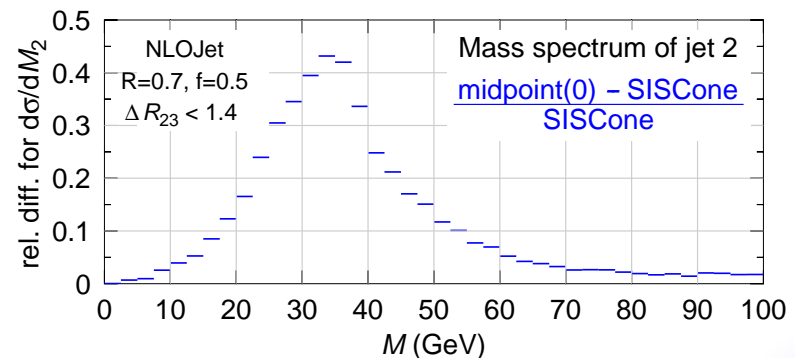
Example: (Midpoint-SISCone)/SISCone

pp $\sqrt{s} = 14$ TeV



● Incl. cross-section: a few %

● Masses in 3-jet events: $\sim 45\%$



Physical impact

Observable	Last meaningful order	
	MidPoint/CMS	JetClu/ATLAS
Inclusive jet cross sect.	NLO	LO (NLOJet: NLO)
3 jet cross section	LO	none (NLOJet: NLO)
$W/Z/H + 2$ jet x-sect.	LO	none (MCFM: NLO)
jet masses in 3 jets	none	none (NLOJet: LO)



Huge effort (~ 50 M€) to compute processes in pQCD

Note:

- arXiv:0903.0814: $W + 2$ jets vs. LO QCD using CDF JetClu
- arXiv:0903.1748: $Z + 2$ jets vs. NLO QCD using the D0runII cone
- arXiv:0903.1801: $Z + 2$ jets vs. NLO QCD using the CMS iterative cone

We (finally) have a good set of tools

Can we do better?

A growing list

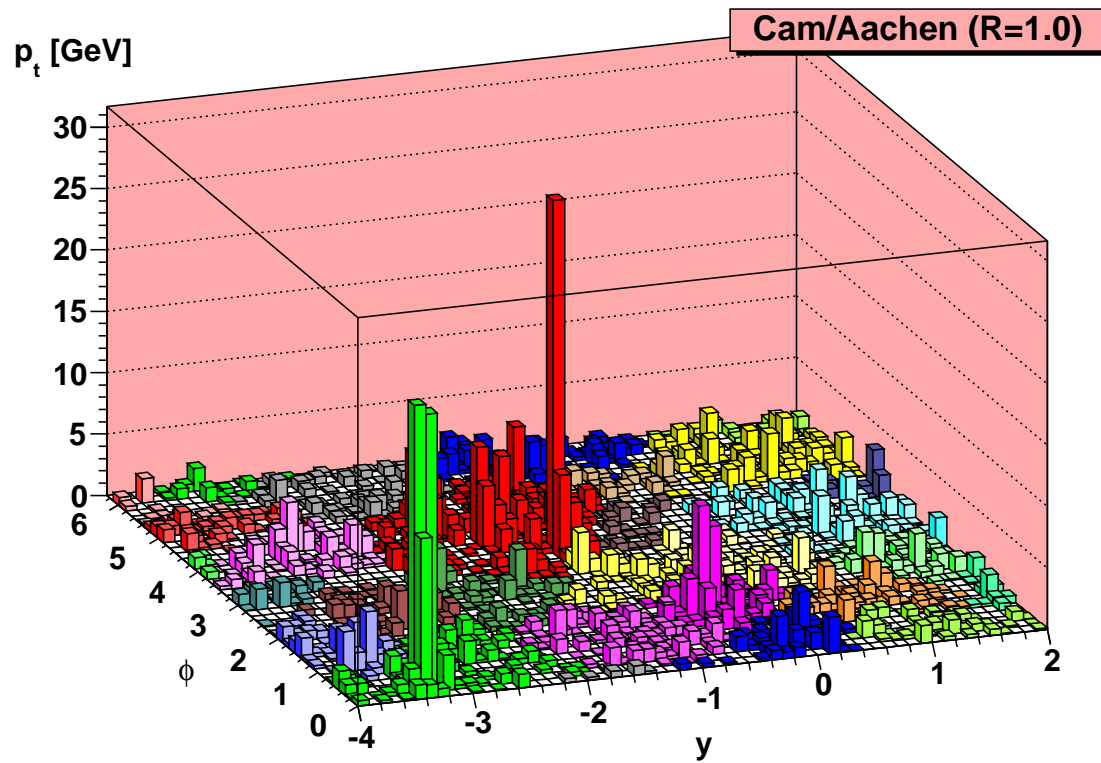
Many ideas and applications:

- ✓ jet areas and background subtraction
→ UE, pileup, heavy-ion background subtraction
- ✓ jet substructure and filtering
→ see below
- ✓ “best” jet definition
→ kinematic dijet reconstruction
- ✓ boosted objects tagging
→ $H \rightarrow b\bar{b}$, t , $\tilde{\chi}_0^1 \rightarrow qqq$, ...

I will cover the first three (see *e.g.* Gavin Salam’s talk here for the 4th)

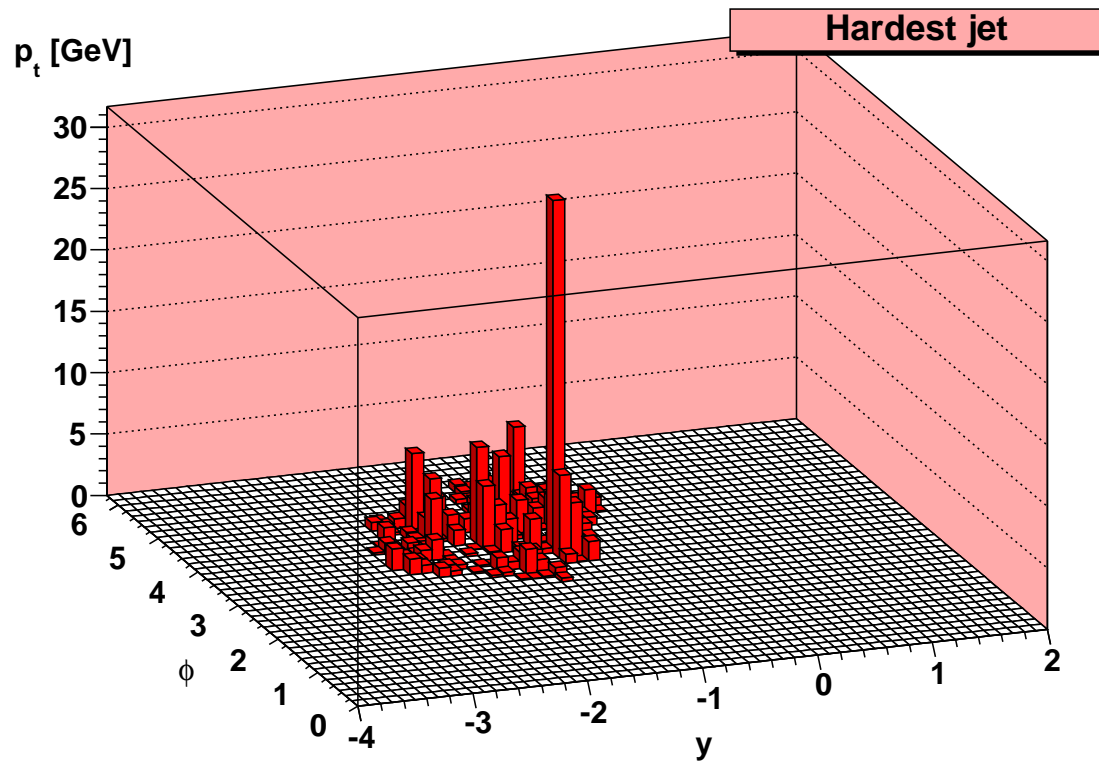
New idea #1: filtering

Filtering



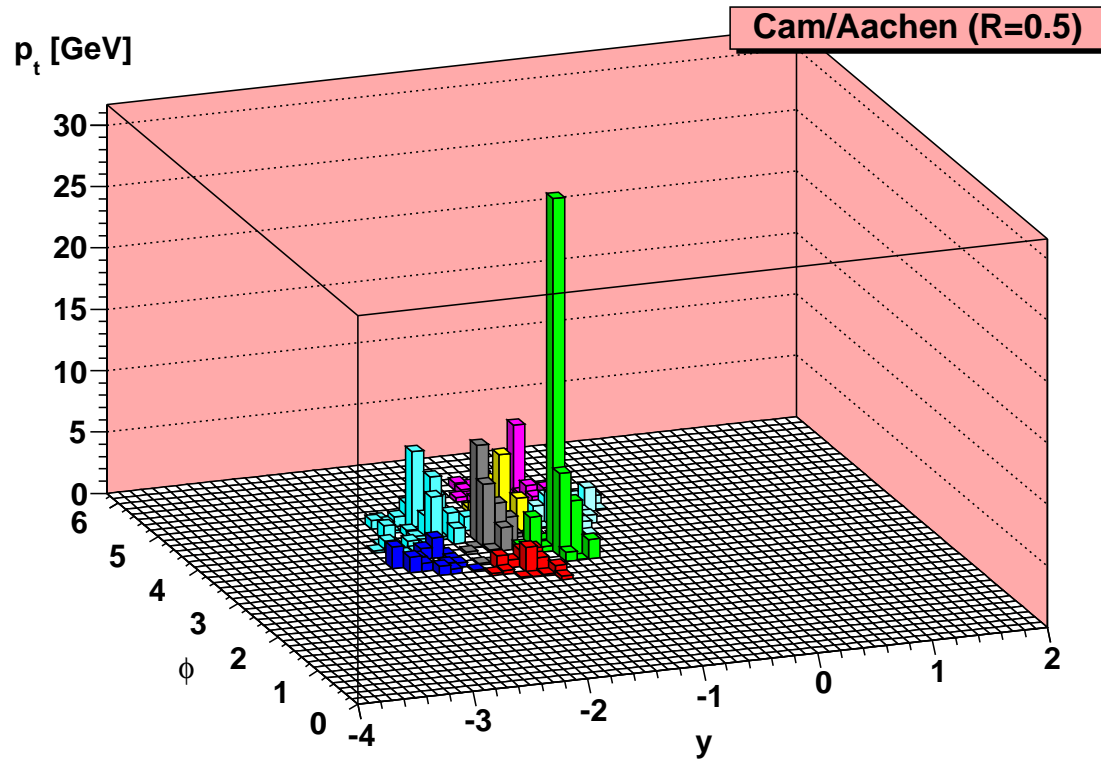
- cluster with Cambridge/Aachen(R)

Filtering



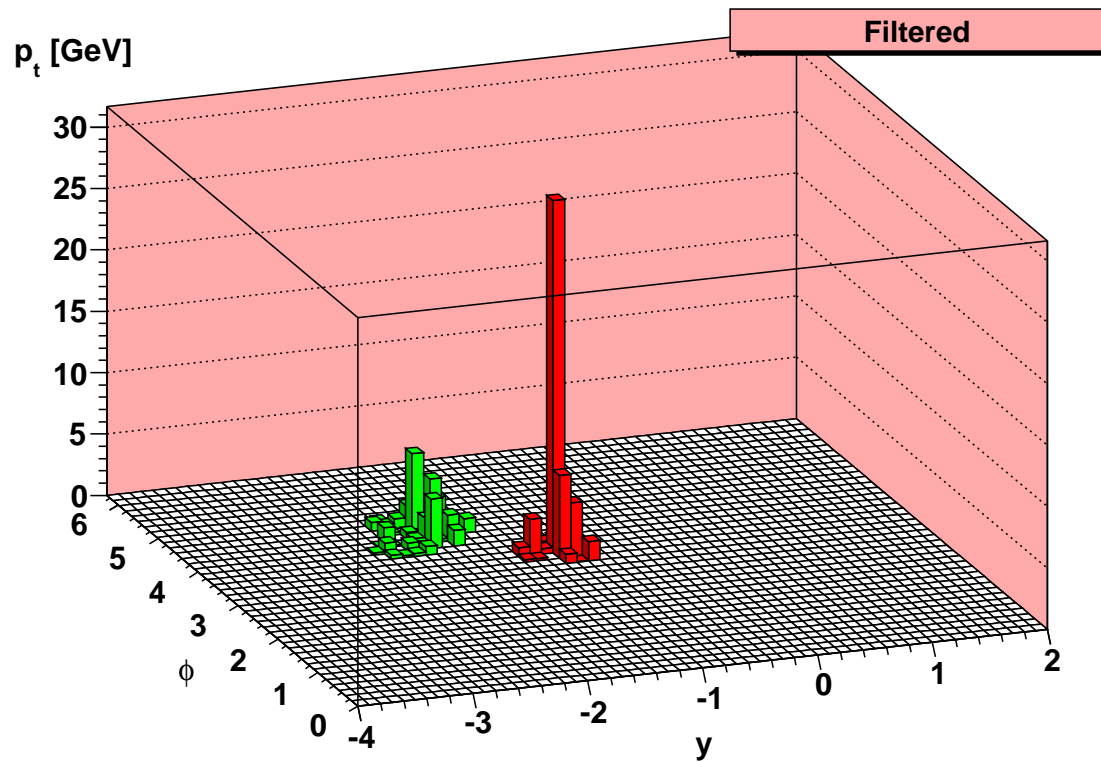
- cluster with Cambridge/Aachen(R)
- for each jet

Filtering



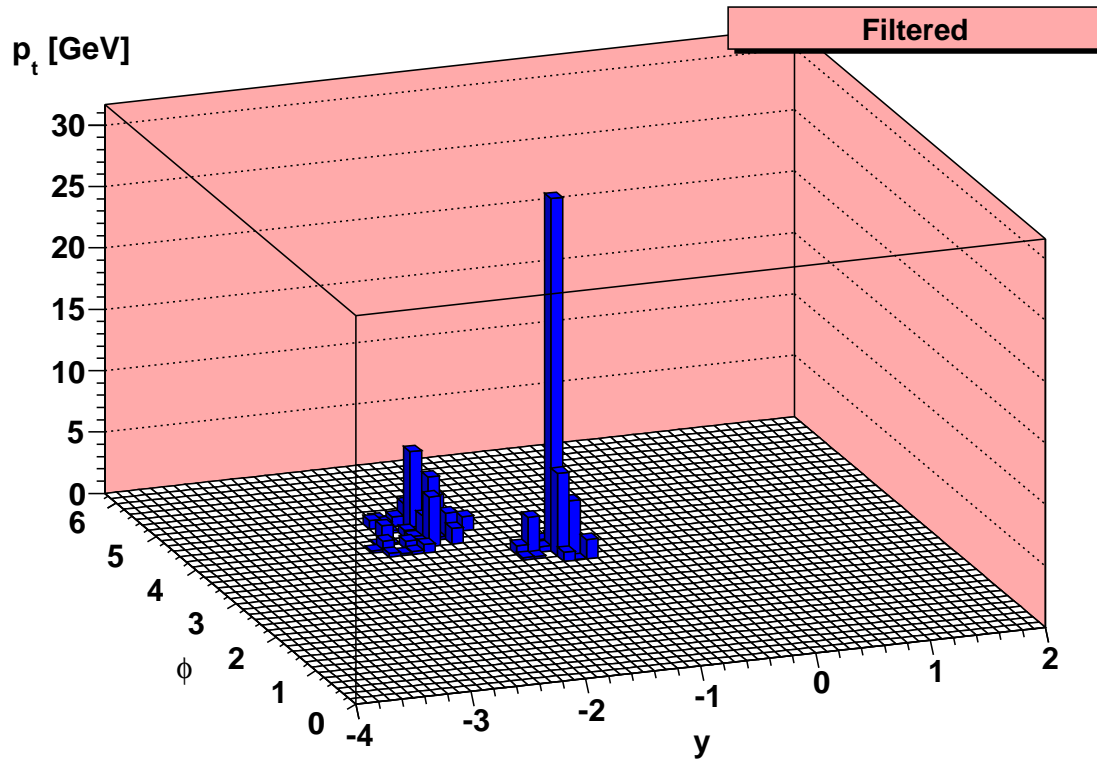
- cluster with Cambridge/Aachen(R)
- for each jet
 - recluster with Cambridge/Aachen($R/2$)

Filtering



- cluster with Cambridge/Aachen(R)
- for each jet
 - recluster with Cambridge/Aachen(R/2)
 - keep the 2 hardest subjects

Filtering



- cluster with Cambridge/Aachen(R)
- for each jet
 - recluster with Cambridge/Aachen(R/2)
 - keep the 2 hardest subjects

Idea:

- ✓ keep perturb. radiation
- ✓ remove UE

- Proven useful for boosted jet $H \rightarrow b\bar{b}$ tagging

[J.Butterworth, A.Davison, M.Rubin, G.Salam, 08]

- Proven useful for kinematic reconstructions

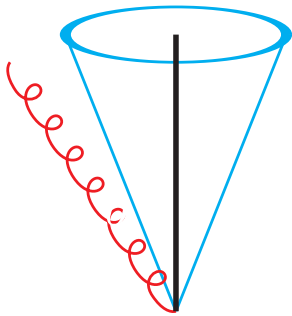
[M.Cacciari, J.Rojo, G.Salam, GS, 08]

New idea #2: jet definition optimisation

Optimisation: underlying idea

Competition between

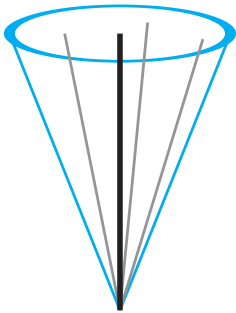
- catching perturbative radiation



Out-of-cone radiation:

$$\langle \delta p_t \rangle \propto - \int_R \frac{d\theta}{\theta} \sim -\log(1/R)$$

- not catching soft background radiation (underlying event)



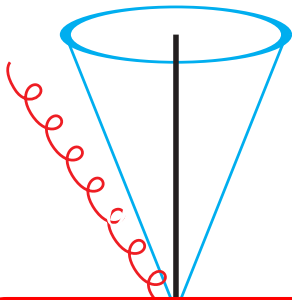
$$\langle \delta p_t \rangle \sim \text{Soft contents} \propto \text{jet area} \sim R^2$$

the coefficients depend on the algorithm

Optimisation: underlying idea

Competition between

- catching perturbative radiation

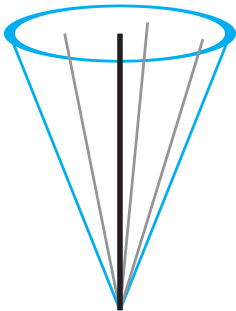


Out-of-cone radiation:

$$\langle \delta p_t \rangle \propto - \int_R \frac{d\theta}{\theta} \sim -\log(1/R)$$

What is the optimal jet definition (algo+ R !)?

- not catching soft content (mostly gluons)



$$\langle \delta p_t \rangle \sim \text{Soft contents} \propto \text{jet area} \sim R^2$$

the coefficients depend on the algorithm

Optimisation: dijet reconstruction

Example process to illustrate various effects:

$$Z' \rightarrow q\bar{q} \rightarrow 2 \text{ jets}$$

- $M_{Z'}$ can be varied (between 100 GeV and 4 TeV)
- Also valid for $H \rightarrow gg$ to study gluon jets
- Reconstruction method:
 - get the 2 hardest jets: j_1 and j_2
 - reconstruct the Z' : $m_{Z'} = (j_1 + j_2)^2$

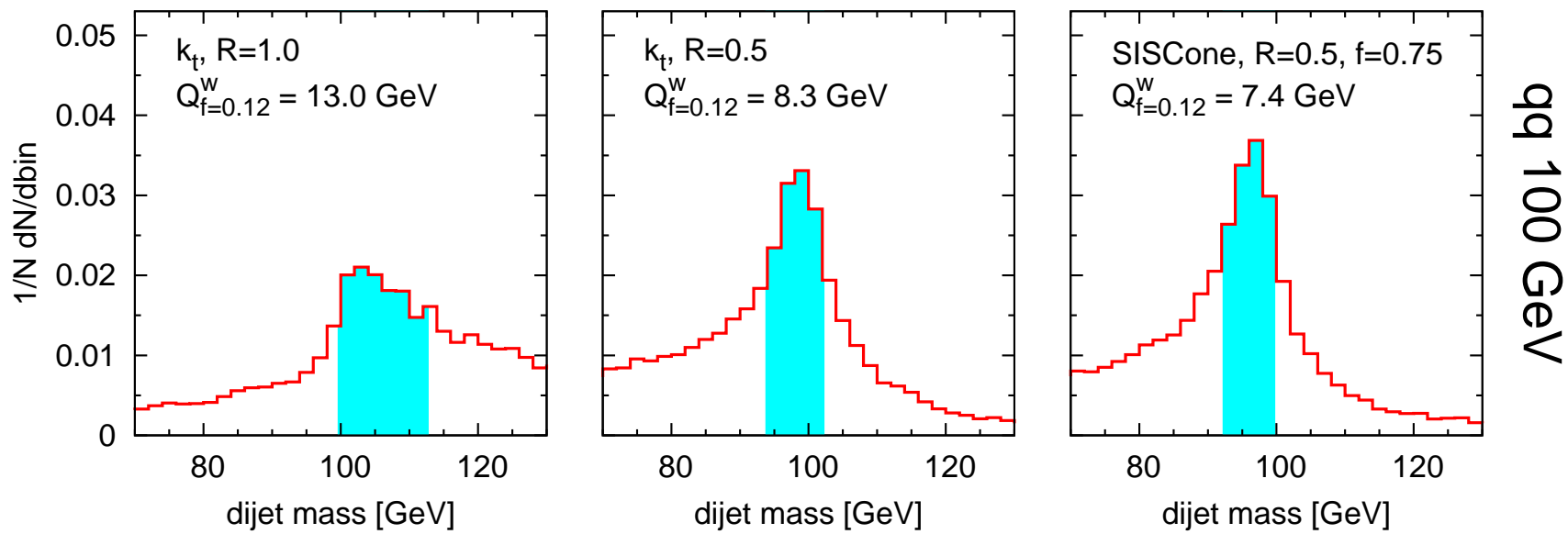
Look how the mass peak is reconstructed

- Also $t\bar{t}$ with full hadronic decay for multijet tests

Optimisation: quality measure (1)

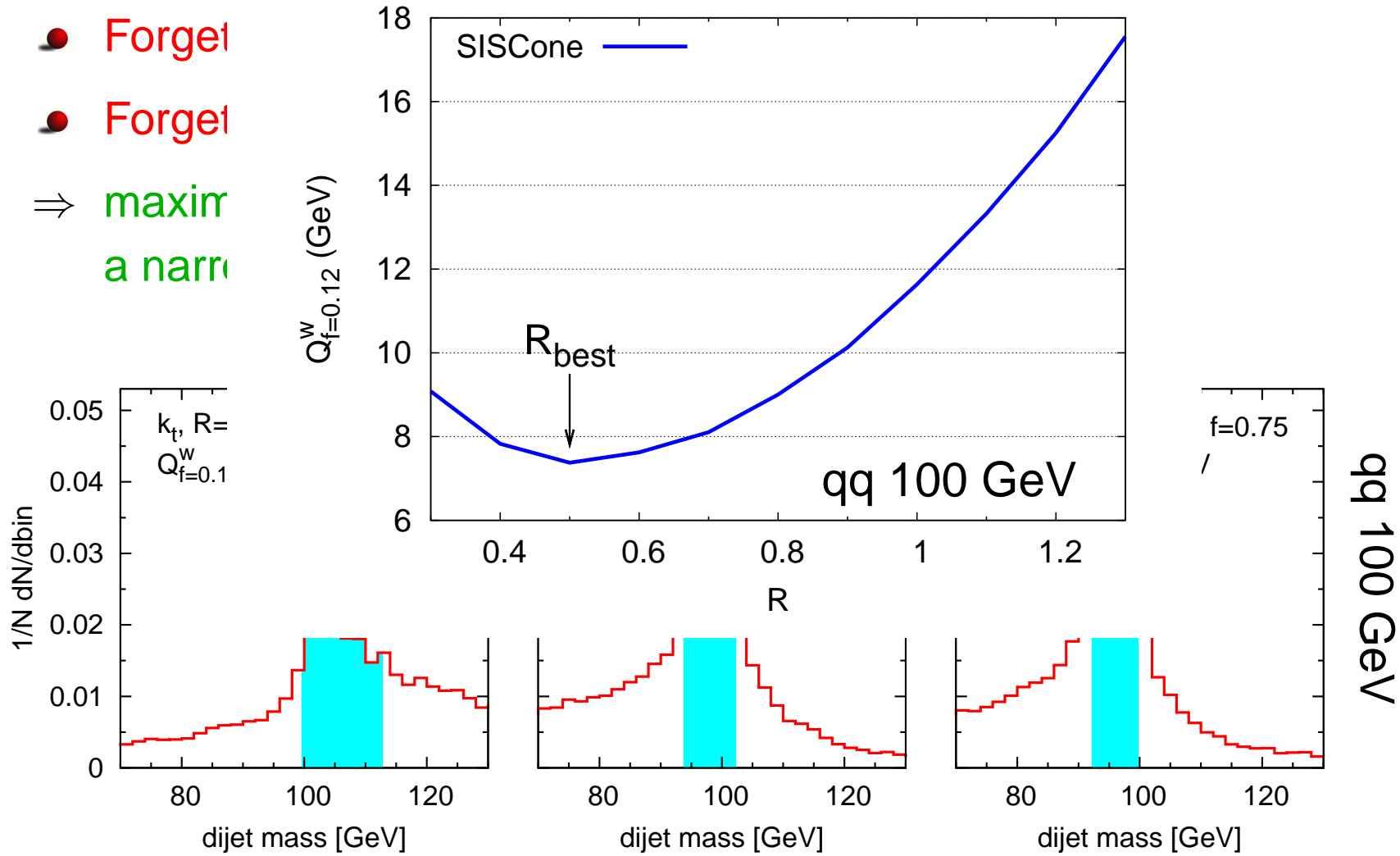
Measure of the jet reconstruction efficiency:

- Forget about measures related to parton-jet matching
 - Forget about fits depending on the shape of the peak
- ⇒ maximise the signal over background ratio (S/\sqrt{B})
a narrower peak is better.



Optimisation: quality measure (1)

Measure of the jet reconstruction efficiency:



Optimisation: quality measure (2)

Assuming a constant background,

quality measure \longrightarrow effective luminosity ratio

$$\rho_{\mathcal{L}}(\text{JD}_2/\text{JD}_1) = \frac{\mathcal{L} \text{ needed with JD}_2}{\mathcal{L} \text{ needed with JD}_1} = \frac{Q_{f=z}^w(\text{JD}_2)}{Q_{f=z}^w(\text{JD}_1)}$$

e.g. $\rho_{\mathcal{L}}(\text{JD}_2/\text{JD}_1) = 2$

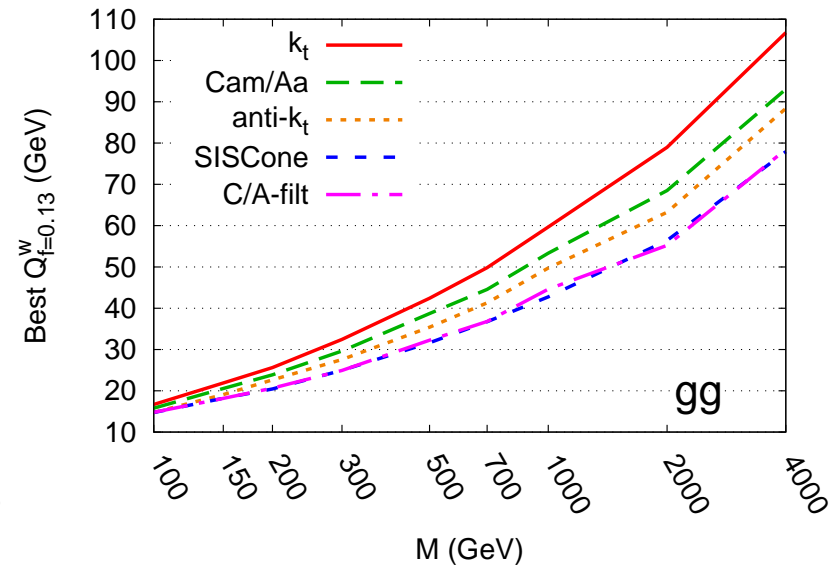
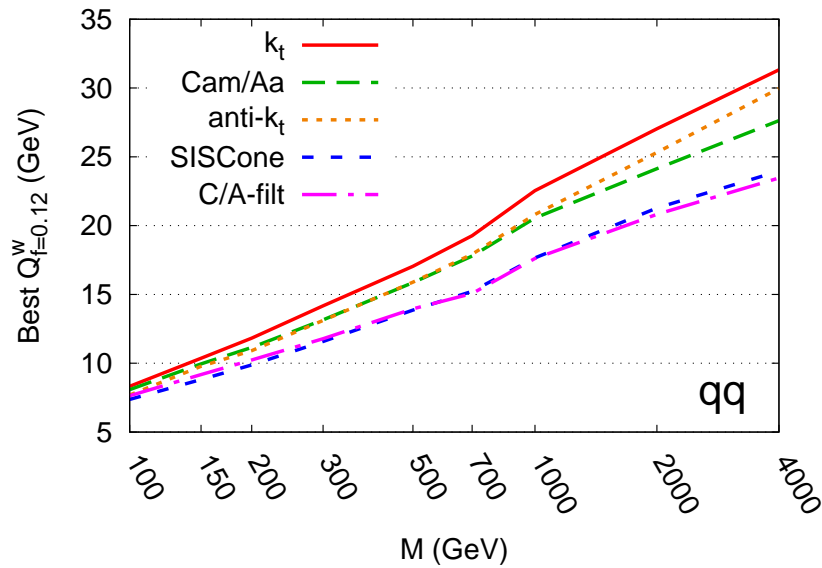
\Leftrightarrow JD_2 requires 2 times the integrated luminosity of JD_1
to achieve the same discriminative power.

Note: results cross-checked with 2 different definitions of the quality measure

Optimisation: best definition

[M.Cacciari, J.Rojo, G.Salam, GS, 08]

- **SISCone and C/A+filt.** do slightly better than k_t , C/A or anti- k_t

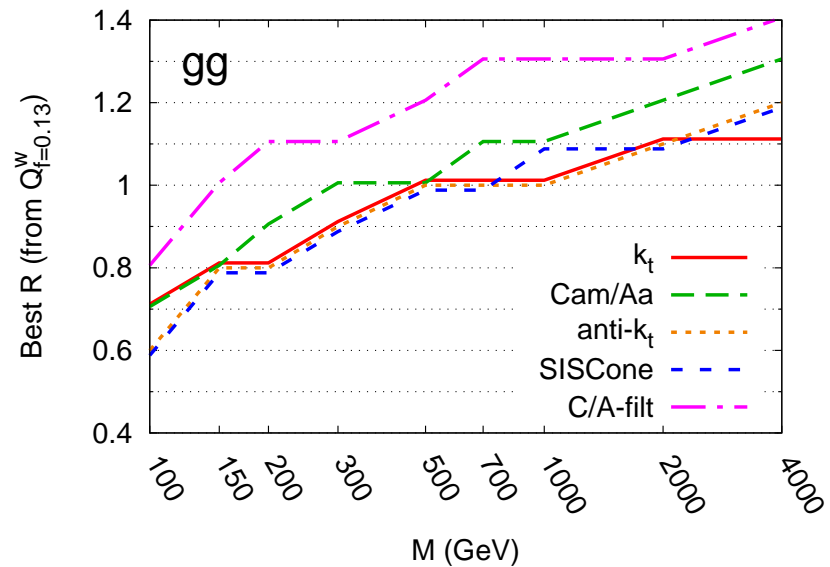
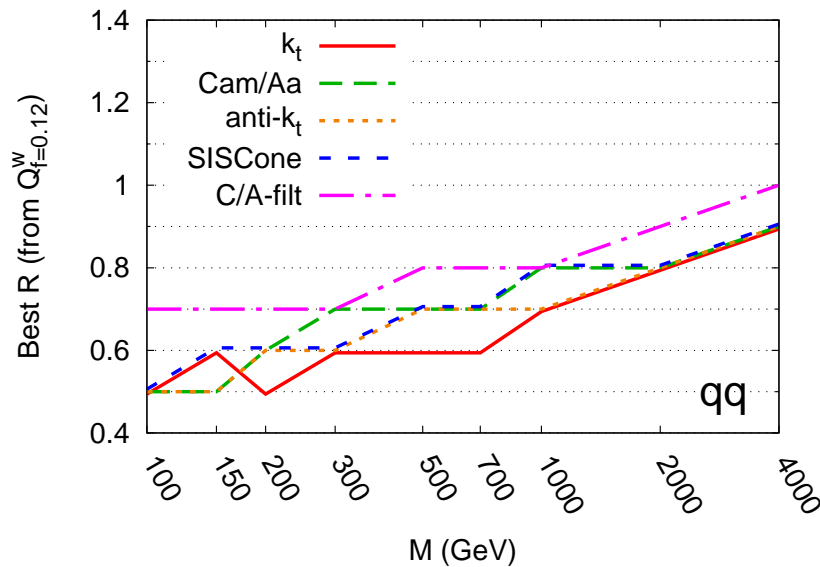


Optimisation: best definition

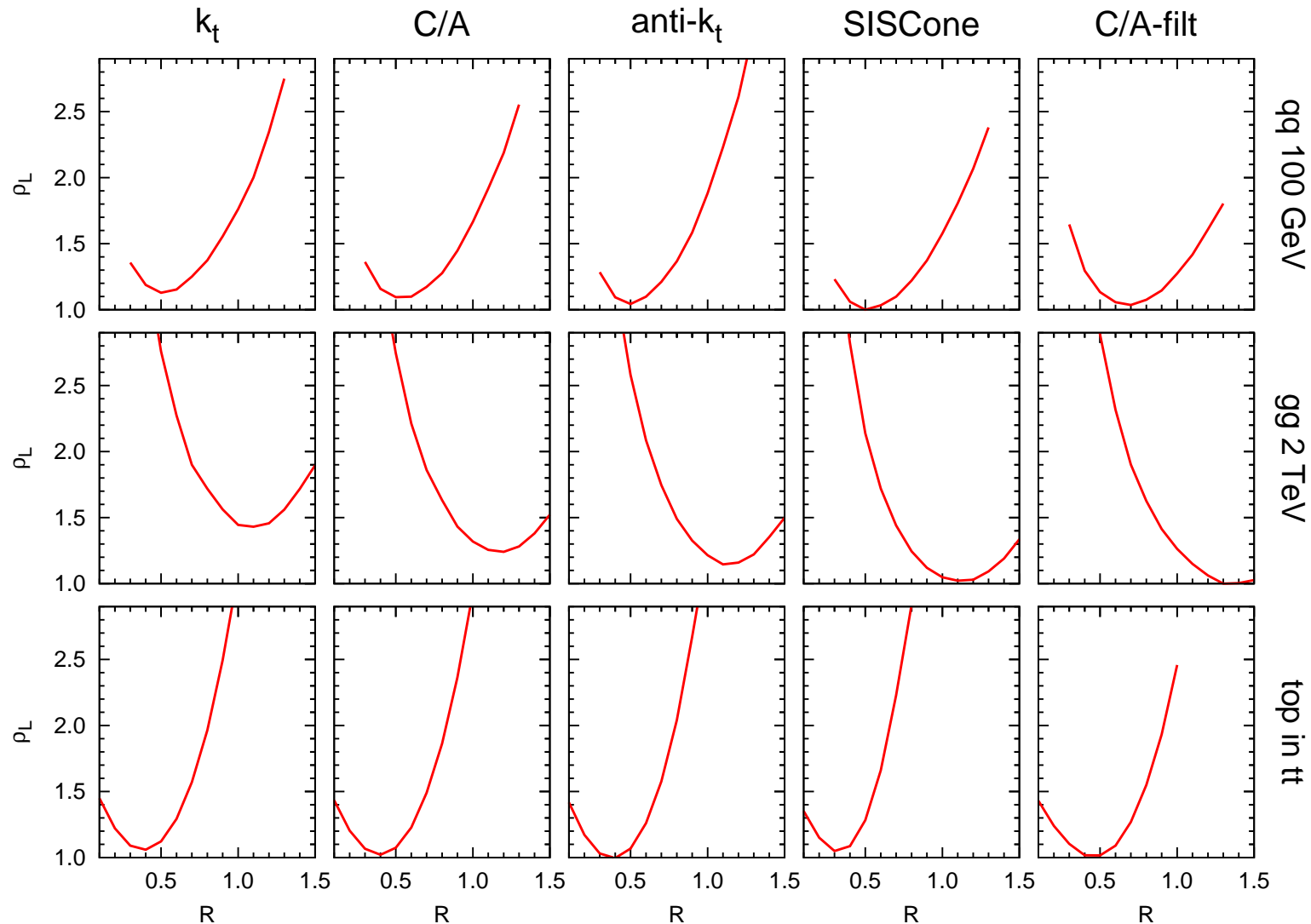
[M.Cacciari, J.Rojo, G.Salam, GS, 08]

● SIScone and C/A+filt. do slightly better than k_t , C/A or anti- k_t

● $M \nearrow \Rightarrow R_{\text{best}} \nearrow$ (and $R_{\text{best}}(g) > R_{\text{best}}(q)$)

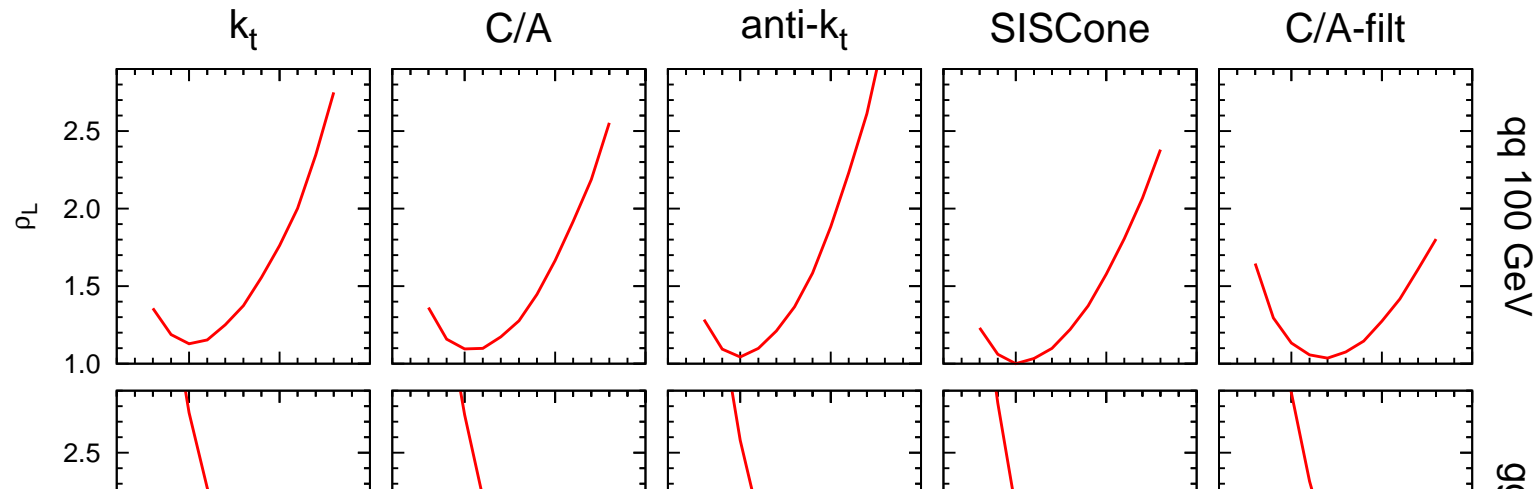


Optimisation: consequences



Using a single jet definition for all processes
may cost a factor ~ 2 in time for early discoveries at the LHC

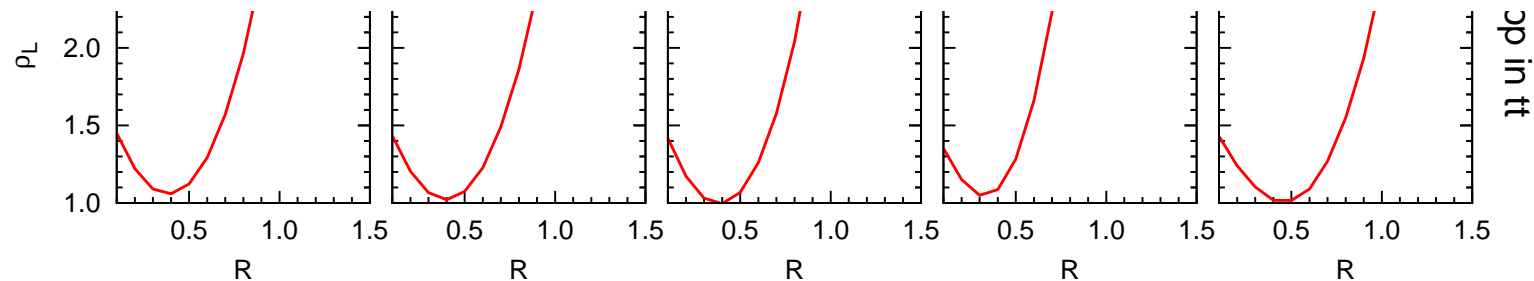
Optimisation: consequences



see

<http://quality.fastjet.fr>

for more



Using a single jet definition for all processes
may cost a factor ~ 2 in time for early discoveries at the LHC

New idea #3: jet area and soft background subtraction

[M.Cacciari, G.Salam, GS, 08]

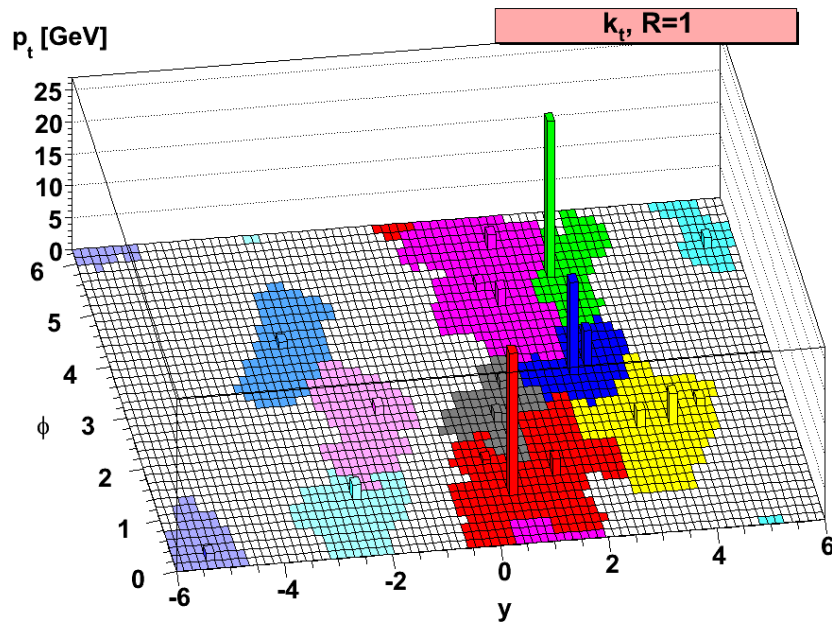
Area \equiv region where the jet catches soft particles

- Recipe: add infinitely soft particles (aka *ghosts*)
and see in which jet they are clustered
- 2 methods:
 - **Passive area**: add one ghost at a time and repeat many times
 - **Active area**: add a set of ghosts and cluster once
- Idea: ghost \approx background particle
 - \Rightarrow **active area \approx uniform background**
 - passive area \approx pointlike background**
- Notes:
 - passive = active for large multiplicities
 - require an IR-safe algorithm!
 - generic/universal definition (e.g. independent of a calorimeter)

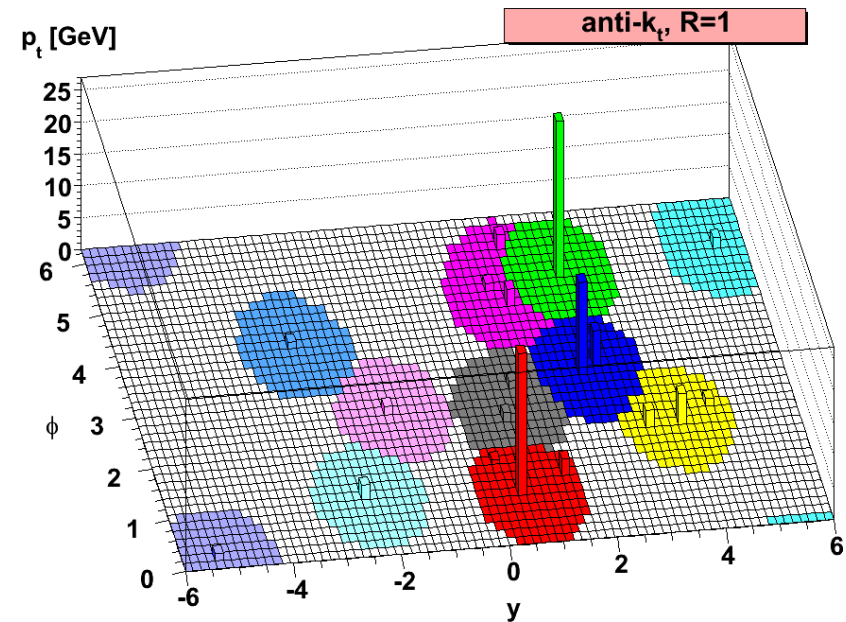
Jet area: examples

Example: active area for a simple event

k_t



anti- k_t



one ghost at every grid cell

Note: analytic control

Example: perturbative expansion of areas (at order α_s)

$$\langle \mathcal{A}(p_t, R) \rangle = \mathcal{A}_0 + \frac{C_{F,A}}{b_0 \pi} \pi R^2 d \log \left(\frac{\alpha_s(Q_0)}{\alpha_s(Rp_t)} \right)$$

- area $\neq \pi R^2$, area $\neq \text{const.}$

- coefficients computable

	$\mathcal{A}_0/(\pi R^2)$		d	
	passive	active	passive	active
k_t	1	0.81	0.56	0.52
Cam/Aachen	1	0.81	0.08	0.08
anti- k_t	1	1	0	0
SISCone	1	1/4	-0.06	0.12

- $Q_0 \equiv \text{IR regulator} \propto \text{background density}$

Pileup subtraction (for uniform backgrounds)

Basic idea: [M.Cacciari, G.Salam, 08]

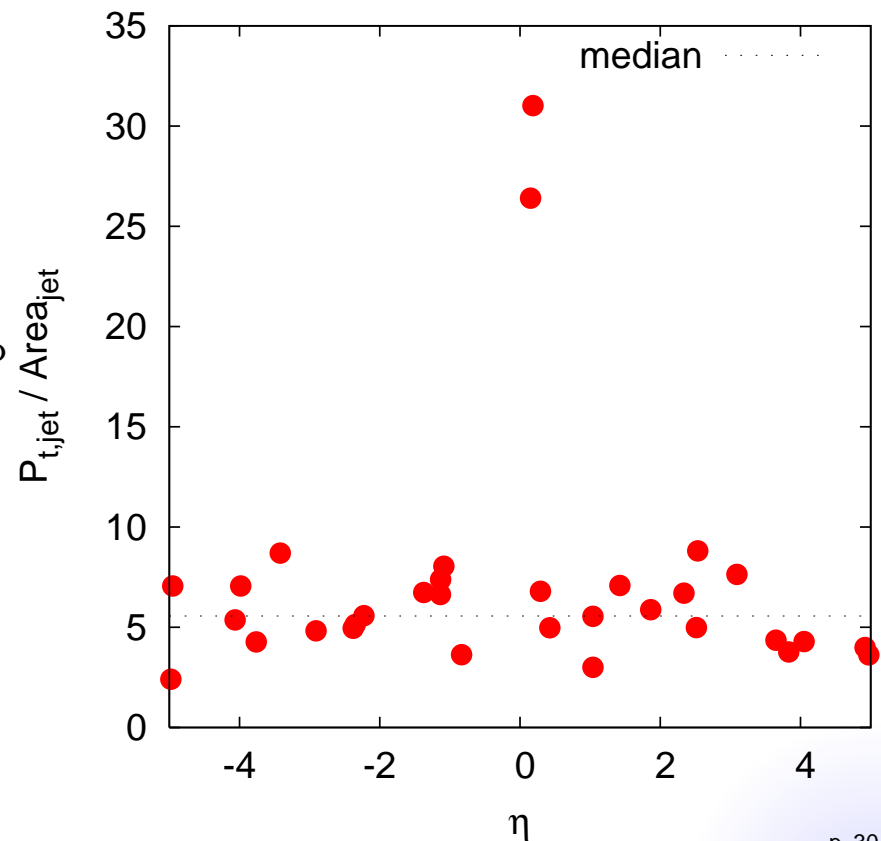
$$p_{t,\text{subtracted}} = p_{t,\text{jet}} - \rho_{\text{pileup}} \times \text{Area}_{\text{jet}}$$

• Jet area: [M.Cacciari, G.Salam, G.S., 08]

- region where the jet catches infinitely soft particles (active/passive)
- analytic control and understanding in pQCD

• Pileup density per unit area: ρ_{pileup}

e.g. estimated from the median
of $p_{t,\text{jet}} / \text{Area}_{\text{jet}}$



Pileup subtraction (for uniform backgrounds)

Basic idea: [M.Cacciari, G.Salam, 08]

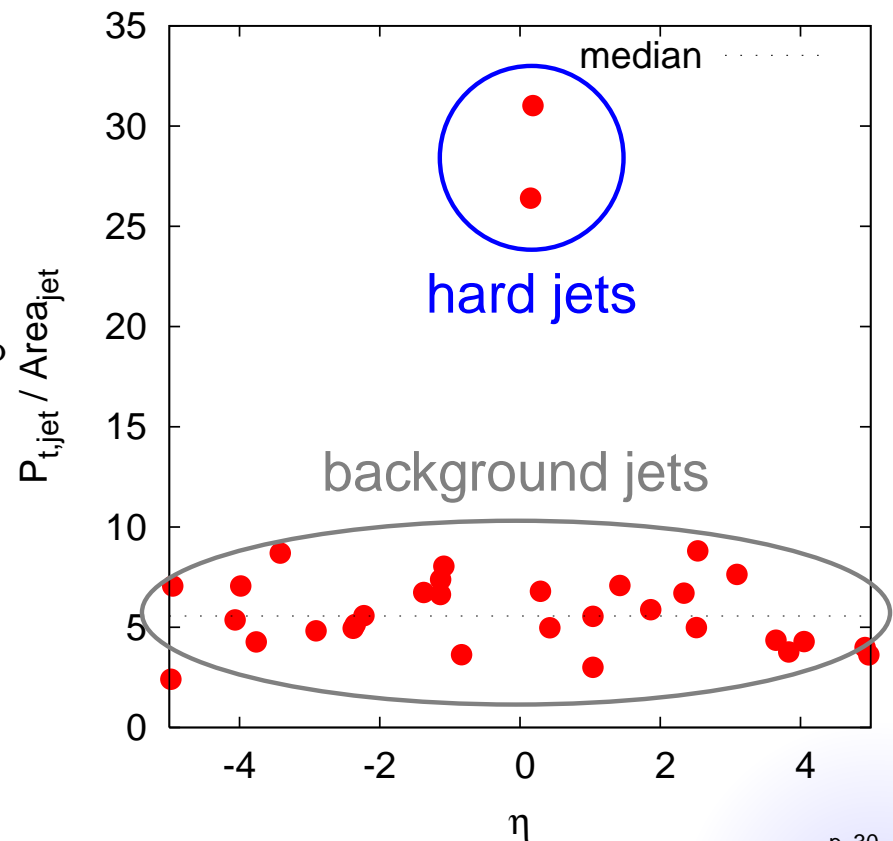
$$p_{t,\text{subtracted}} = p_{t,\text{jet}} - \rho_{\text{pileup}} \times \text{Area}_{\text{jet}}$$

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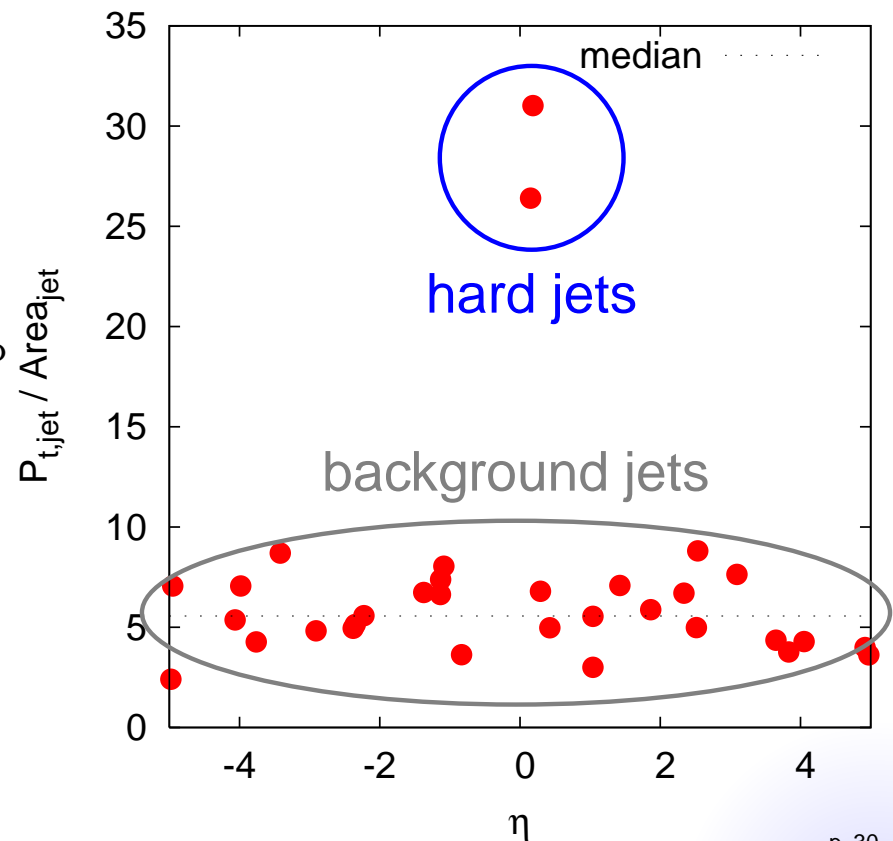
● Jet area: [M.Cacciari, G.Salam, G.S., 08]

- region where the jet catches infinitely soft particles (active/passive)
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● Pileup density per unit area: ρ_{pileup}

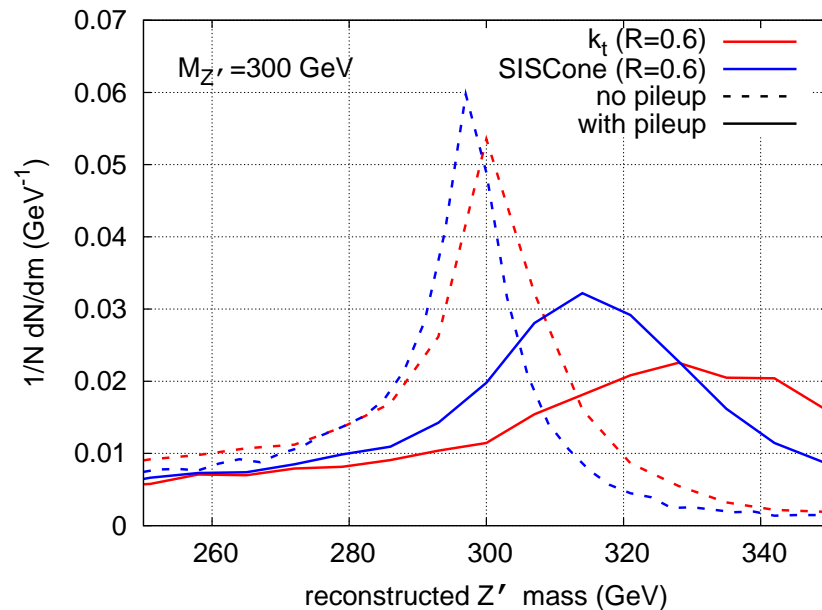
e.g. estimated from the median
of $p_{t,\text{jet}} / \text{Area}_{\text{jet}}$

implemented in FastJet
on an event-by-event basis



Effect on dijet reconstruction

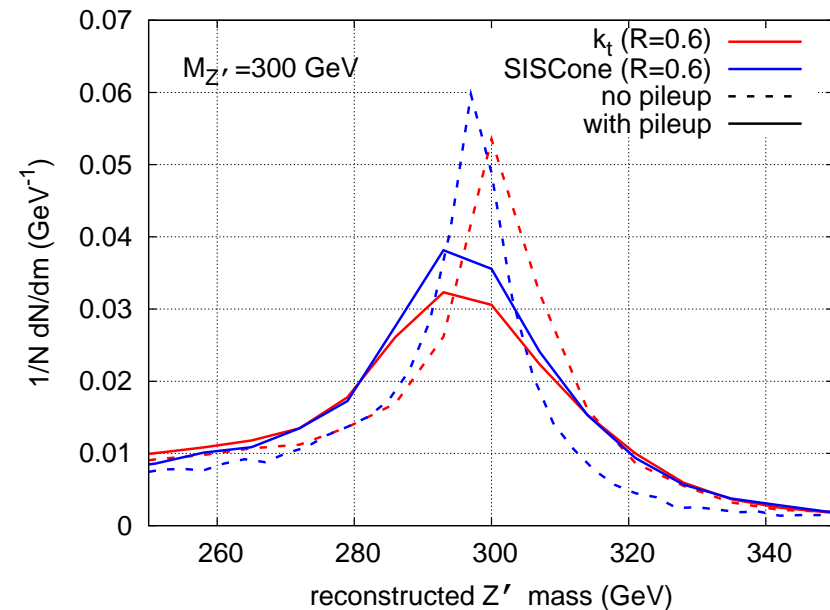
Pileup unsubtracted



width = 29.5 GeV

width = 21.0 GeV

pileup subtracted



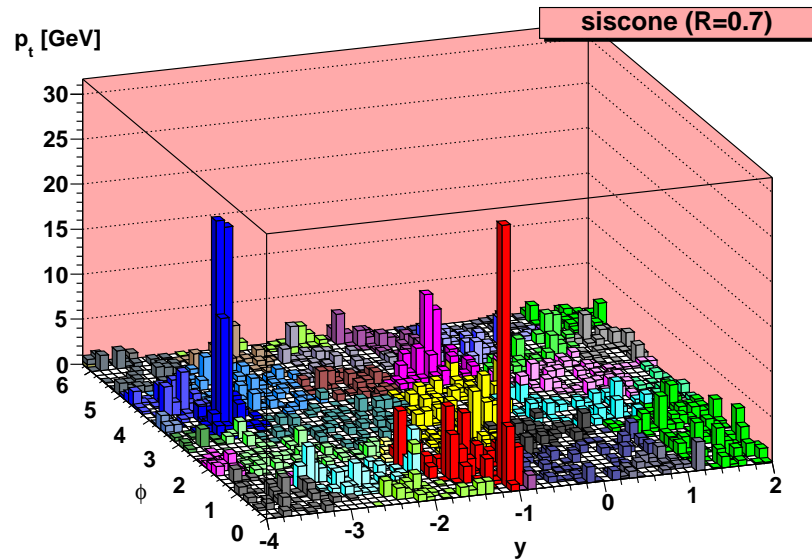
width = 21.0 GeV

width = 17.7 GeV

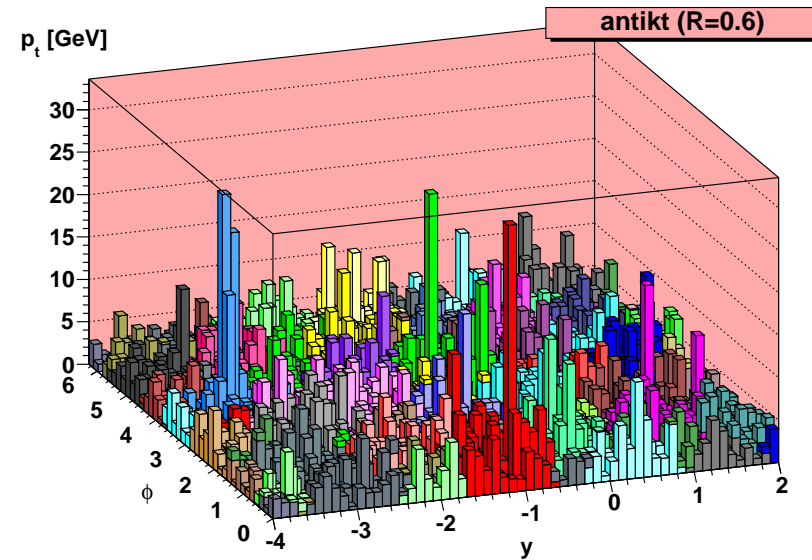
- ✓ position reasonable
- ✓ dispersion reduced (thanks to the event-by-event approach)
- ✓ used by STAR for the first jet analysis in heavy-ions

Example: application to HI collisions

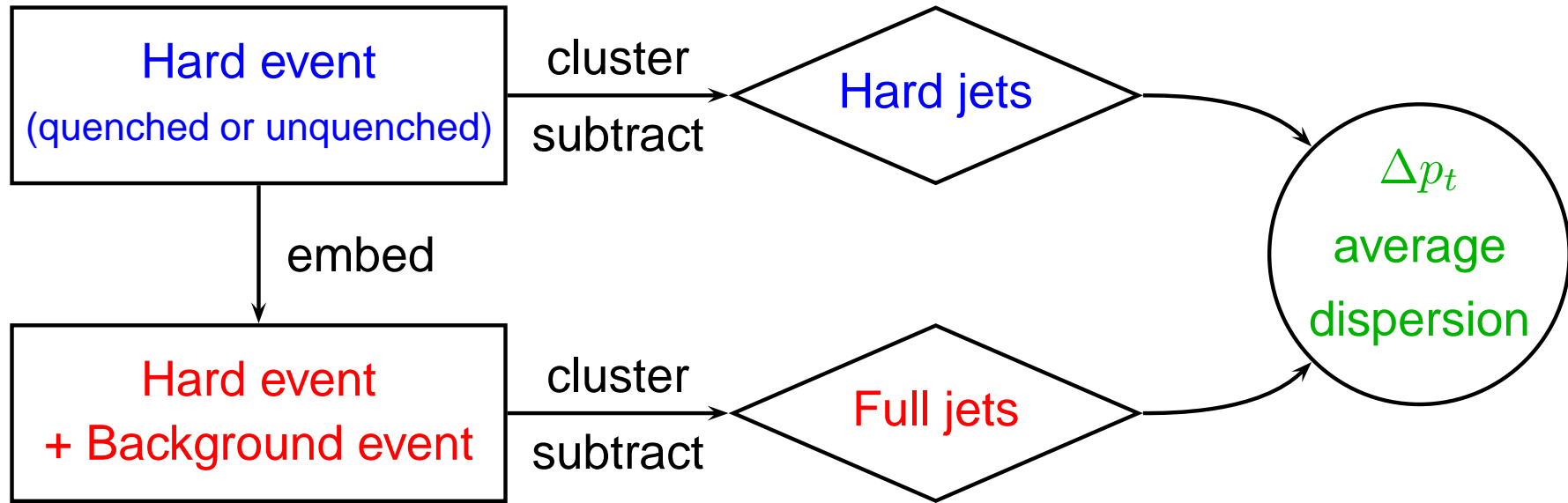
pp + pileup



AA

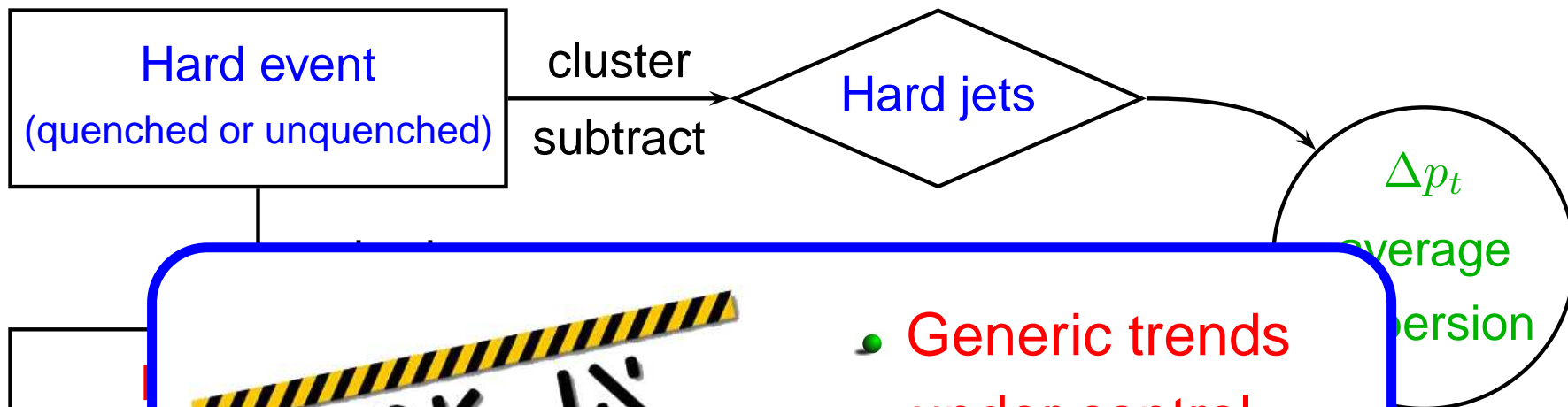


Framework for study



- **Hard event:** Pythia(v6.4) or Pythia(v6.4)+PyQuen(v1.5)
- **Background:** Hydjet(v1.5) (others under study)
- **Analysis:** FastJet(v2.4)
Ideally: smallest Δp_t shift, smallest Δp_t dispersion
- Note: in what follows, R fixed to 0.4

Framework for study



+ Ba



- Generic trends under control
- Final numbers may change

[M.Cacciari, J.Rojo, G.Salam, GS, in prep.]

- Analysis: FastJet(v2.4)

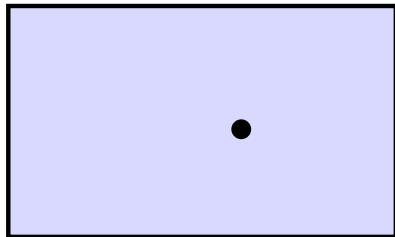
Ideally: smallest Δp_t shift, smallest Δp_t dispersion

- Note: in what follows, R fixed to 0.4

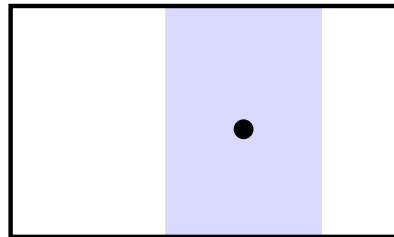
Idea #1: use a local range to compute ρ_{bkg}

- Fluctuating background
 - determine the background density ρ_{bkg} from jets in the vicinity of the jet we want to subtract

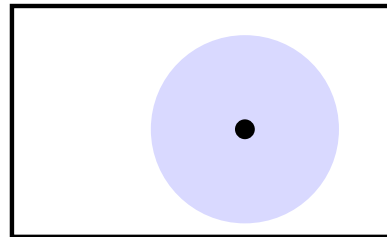
global



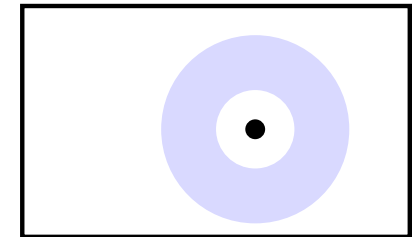
StripRange



CircularRange

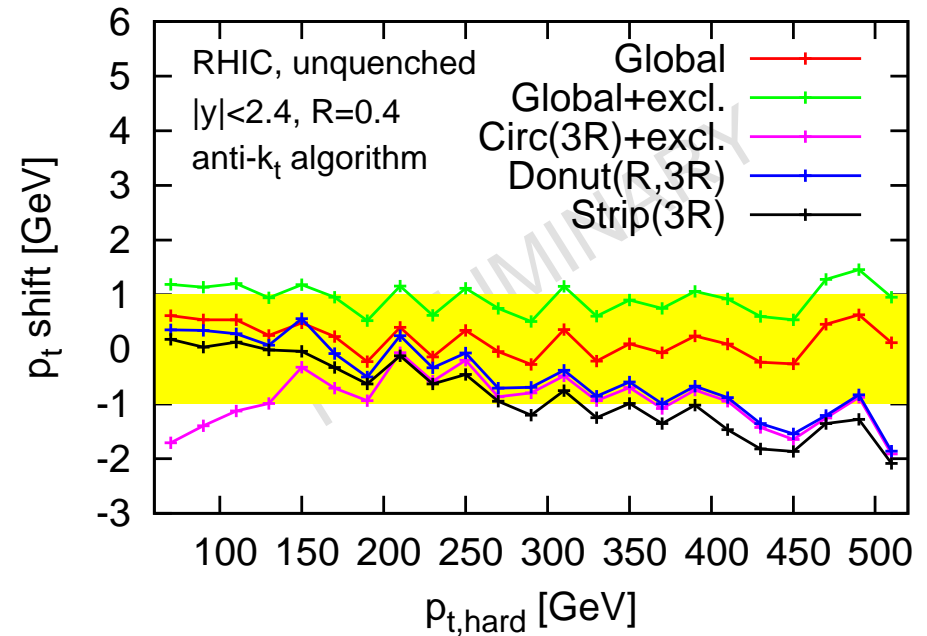
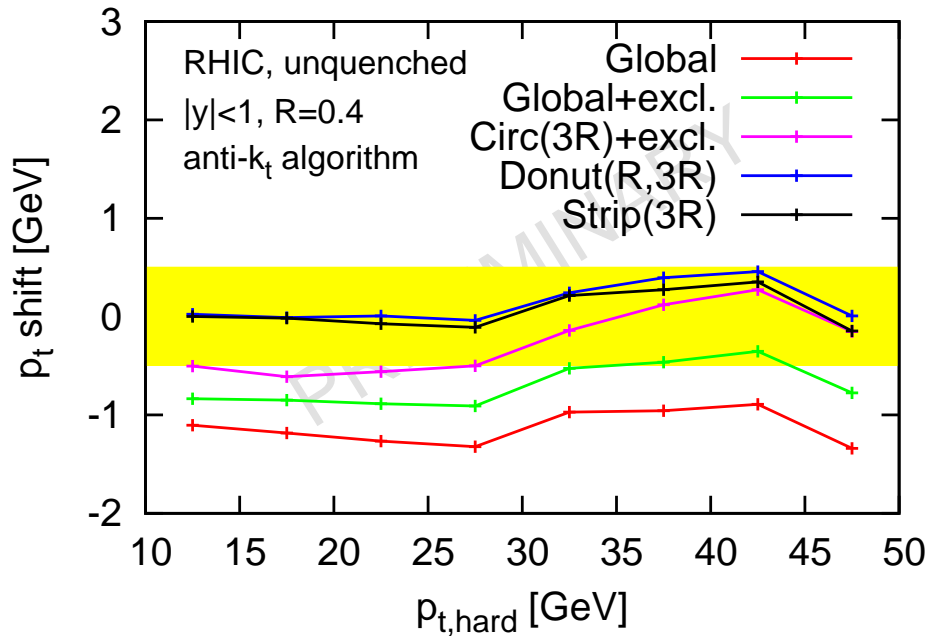


DoughnutRange



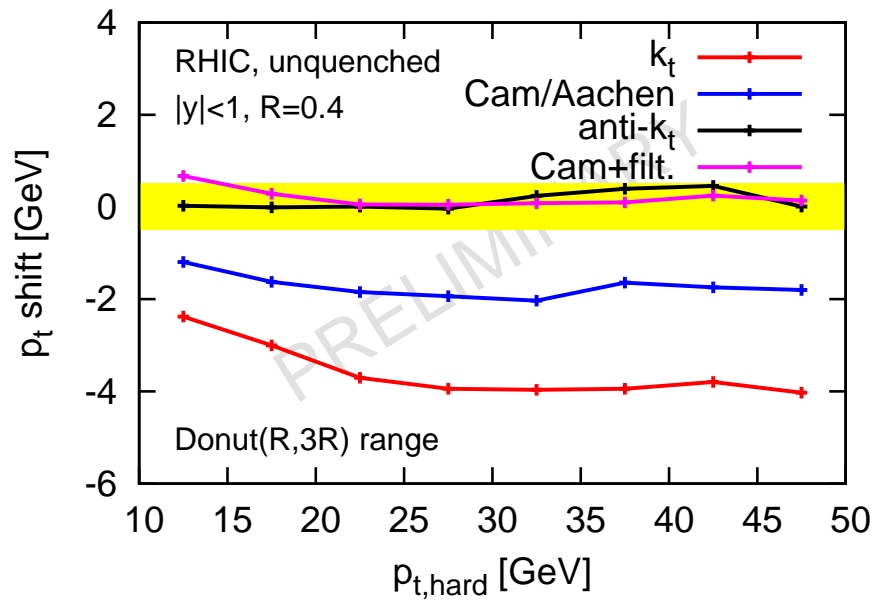
- Exclude the hardest jets from the determination of ρ_{bkg}
 - ⇒ reduce the bias in the computation median

Effect of choosing a local range



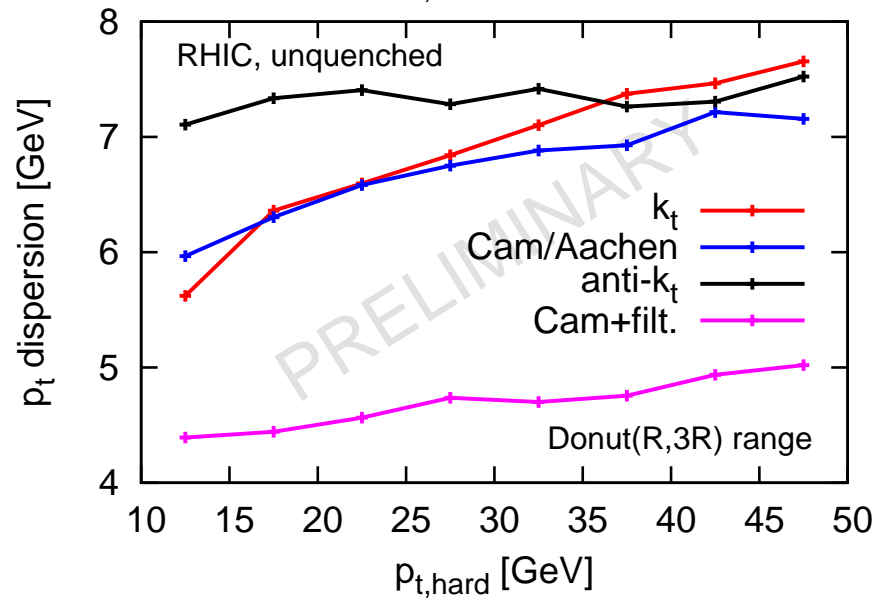
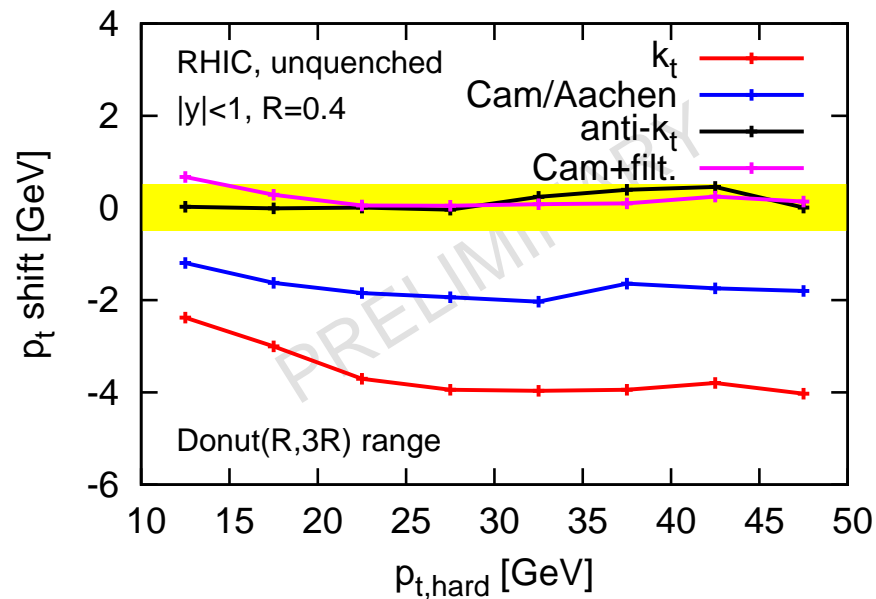
- effect $\sim 0.5-1$ GeV
- differences between local ranges \longrightarrow uncertainty
- for limited acceptance, global range \approx local range
- analytic control would be nice

Results: RHIC kinematics



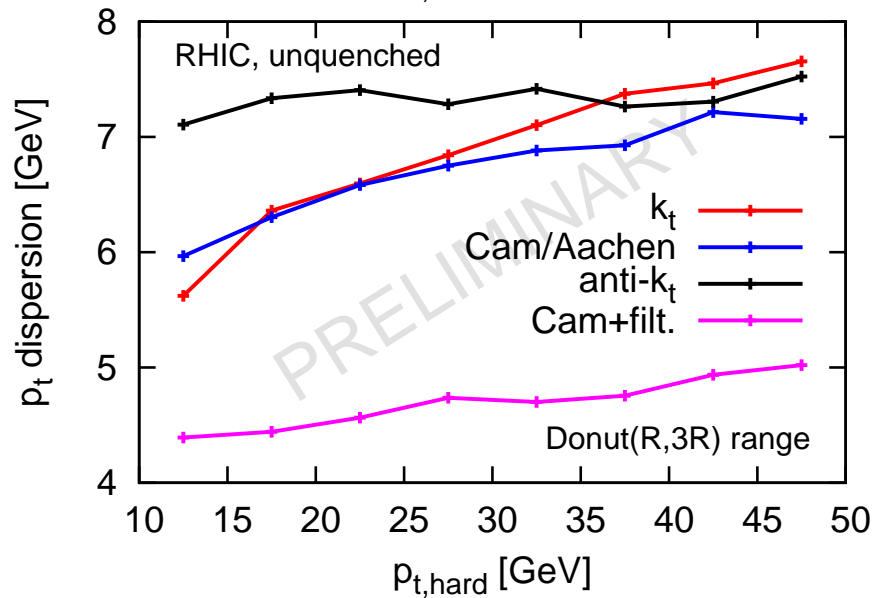
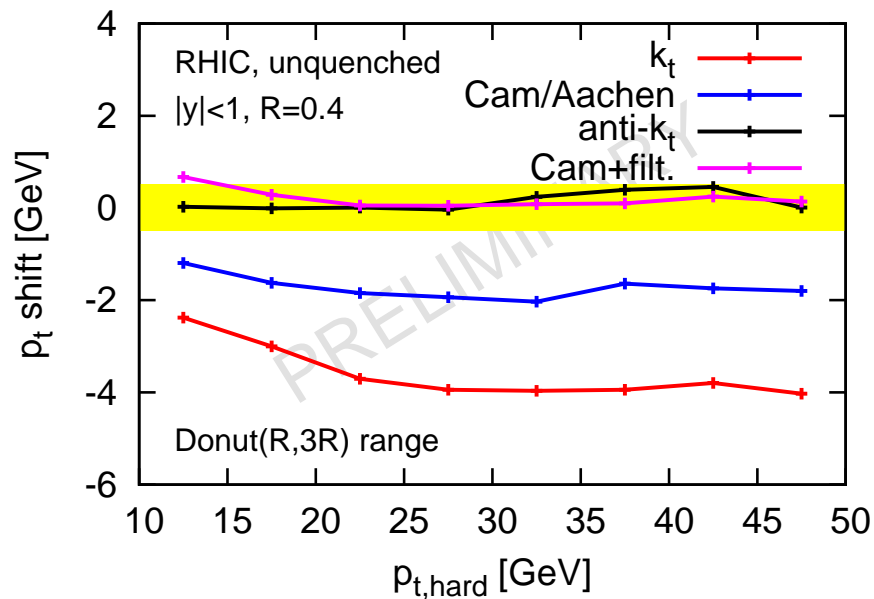
- average p_t shift:
anti- k_t and Cam+filt. Ok

Results: RHIC kinematics

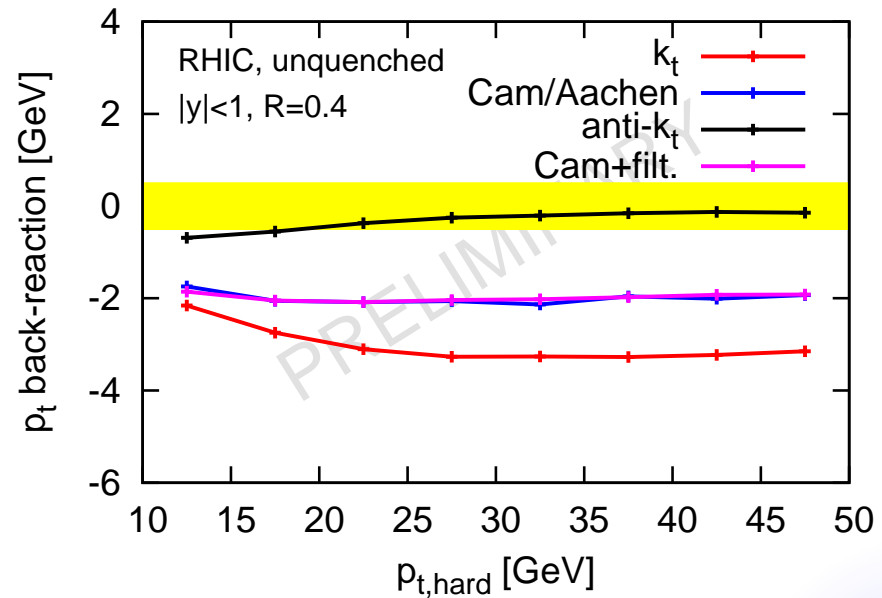


- average p_t shift:
anti- k_t and C/A+filt. Ok
- p_t shift dispersion:
C/A+filt. better

Results: RHIC kinematics

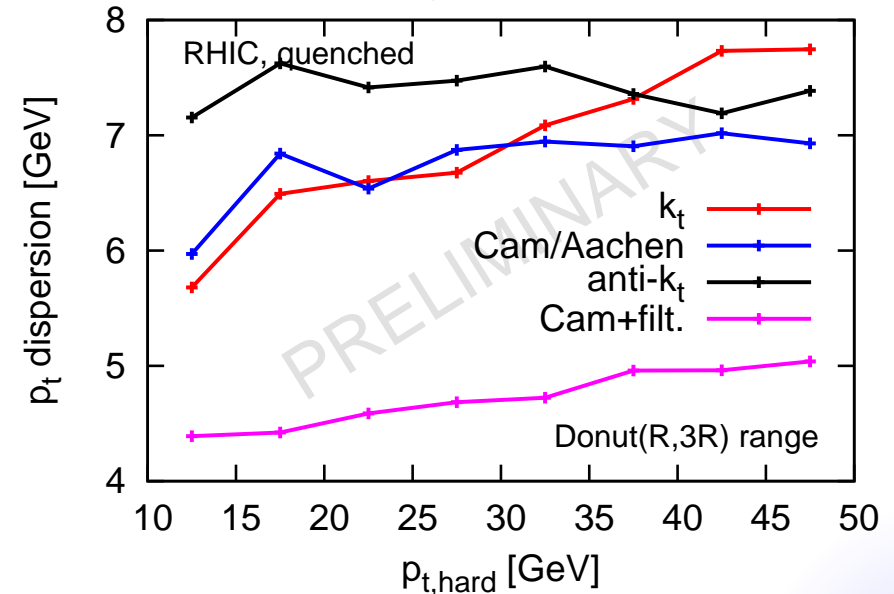
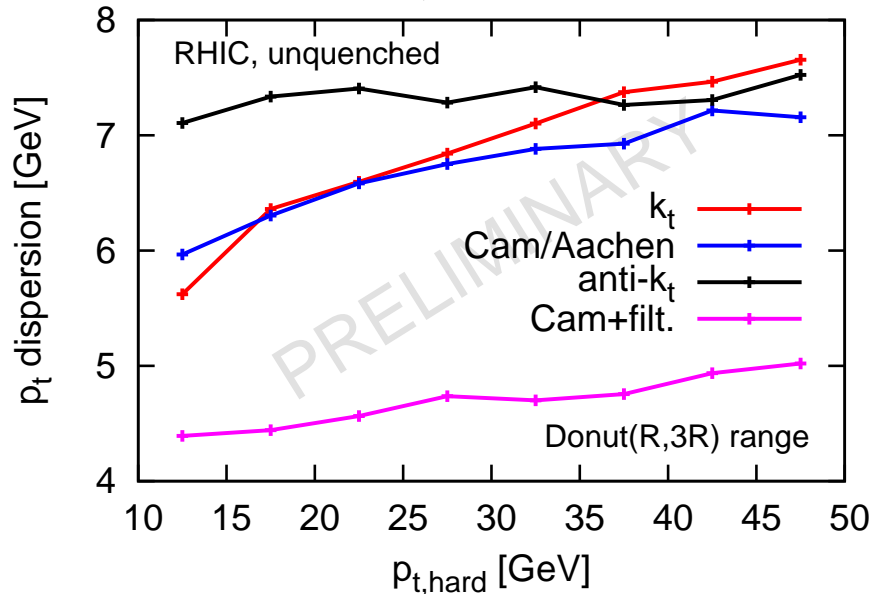
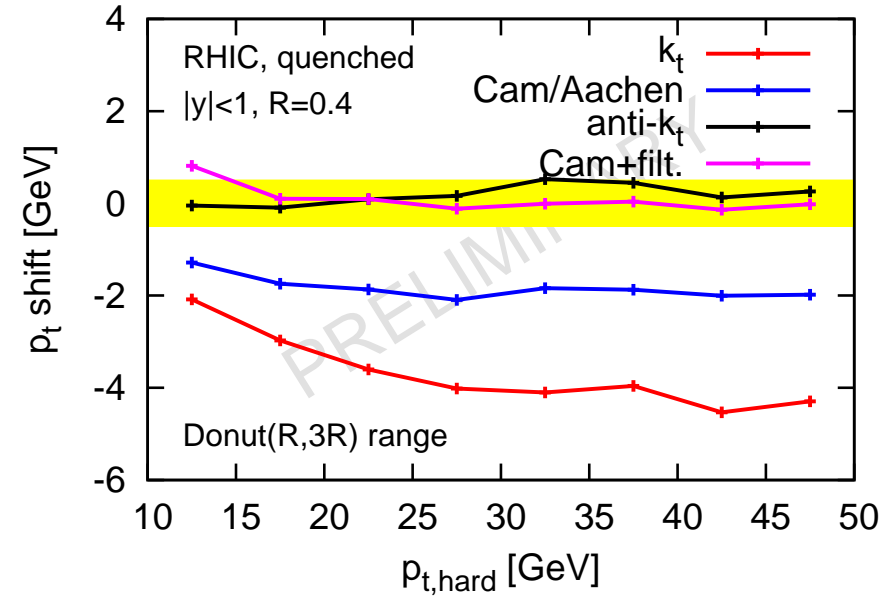
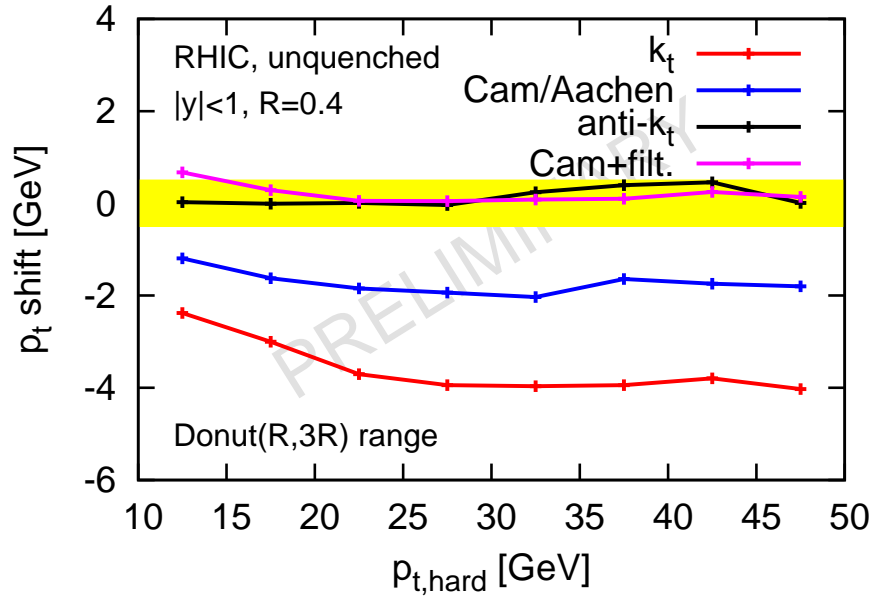


- average p_t shift:
anti- k_t and C/A+filt. Ok
- p_t shift dispersion:
C/A+filt. better
- watch out C/A+filt. average:
back-reaction compensated

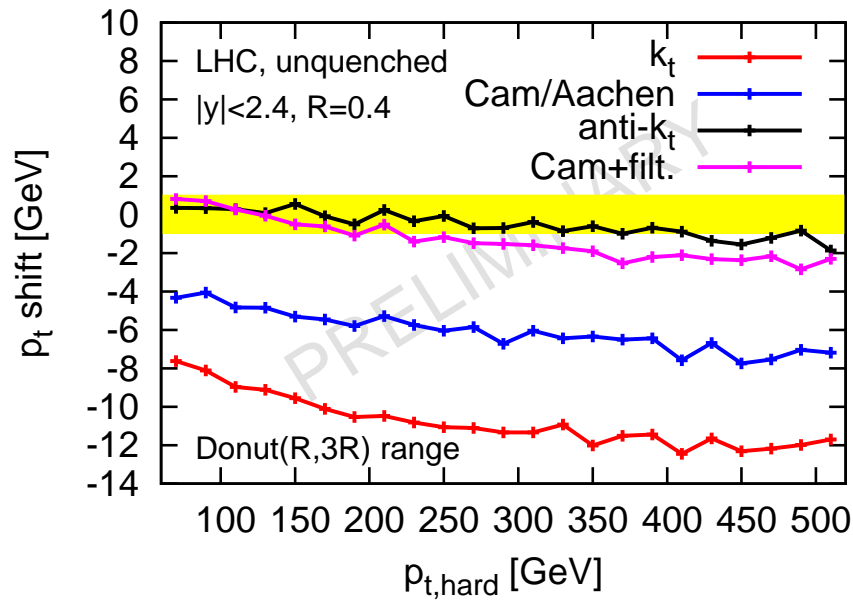


Results: RHIC kinematics – quenching

Performances not much affected by quenching (need more models)

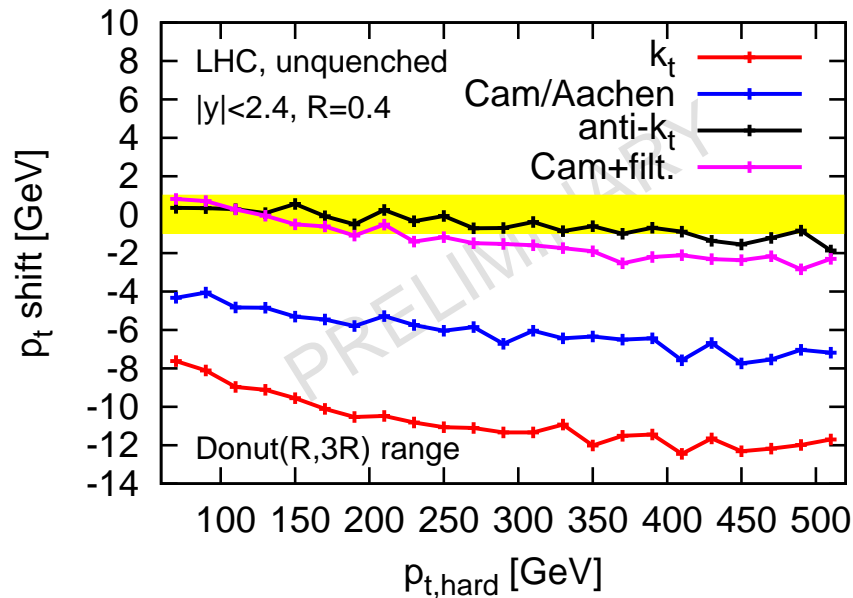


Results: LHC kinematics

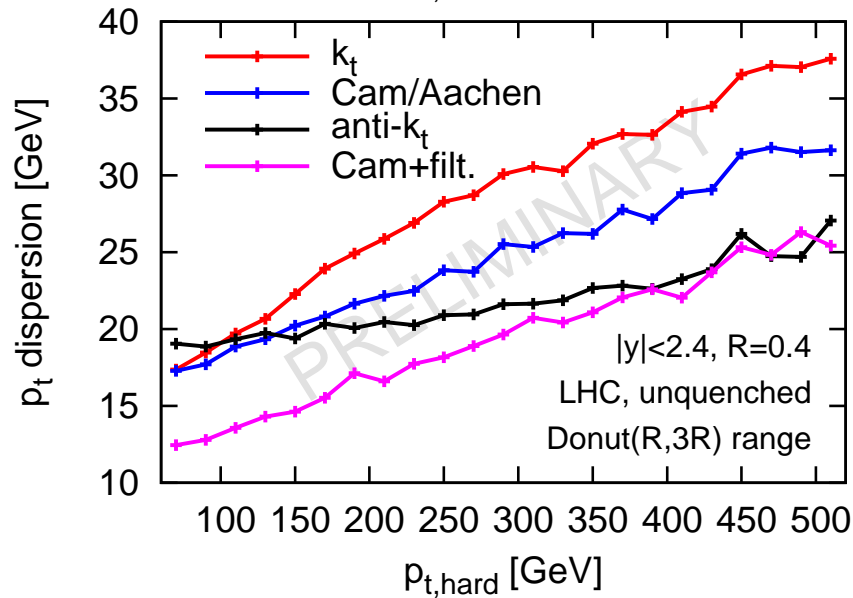


- average p_t shift:
anti- k_t and C/A+filt. Ok

Results: LHC kinematics



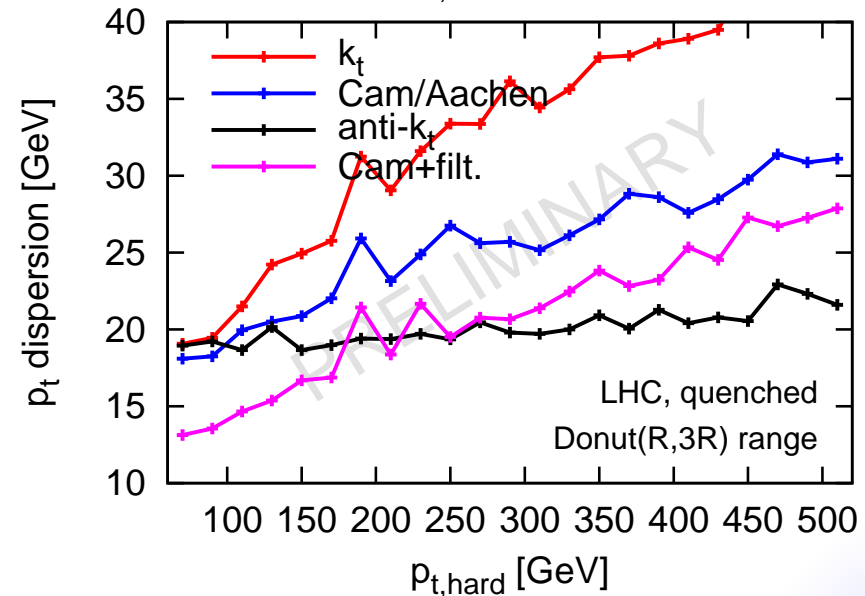
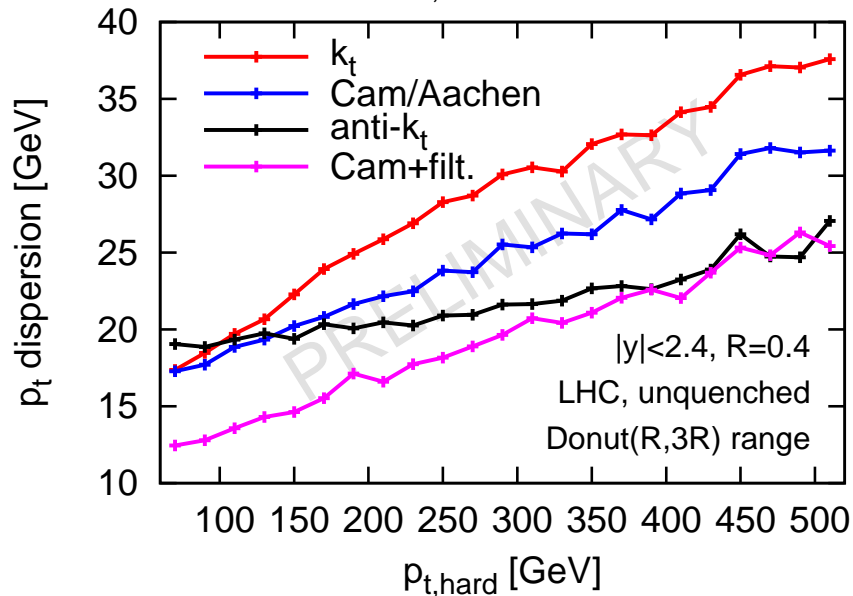
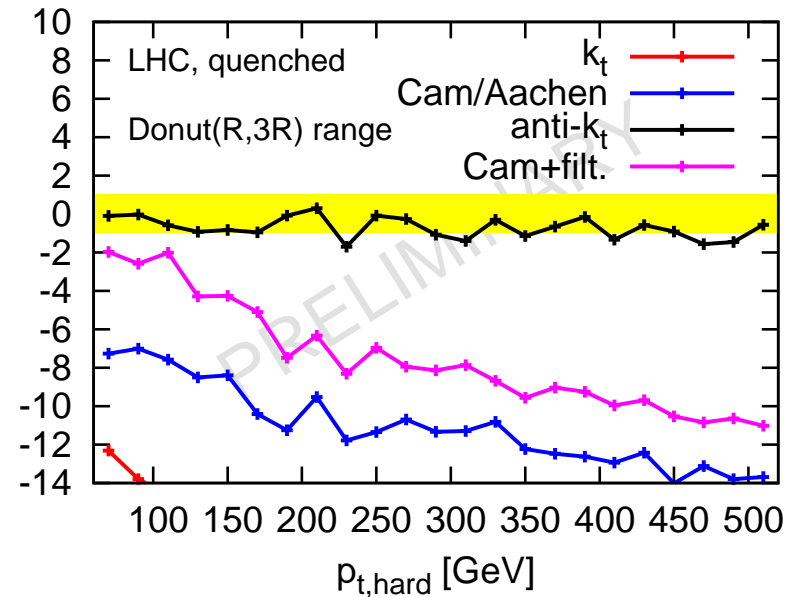
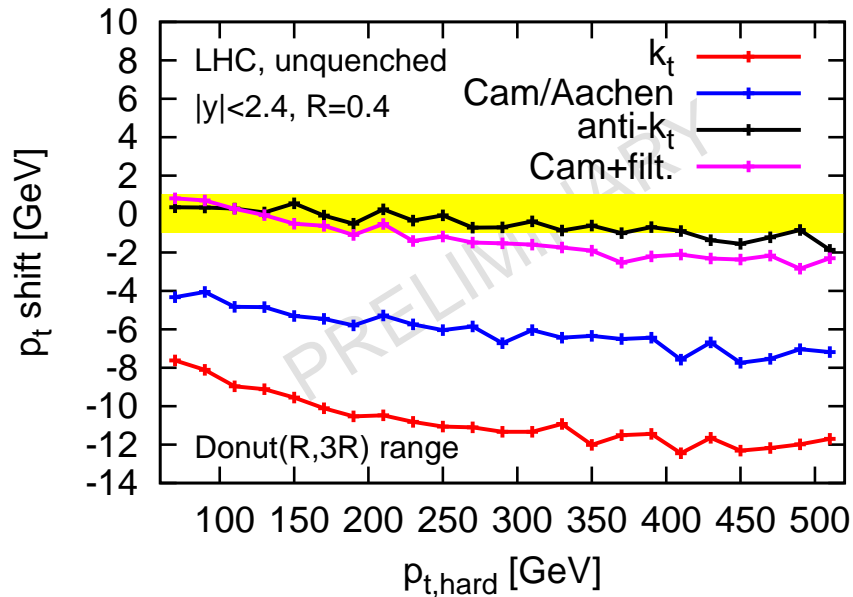
- average p_t shift:
anti- k_t and C/A+filt. Ok



- p_t shift dispersion:
C/A+filt. better
anti- k_t Ok

Results: LHC kinematics – quenching

Large quenching effect but anti- k_t 's rigidity plays for it



Summary (1)

Message #1:

Use infrared-and-collinear-safe algorithms

ATLAS Cone CDF/D0 MidPoint	} →	SISCone	✓ fast ✓ safe
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CMS It. Cone	→	anti- k_t	✓ fast ✓ safe
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Important to benefit fully from pQCD multilegs/multiloops calculations

Summary (2)

Message #2:

correct tools \Rightarrow new ideas, new concepts
 \Rightarrow new generation of jet definitions

- jet areas \longrightarrow pileup and HI background subtraction
- jet substructure improves reconstruction (Higgs, top, SUSY, ...)

Message #3:

keep some flexibility in the jet definition choice

- optimisation \longrightarrow luminosity gains for LHC searches
- different approaches \longrightarrow better understanding of HI collisions

backup slides

The SIScone search for stable cones

- Solution: use a seedless approach, find **ALL** stable cones
- Naive approach: check stability of each subset of particle

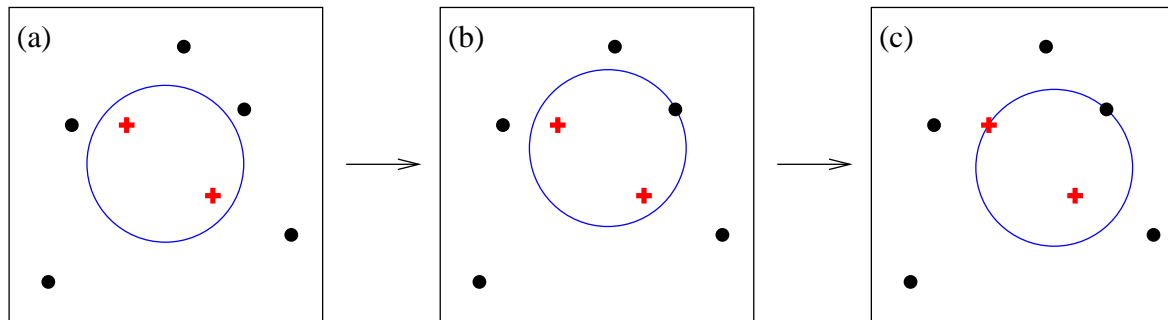
The SIScone search for stable cones

- Solution: use a seedless approach, find **ALL** stable cones
- Naive approach: check stability of each subset of particle
Complexity is $\mathcal{O}(N2^N)$
 \Rightarrow **definitely unrealistic: 10^{17} years for $N = 100$**
- Midpoint complexity: $\mathcal{O}(N^3)$

The SIScone search for stable cones

- Solution: use a seedless approach, find **ALL** stable cones
- Midpoint complexity: $\mathcal{O}(N^3)$

Idea: use geometric arguments



- Each enclosure can be moved (in any dir.) until it touches a point
- ... then rotated until it touches a second one

⇒ Enumerate all pairs of particles
with 2 circle orientations and 4 possible inclusion/exclusion
→ find all enclosures

The SIScone search for stable cones

- Solution: use a seedless approach, find **ALL** stable cones
- Midpoint complexity: $\mathcal{O}(N^3)$

Idea: use geometric arguments

⇒ Enumerate all pairs of particles
with 2 circle orientations and 4 possible inclusion/exclusion
→ find all enclosures

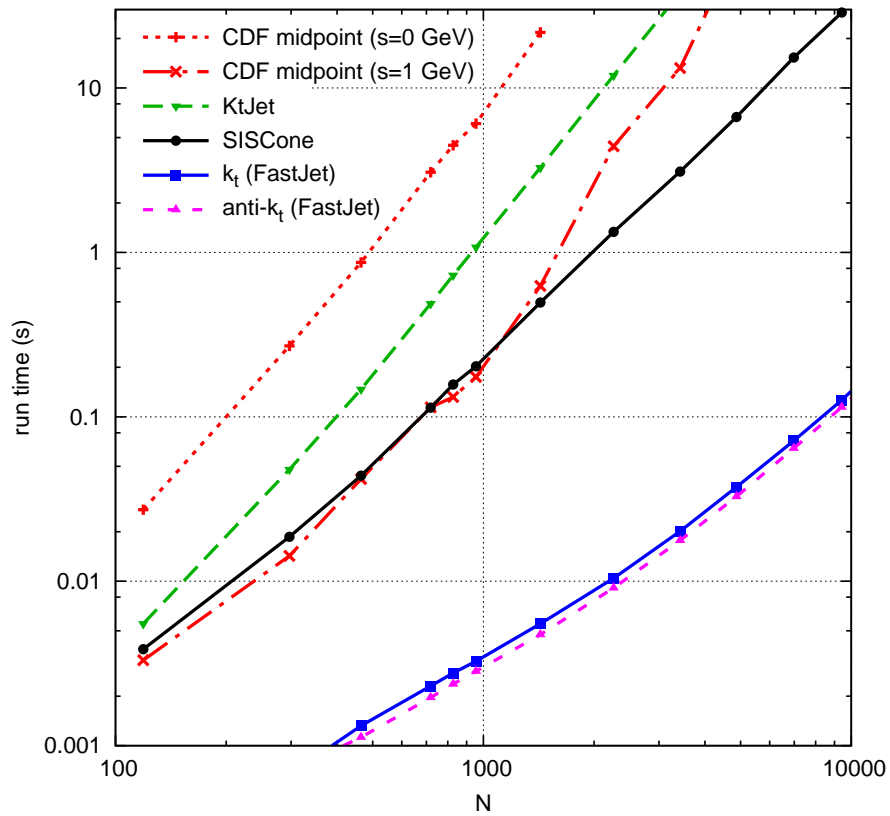
- Complexity: $\mathcal{O}(N^3)$, with improvements: $\mathcal{O}(N^2 \log(N))$

→ C++ implementation: Seedless Infrared-Safe Cone algorithm (SIScone)
G.Salam, G.S., JHEP 04 (2007) 086; <http://projects.hepforge.org/siscone>

NB.: also available from FastJet

[M.Cacciari, G.Salam, G.S.]; <http://www.fastjet.fr>

Algorithm timings



- Recombination algorithms very fast

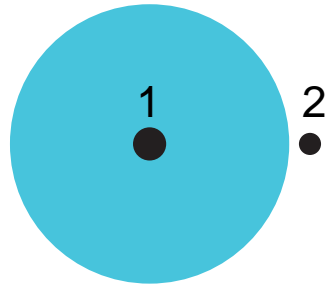
[M. Cacciari, G. Salam, 06]

- SISCone not slower than Midpoint (even with a 1 GeV seed threshold)

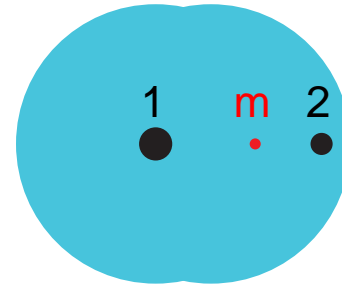
A technical point: Back-reaction

Additional soft background has 2 effects:

- Throw soft particles in the hard jet: dealt with by subtraction
- Modify the hard scattering (back-reaction)
 - can be pointlike or diffuse
 - gain:

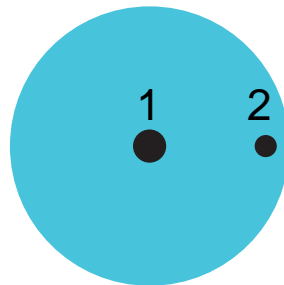


no medium: $p_t = p_{t1}$

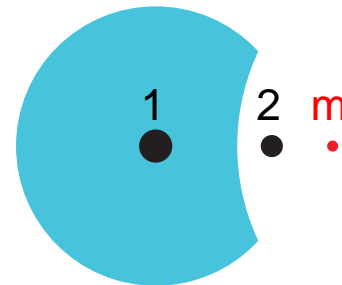


medium: $p_t = p_{t1} + p_{t2} + p_{tm}$

- loss:



no medium: $p_t = p_{t1} + p_{t2}$



medium: $p_t = p_{t1} + p_{tm}$

A technical point: Back-reaction

Additional soft background has 2 effects:

- Throw soft particles in the hard jet: dealt with by subtraction
- Modify the hard scattering (back-reaction)
 - can be pointlike or diffuse
 - tractable analytically (similar to areas)
 - $k_t \gtrsim \text{Cambridge} > \text{SISCone} \gg \text{anti-}k_t$

